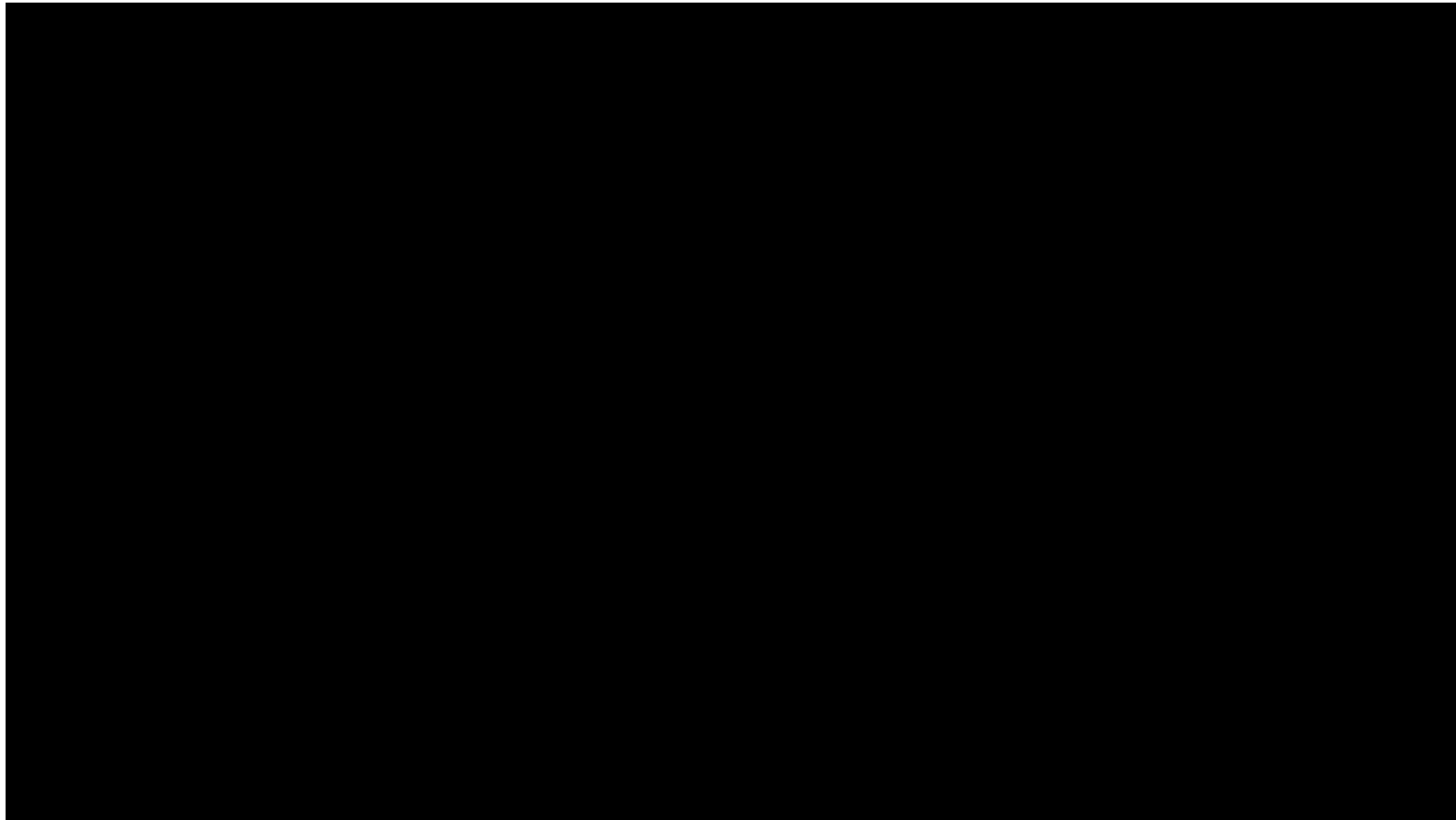


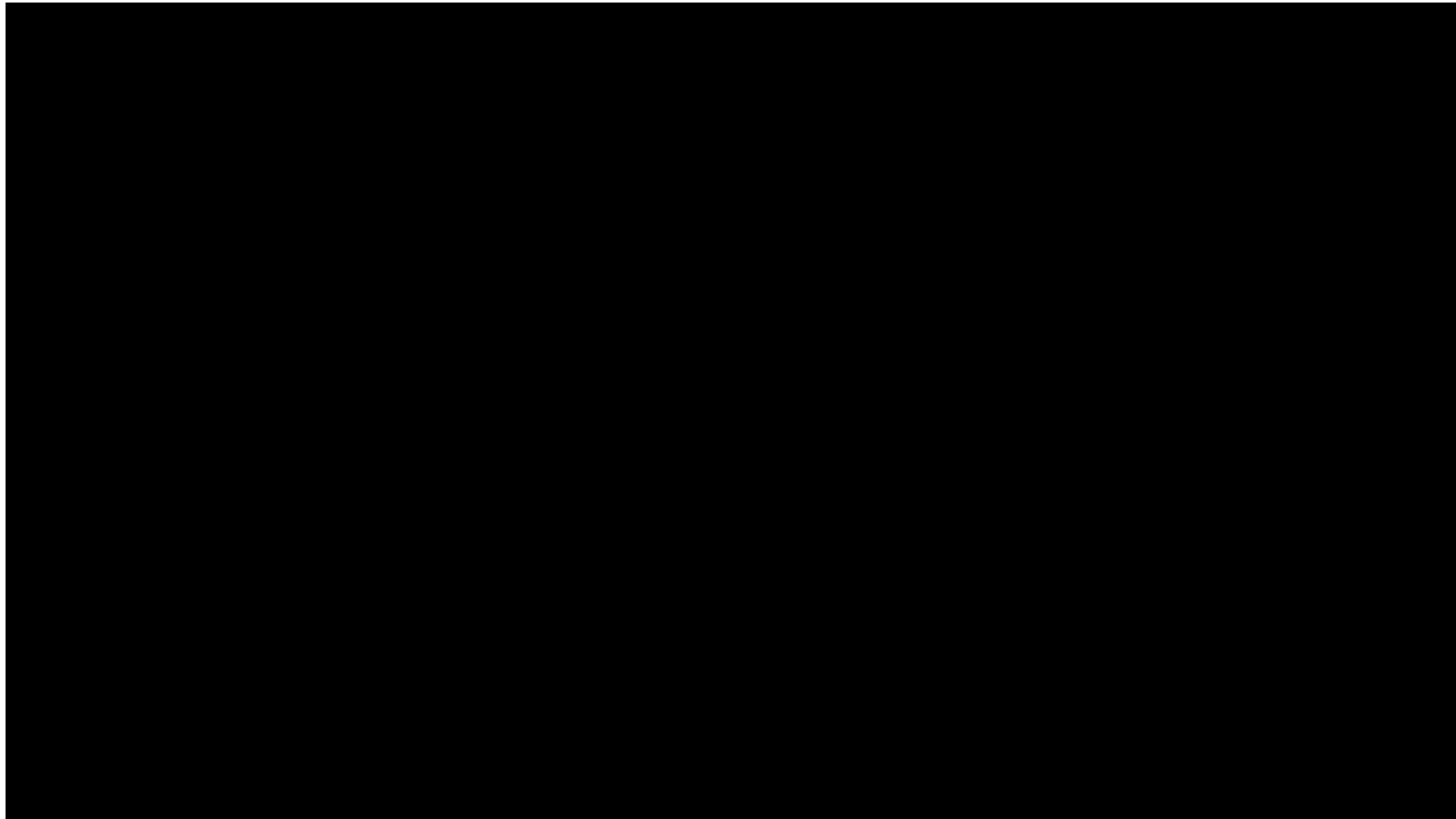
Horizontal circulation and Coriolis

EPS131, Introduction to Physical Oceanography and Climate
Dept of Earth and Planetary Sciences, Harvard University
Eli Tziperman



Horizontal circulation and Coriolis

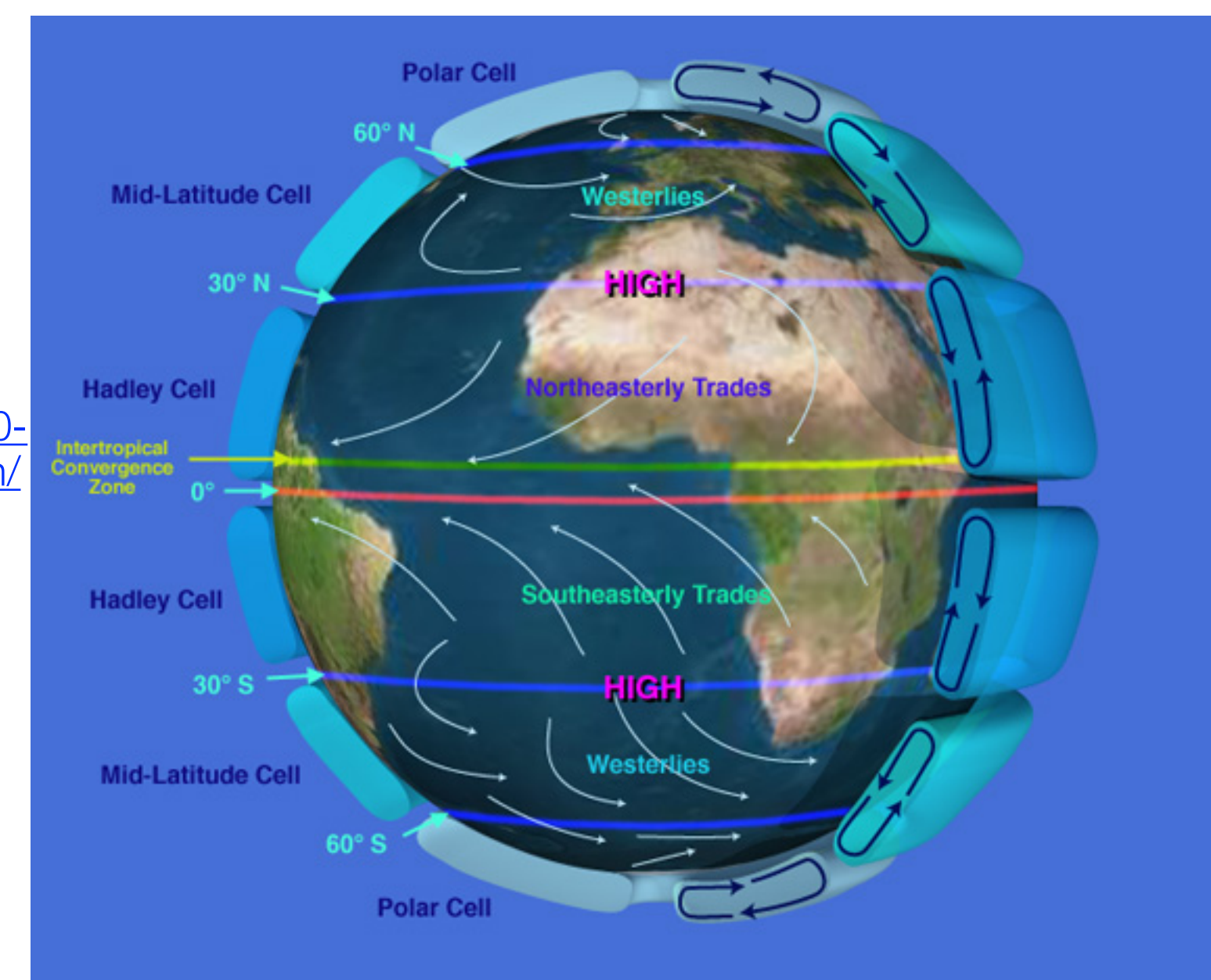
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1 Geostrophy - introduction (wind driving of ocean currents)

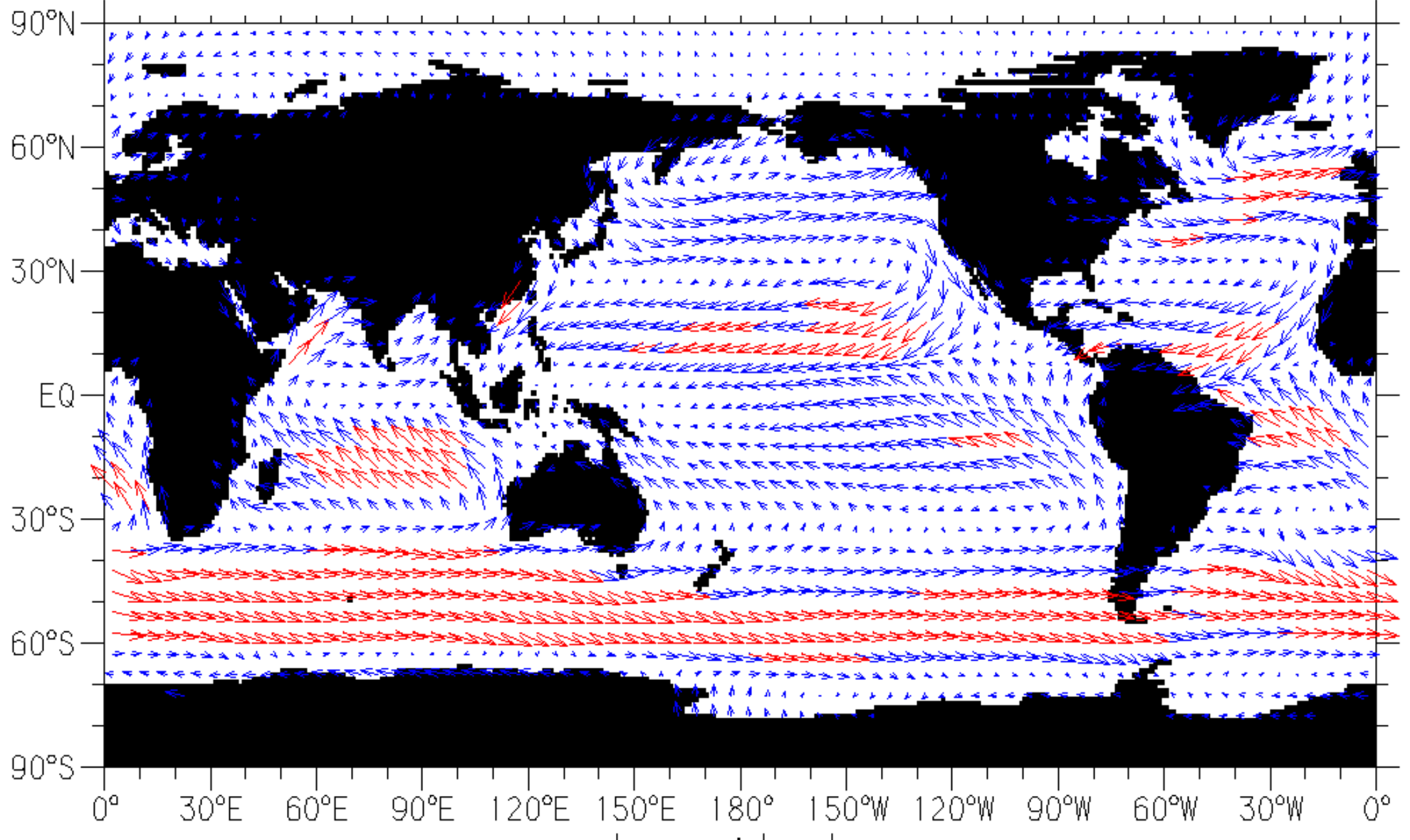
winds schematic

<https://slidetodoc.com/astr-2310-chapter-9-earth-and-moon-earth/>



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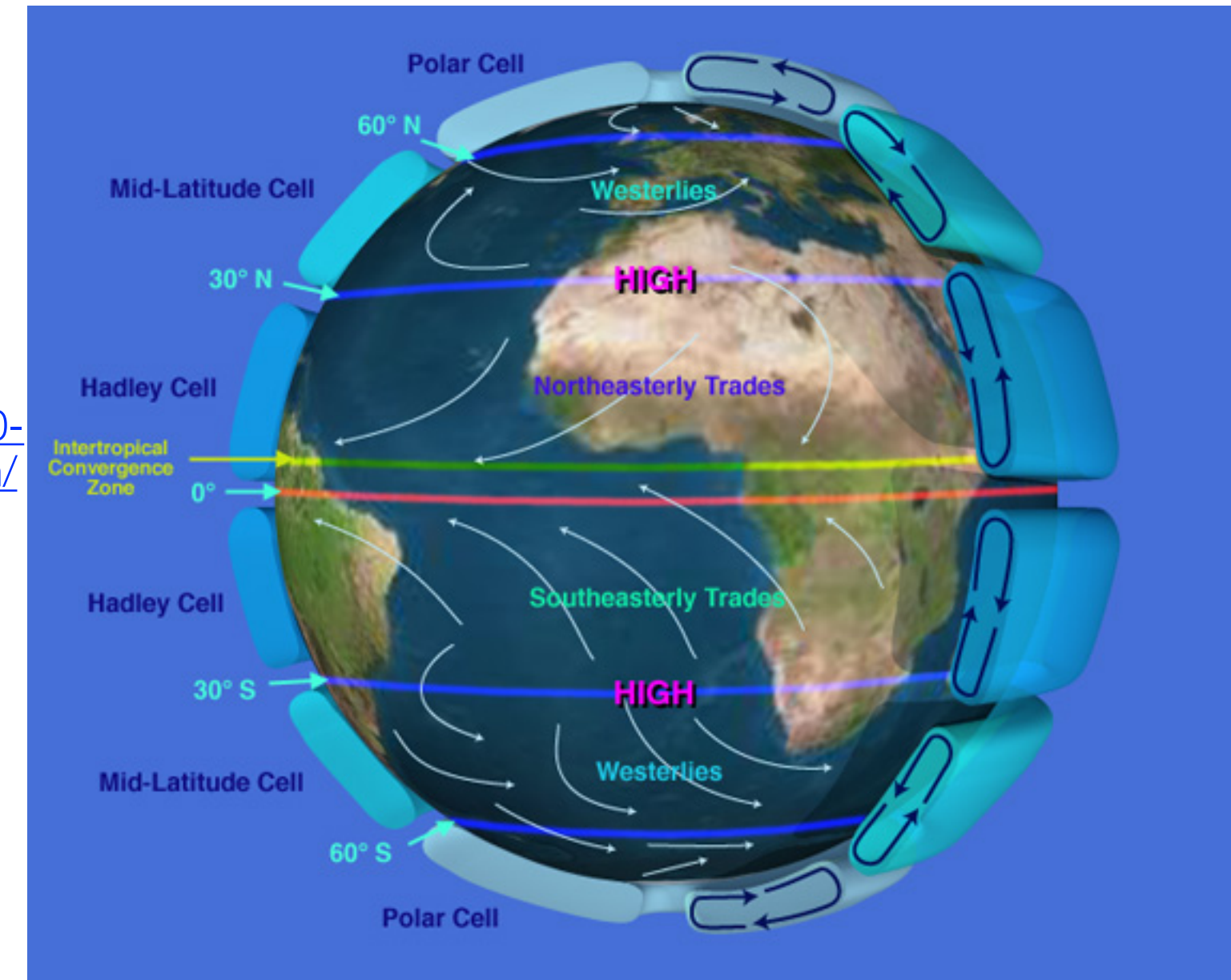
a annual mean surface winds stress



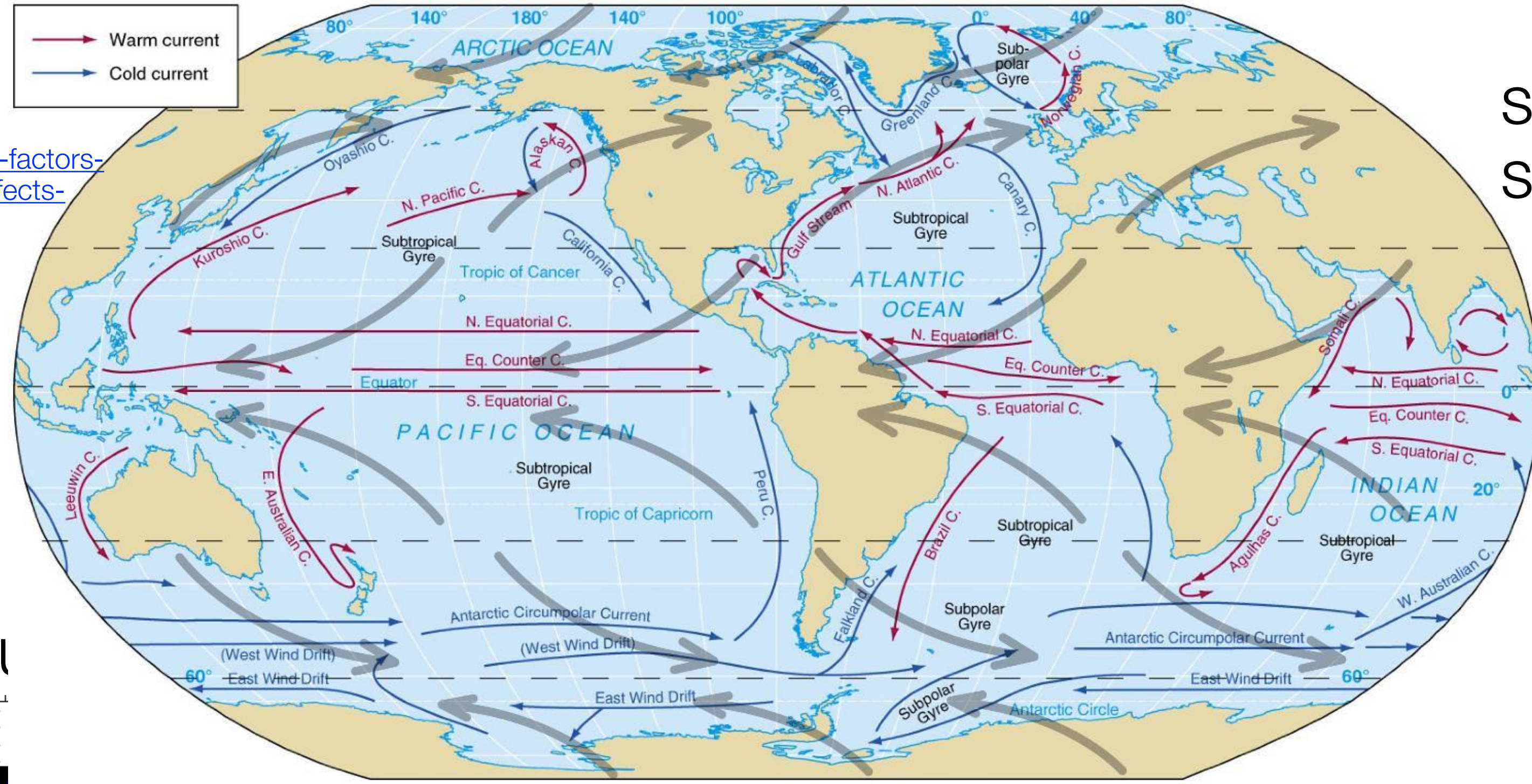
winds schematic

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<https://dandelionsandthings.blogspot.com/2018/09/33-label-global-winds-worksheet.html>



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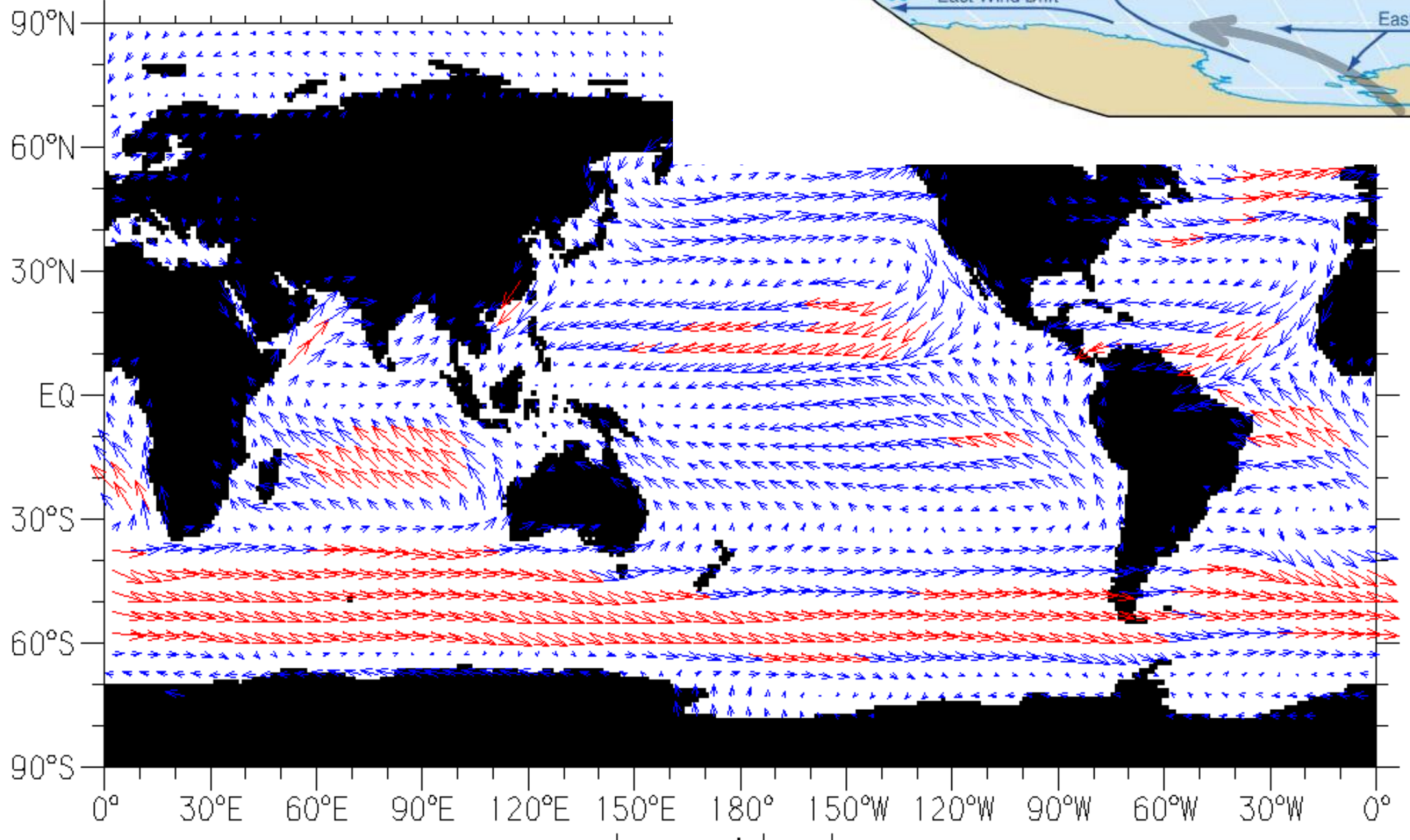


surface currents schematic

<https://www.pmfias.com/ocean-currents-factors-responsible-formation-ocean-currents-effects-ocean-currents/>

http://staff.orecity.k12.or.us/steve.tebor/atm%20currents/current/images/world_circulation.jpg

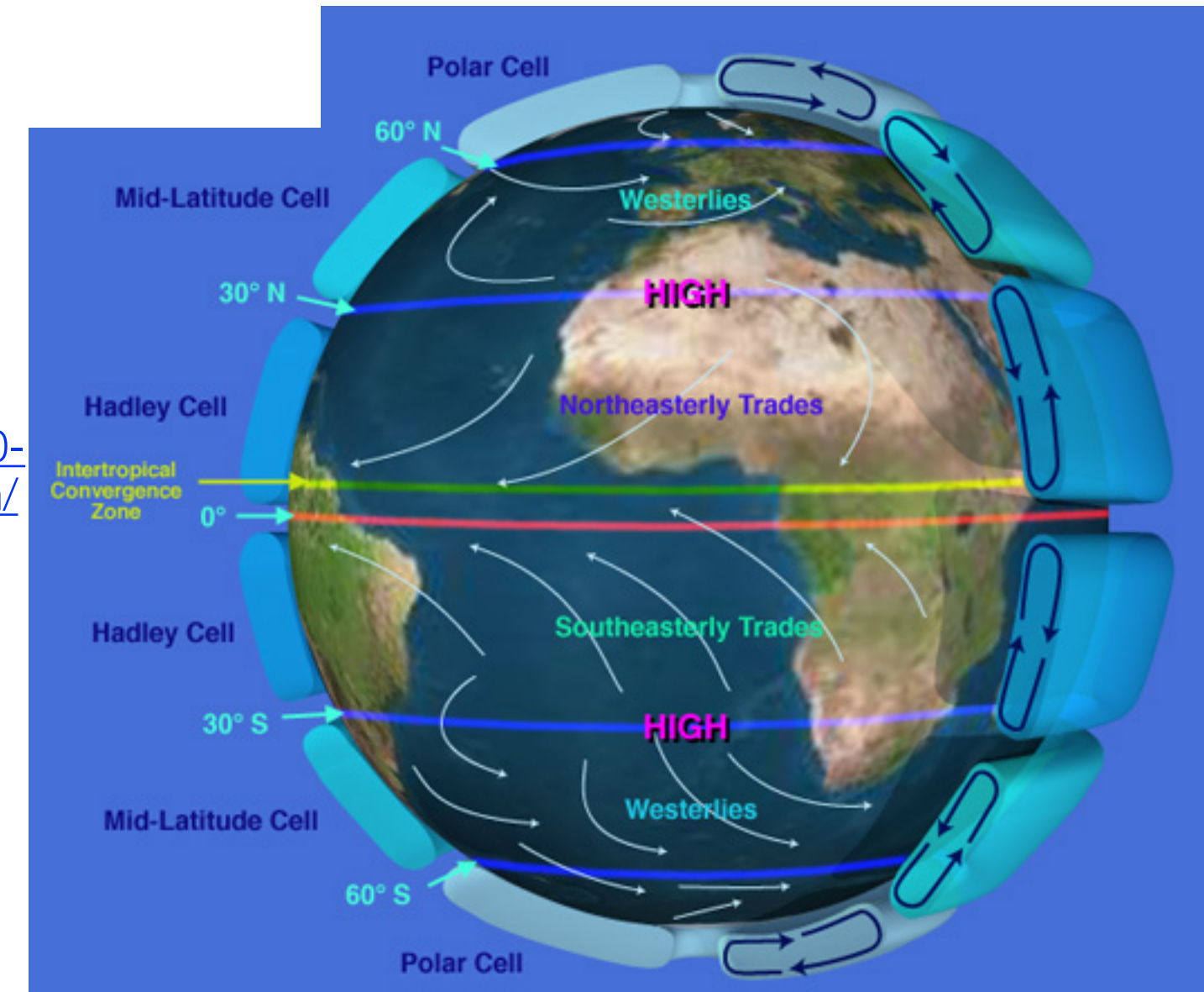
a annual mean st



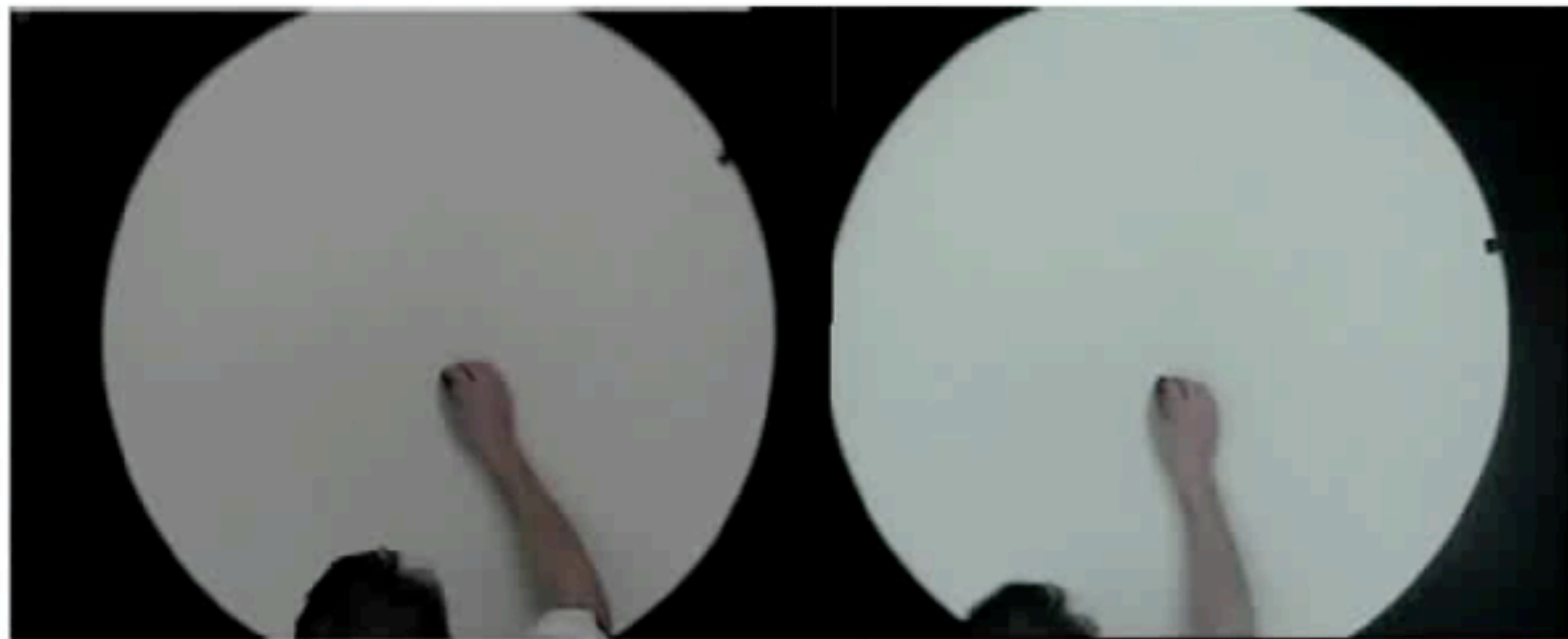
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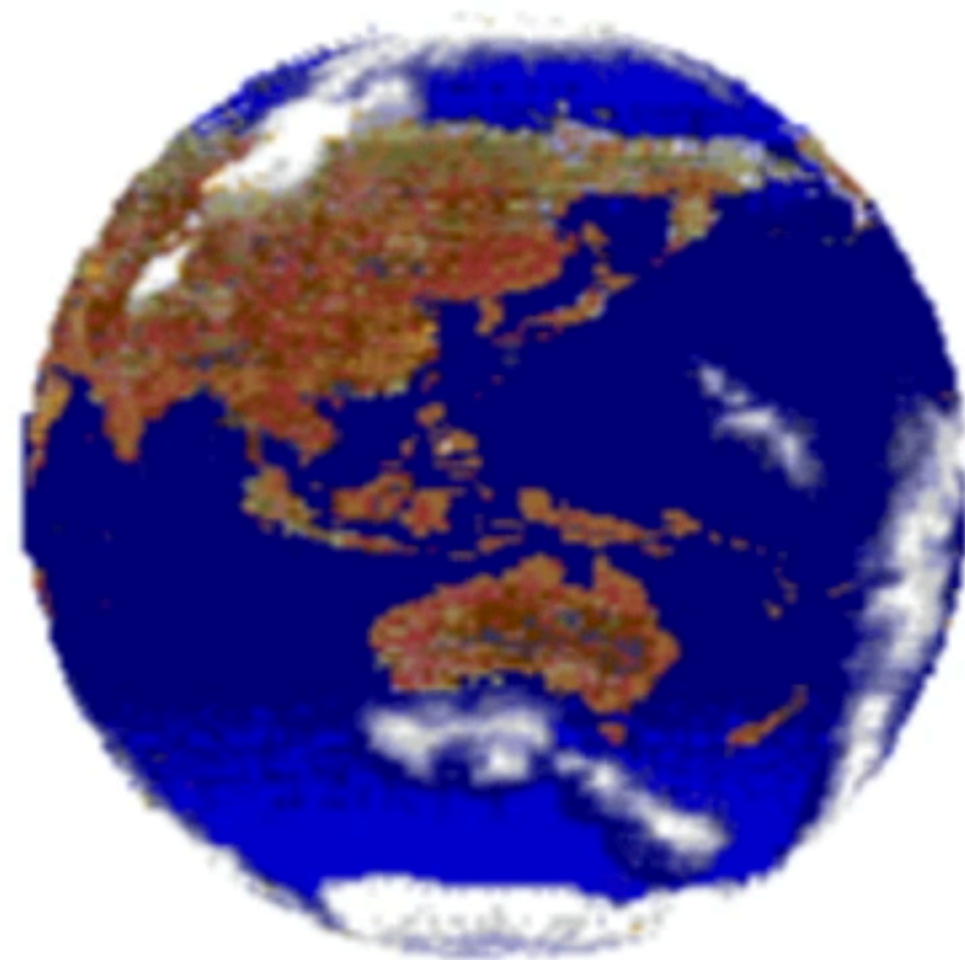
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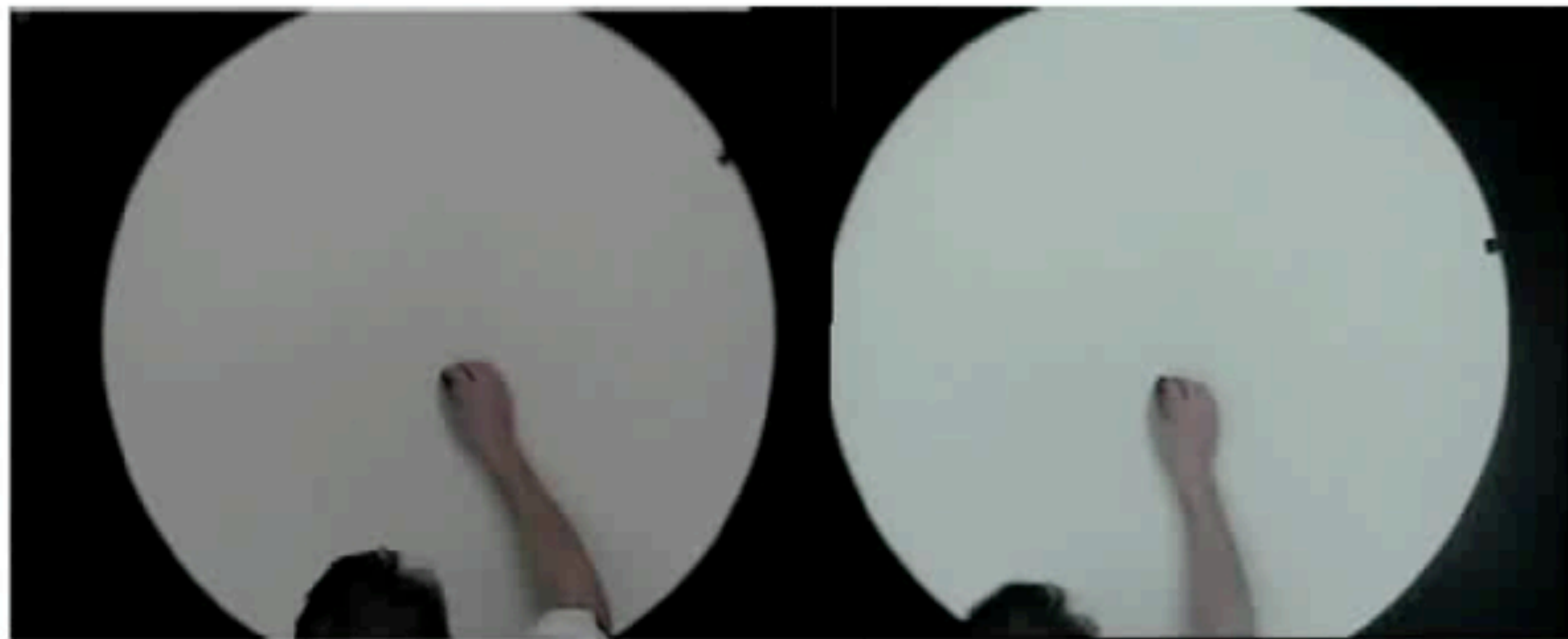
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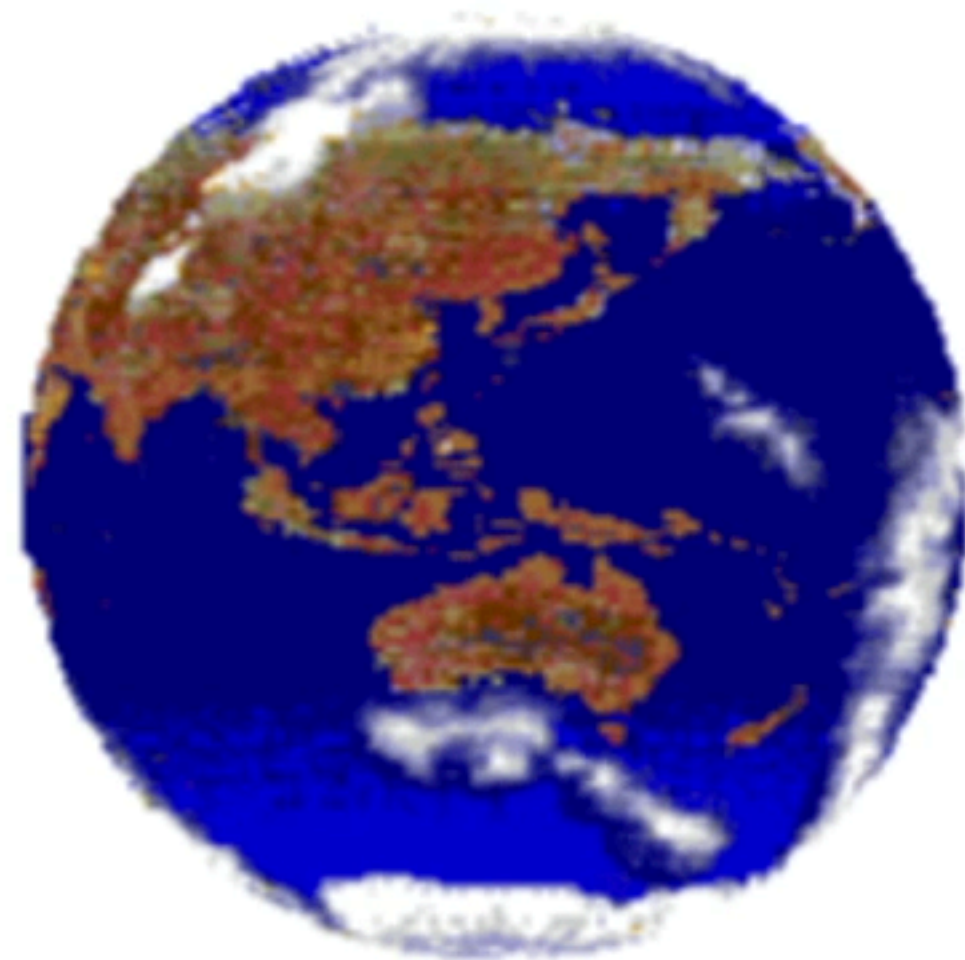
(<https://www.youtube.com/watch?v=RrWKS0vqV-0> J. Marshall, MIT)



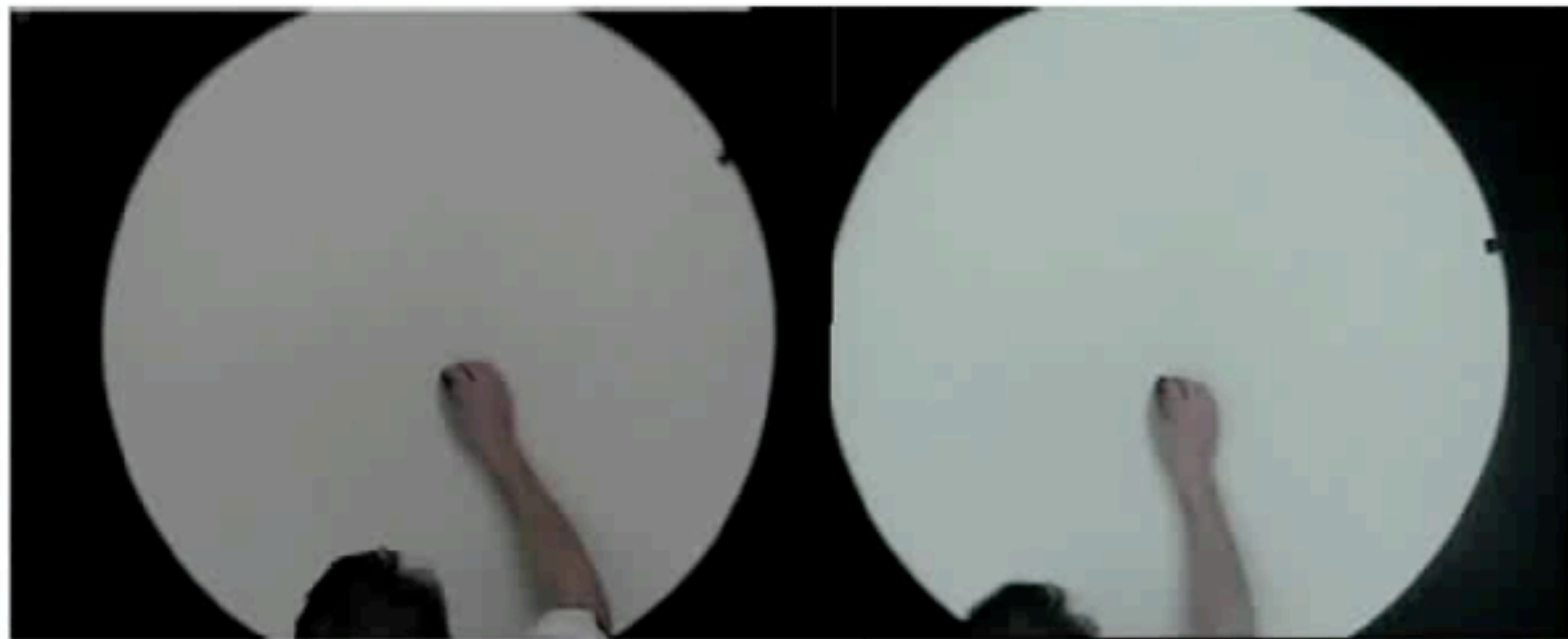
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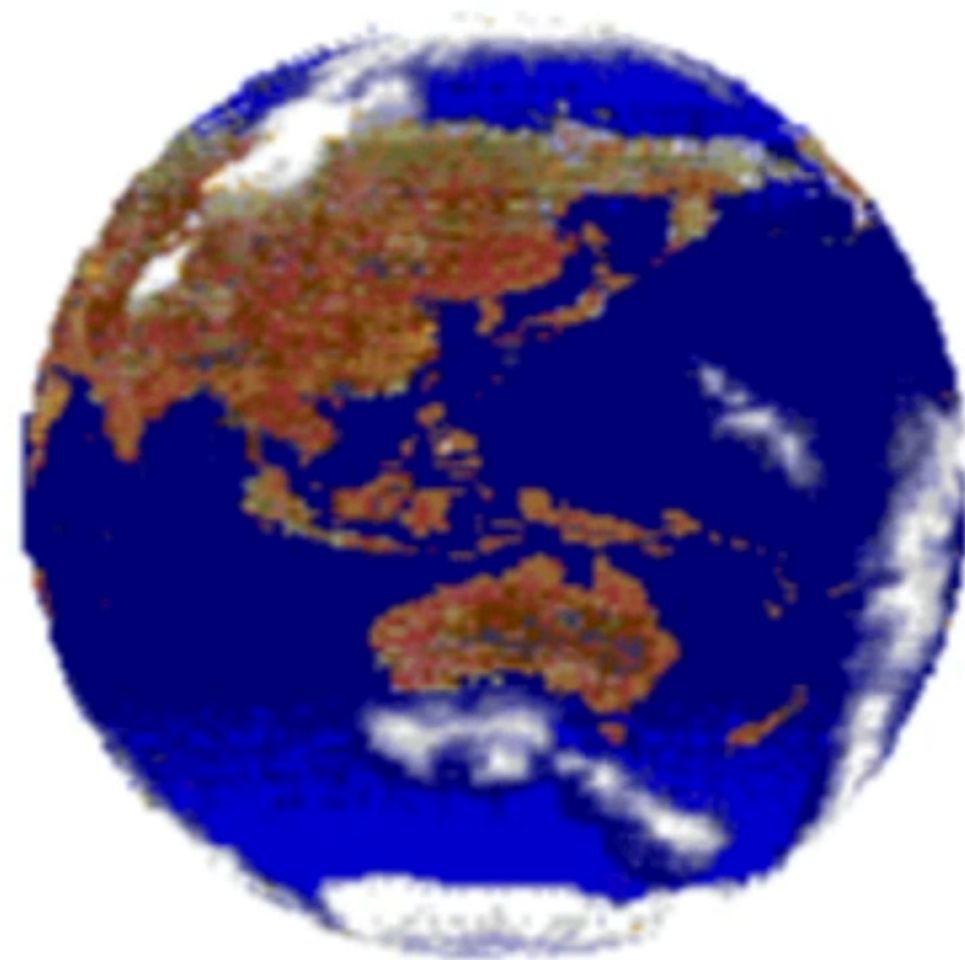
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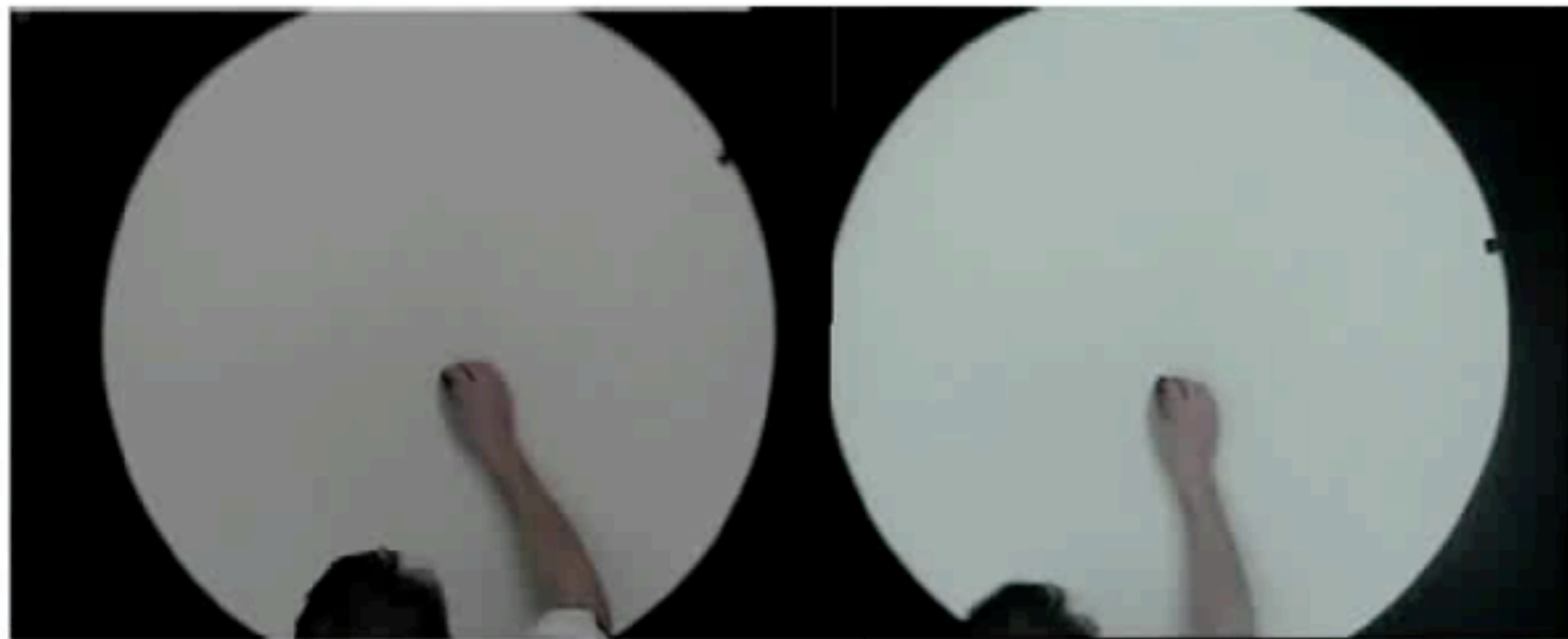
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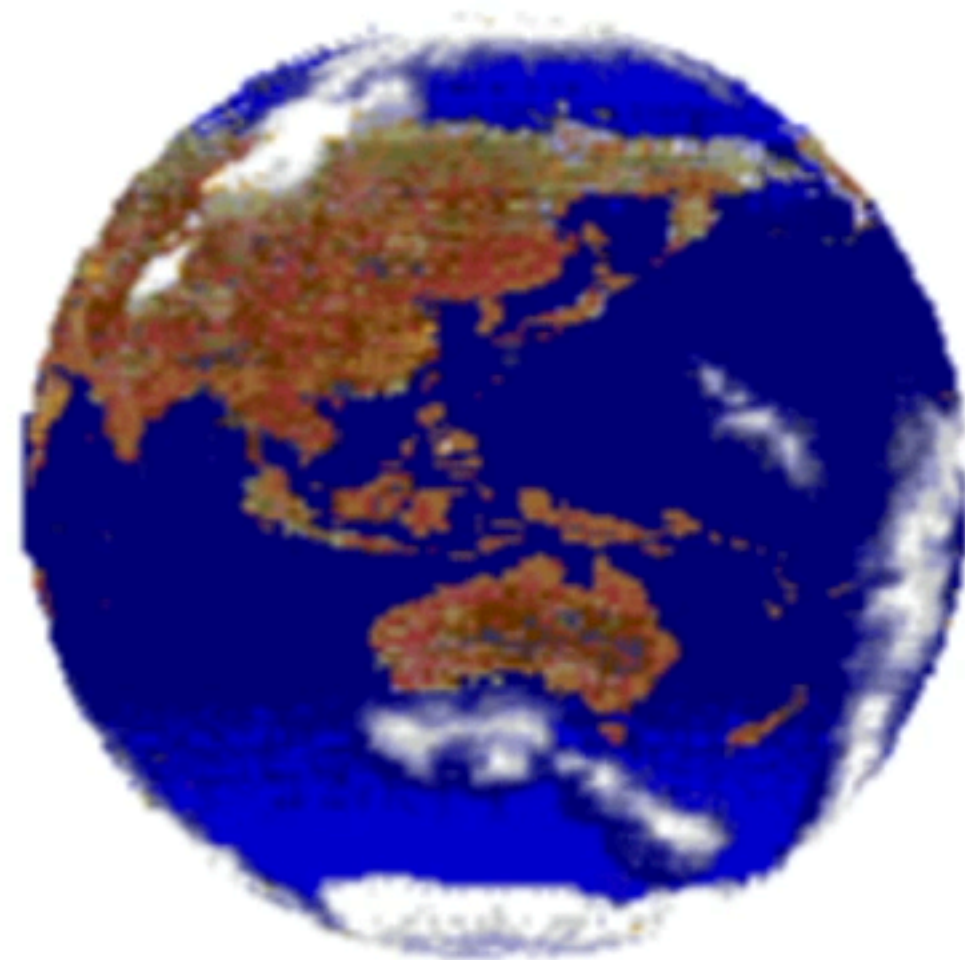
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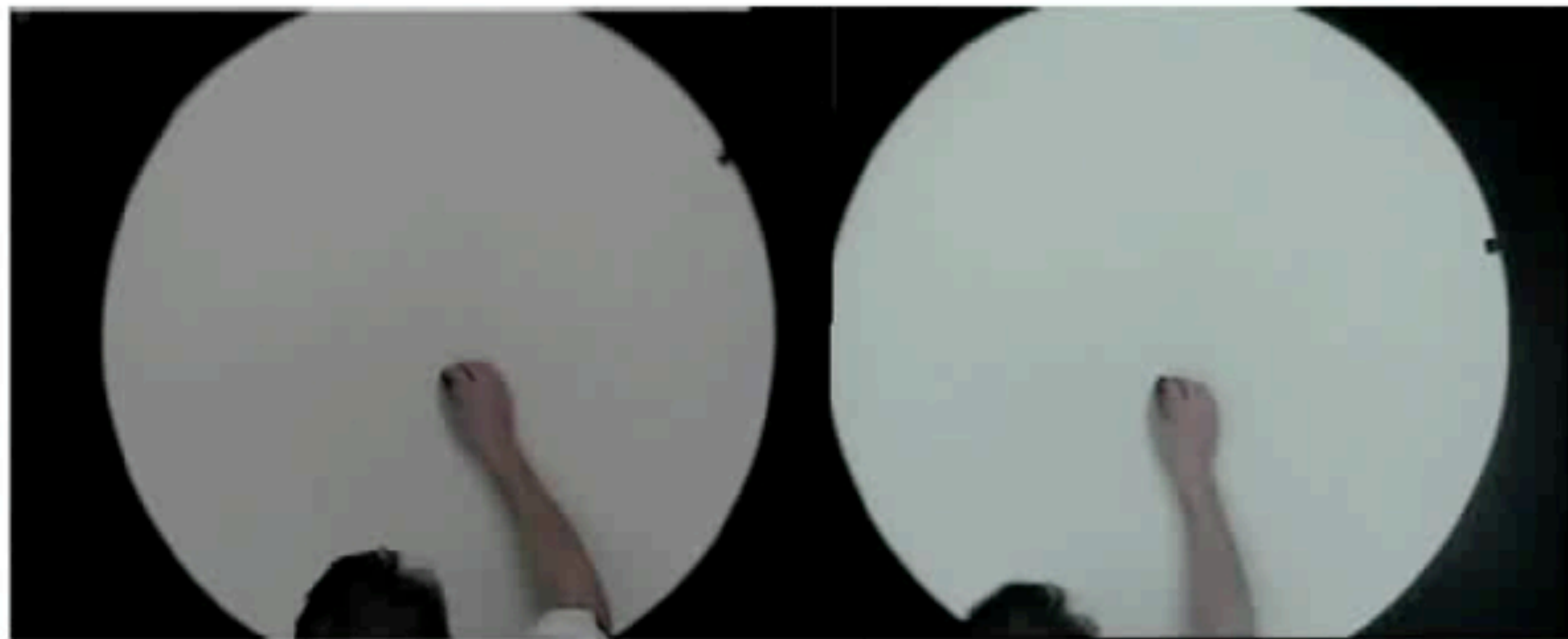
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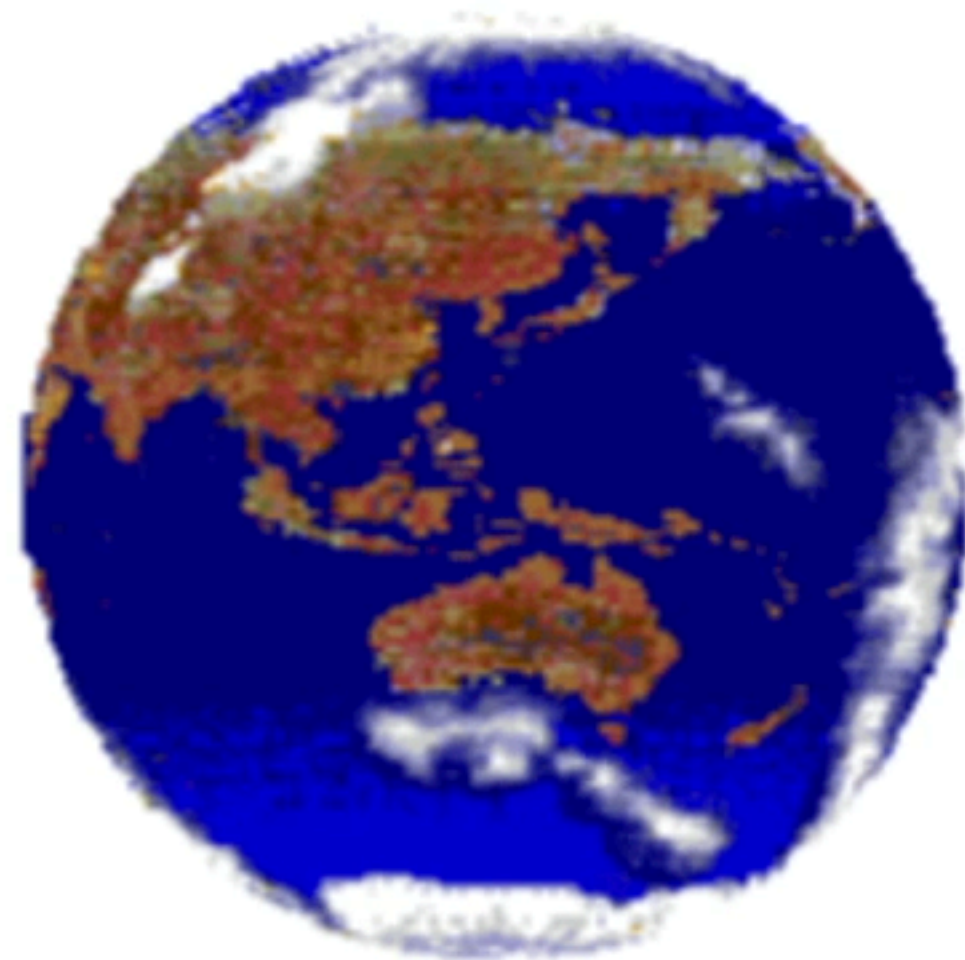
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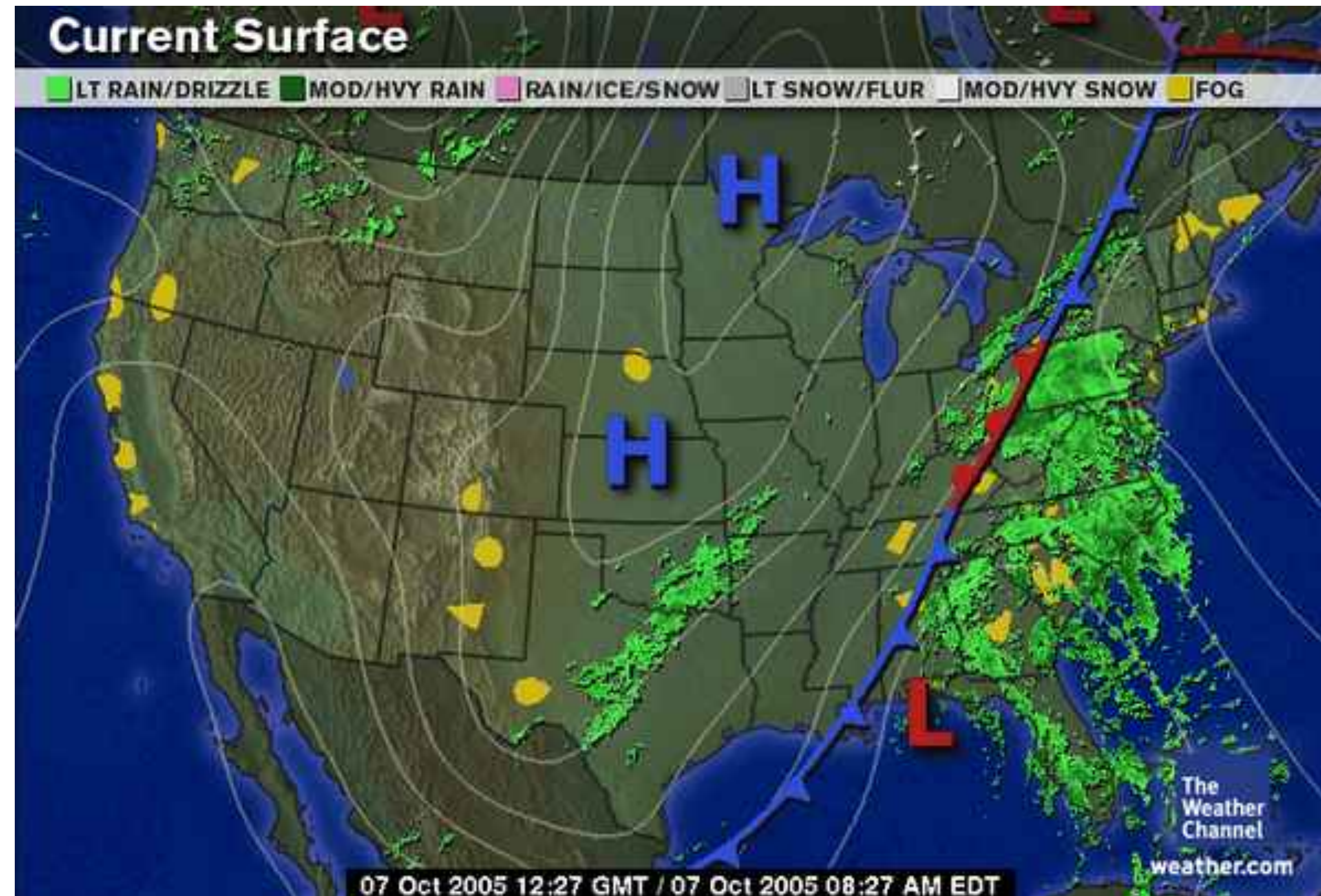


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geostrophy - motivation

Atmosphere: sea level pressure and wind direction



The weather channel

Notes

2 Geostrophy - derivation

(see two following slides with mini quizzes)

Miniquiz

Coriolis force form and sign in two horizontal $F=ma$

What is the Coriolis force (kg m s^{-2}) acting in the $(x, y) = (\text{east, north})$ directions on a fluid element moving at a speed (u, v) , whose volume is $\Delta x \Delta y \Delta z$, density is ρ , and where the Coriolis parameter (s^{-1}) is f .

Miniquiz:

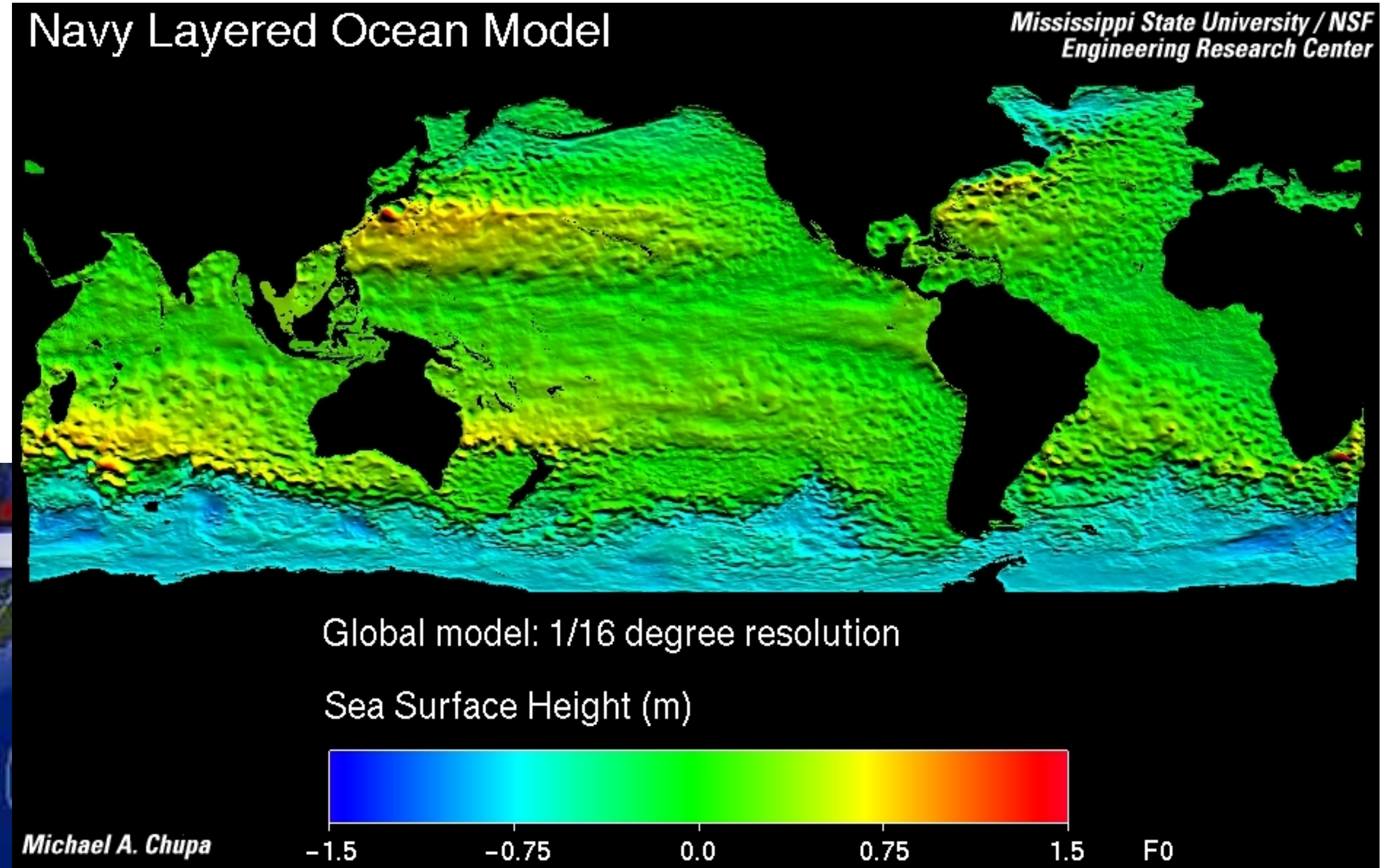
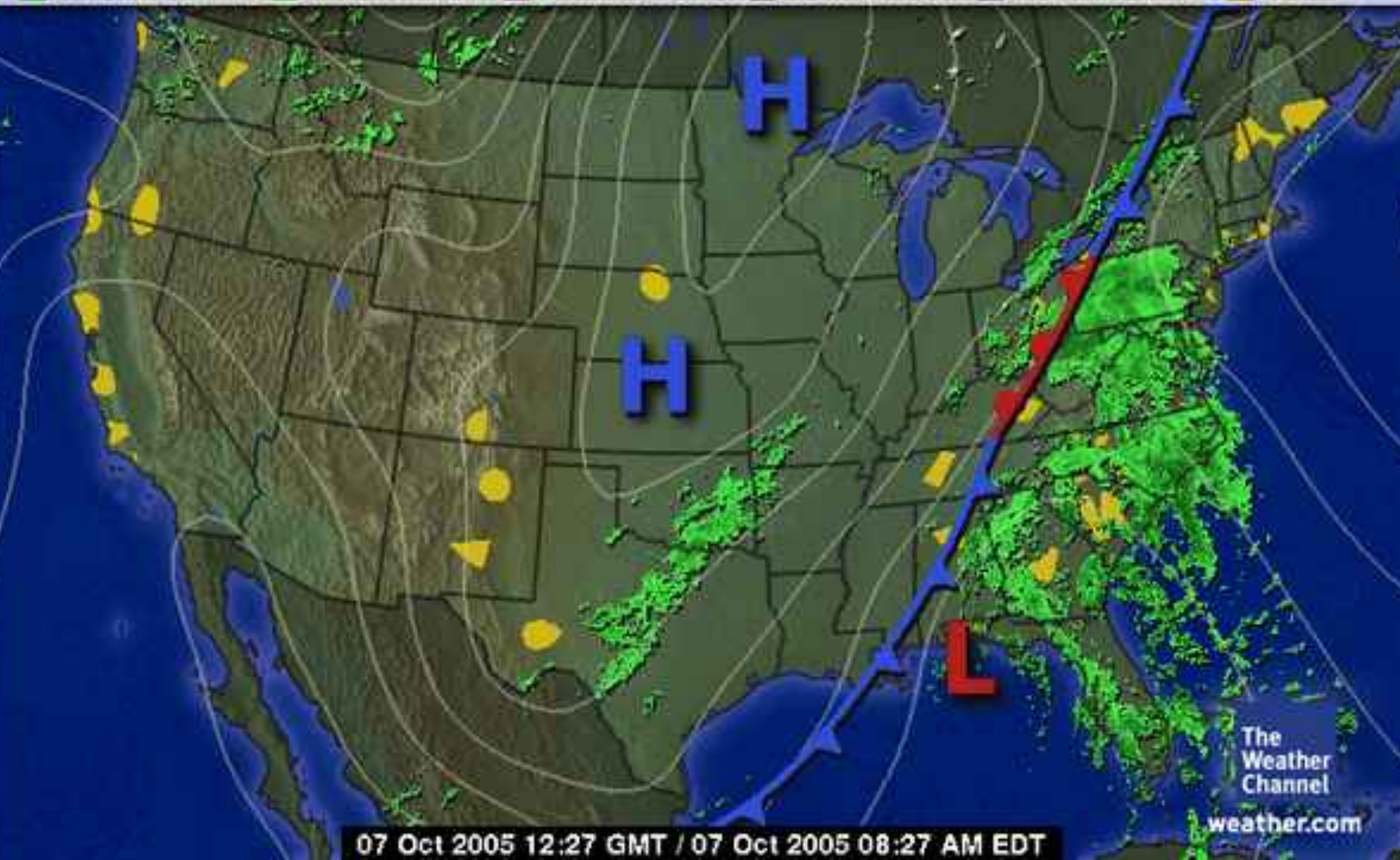
Geostrophy: write the form of the two horizontal momentum equations, that represent $F = ma$ including the Coriolis force and the pressure force, and where acceleration is zero (steady state).

3 Examples of geostrophic balance

Atmosphere: sea level pressure corresponding to winds

Current Surface

LT RAIN/DRIZZLE MOD/HVY RAIN RAIN/ICE/SNOW LT SNOW/FLUR MOD/HVY SNOW FOG



Ocean: sea surface height variations involved with major currents: western boundary currents and the Antarctic circumpolar current.

The weather channel

Miniquiz

wind velocity from sea level pressure (SLP) on a weather
map

steps:

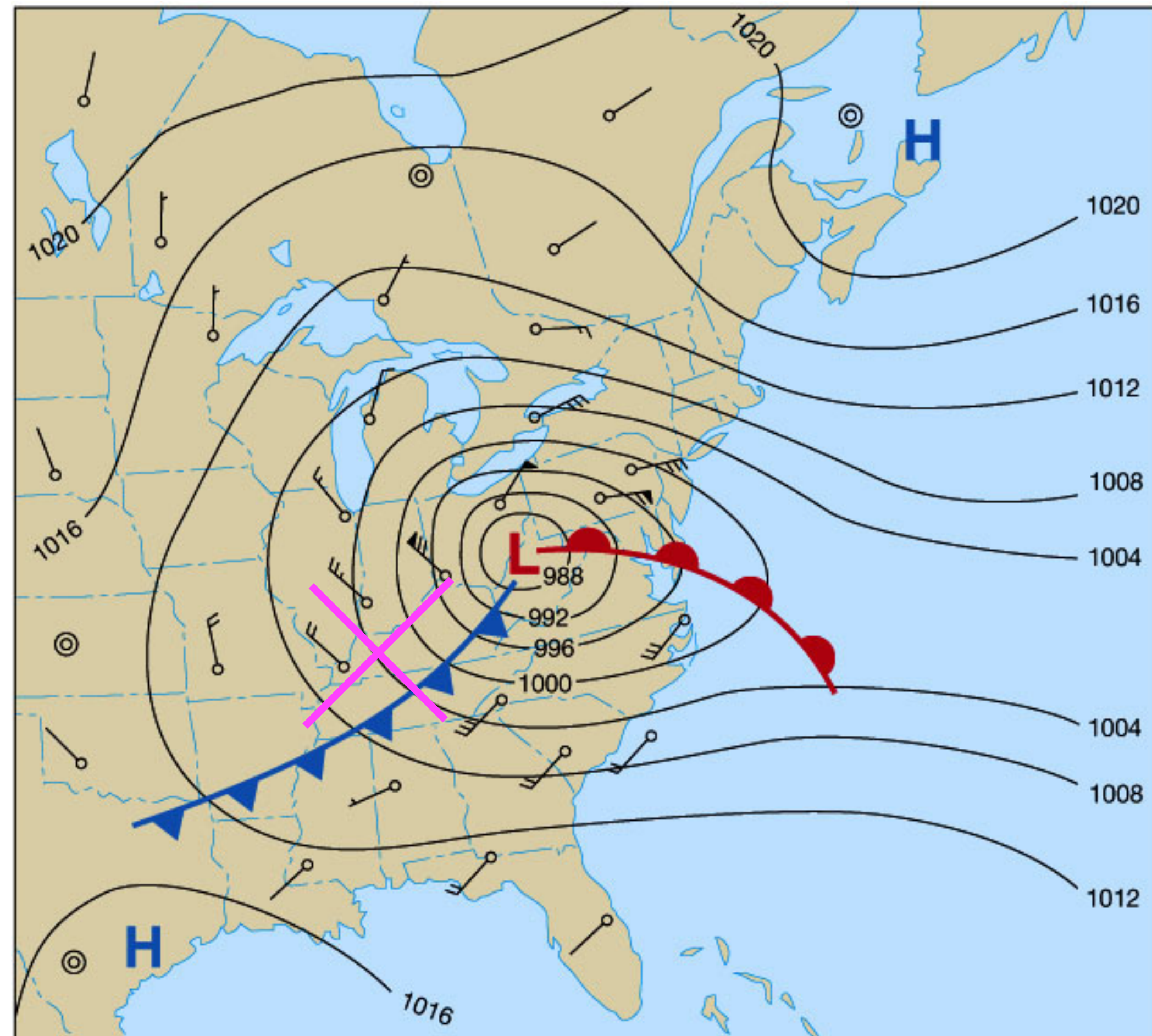
$$f = 2\Omega \sin \theta =$$

$$\Delta p =$$

$$\Delta x =$$

$$\rho_{air} =$$

$$(u, v) =$$



Miniquiz

wind velocity from sea level pressure (SLP) on a weather map

steps:

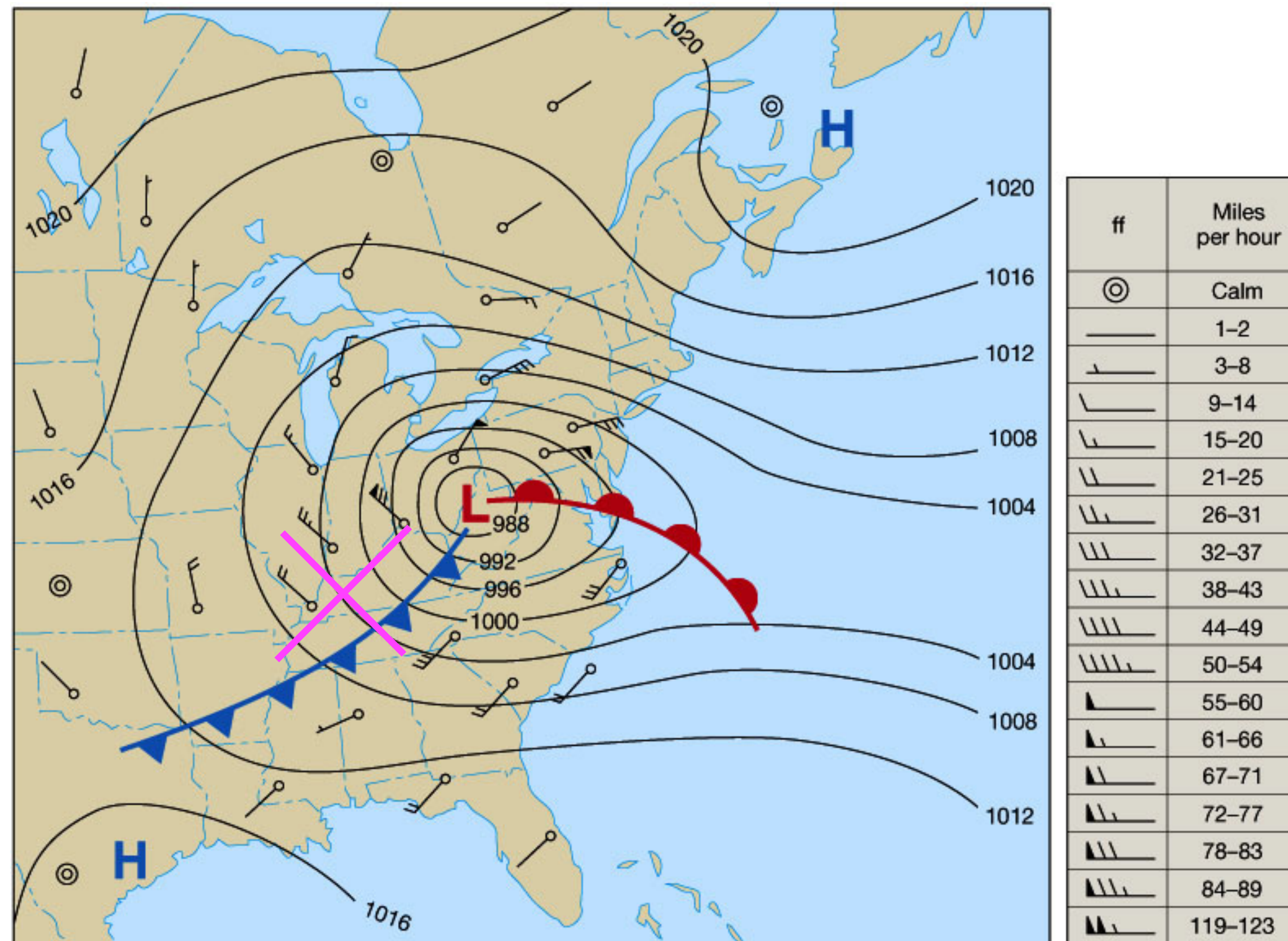
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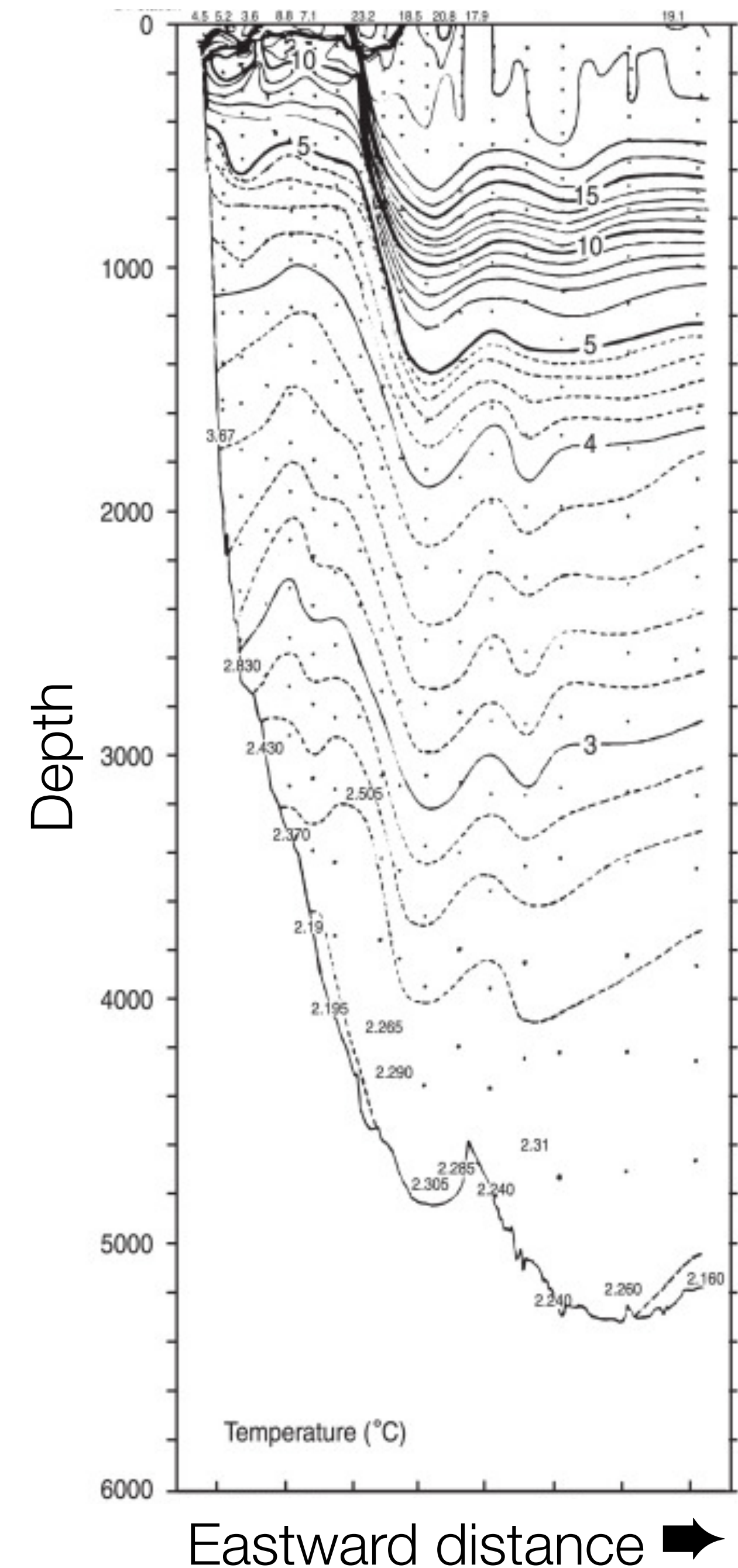


miniquiz:

Derive the vertical momentum budget equation, balancing pressure force with gravity force: consider a fluid parcel of volume $\Delta x \Delta y \Delta z$ and density ρ .

miniquiz:

Find the direction of the long-shore velocity from a temperature section in the Northern Hemisphere



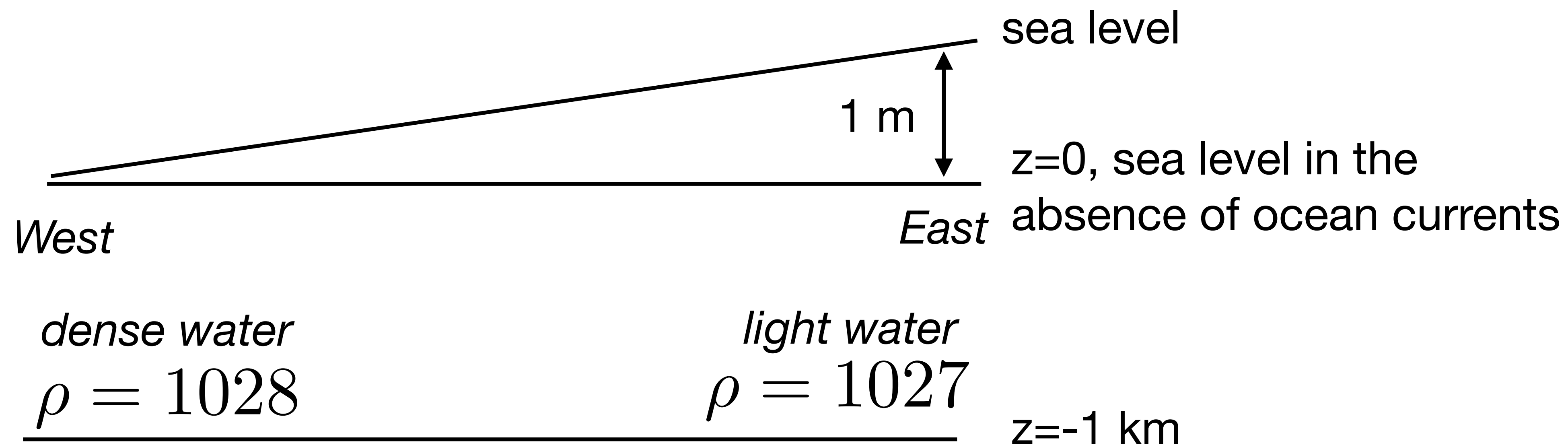
Notes

4 The hydrostatic balance

5 Boussinesq approximation

Notes

6 sea level vs stratification in a stratified geostrophic flow such as the Gulf Stream

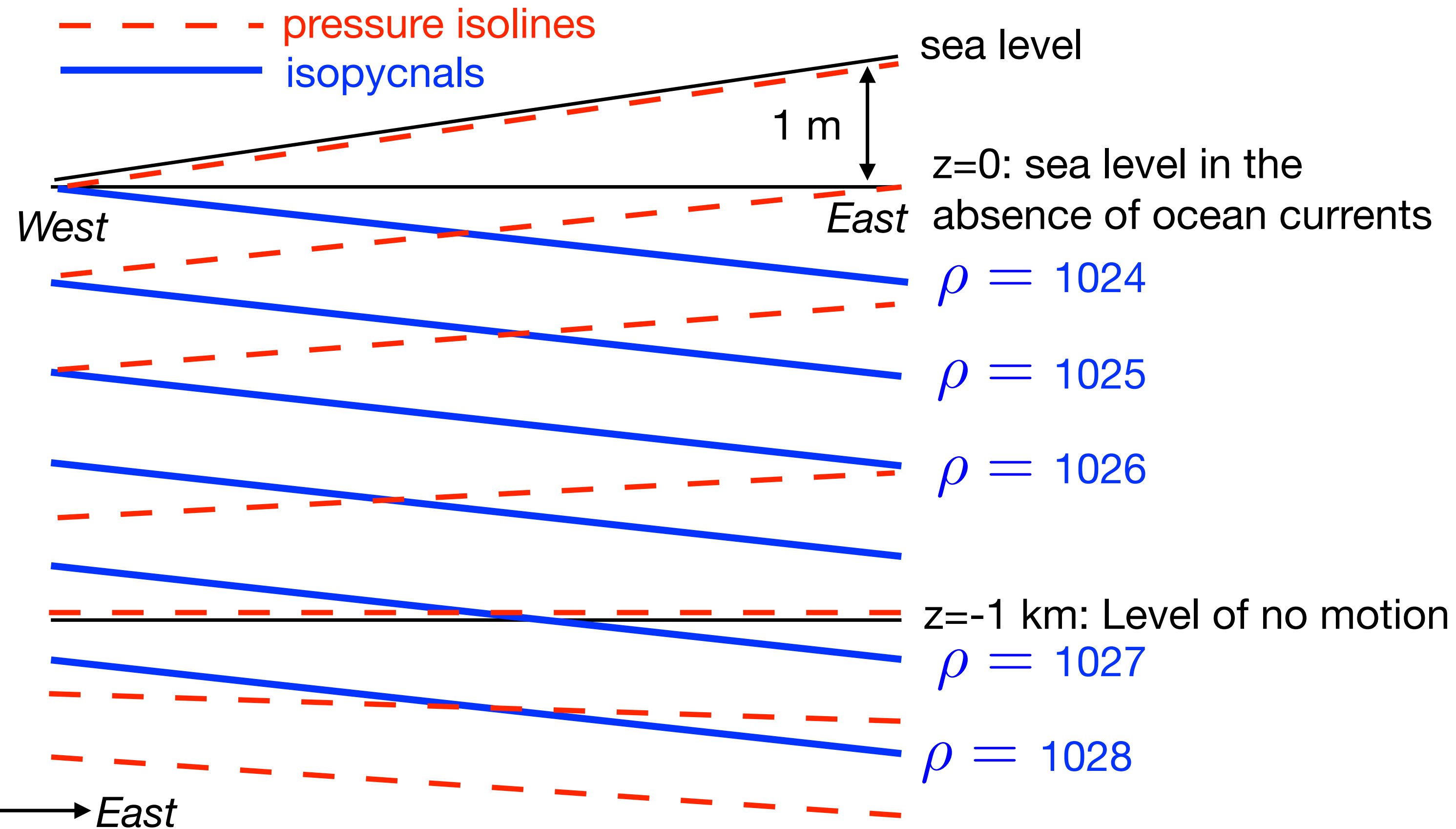


Notes

6 sea level vs stratification in a stratified geostrophic flow such as the Gulf Stream

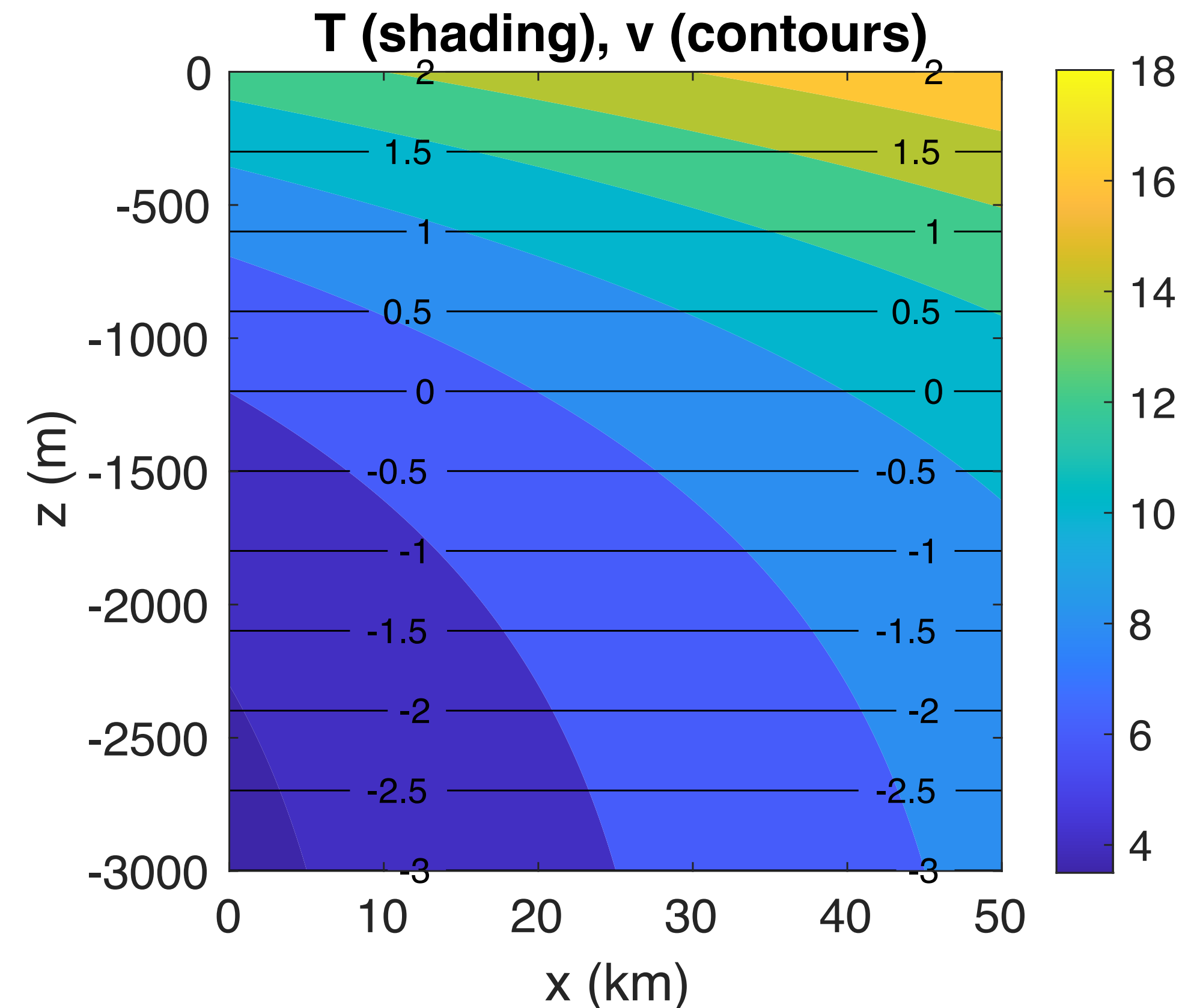
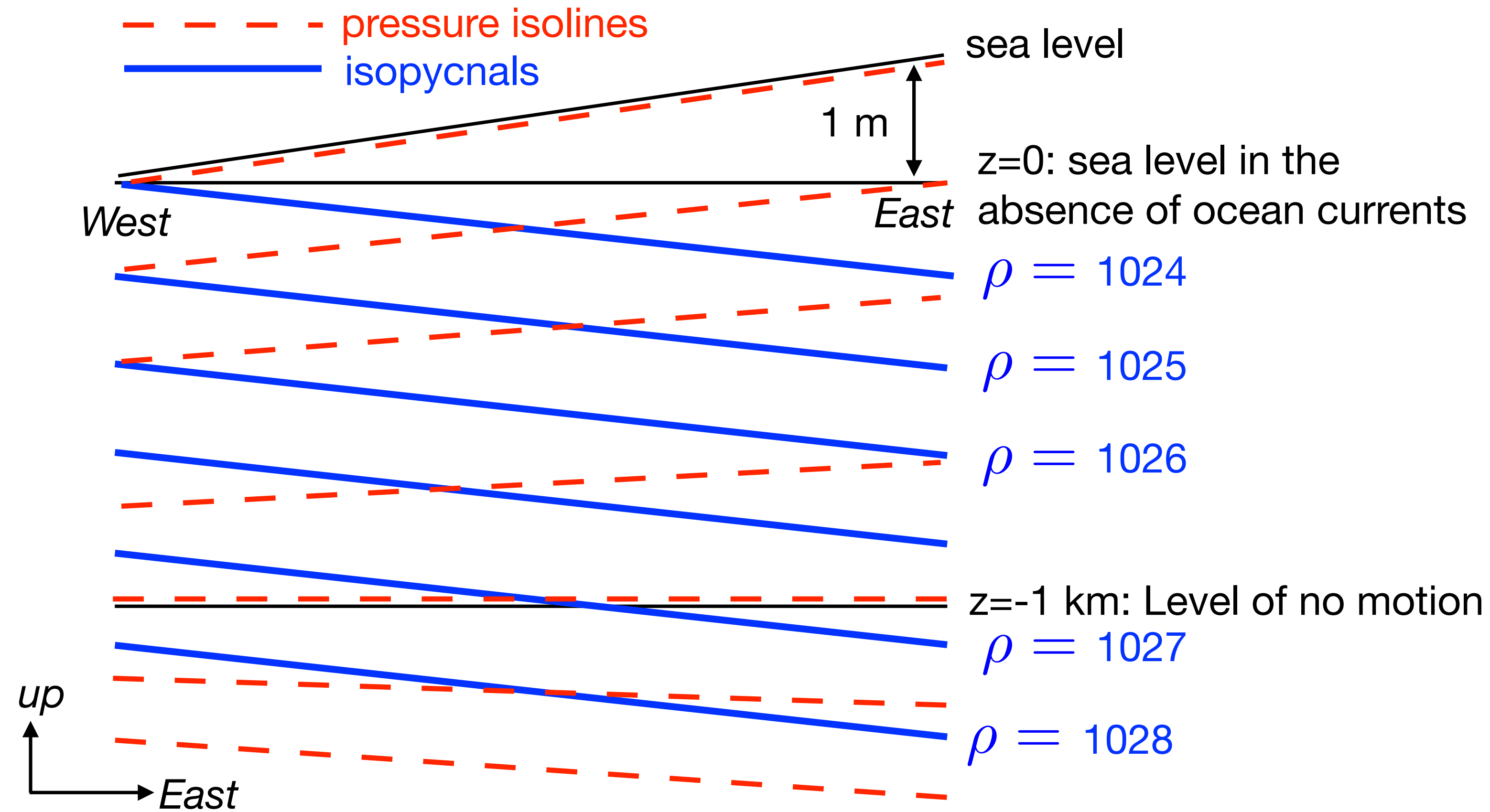
Notes

6 sea level vs stratification in a stratified geostrophic flow such as the Gulf Stream



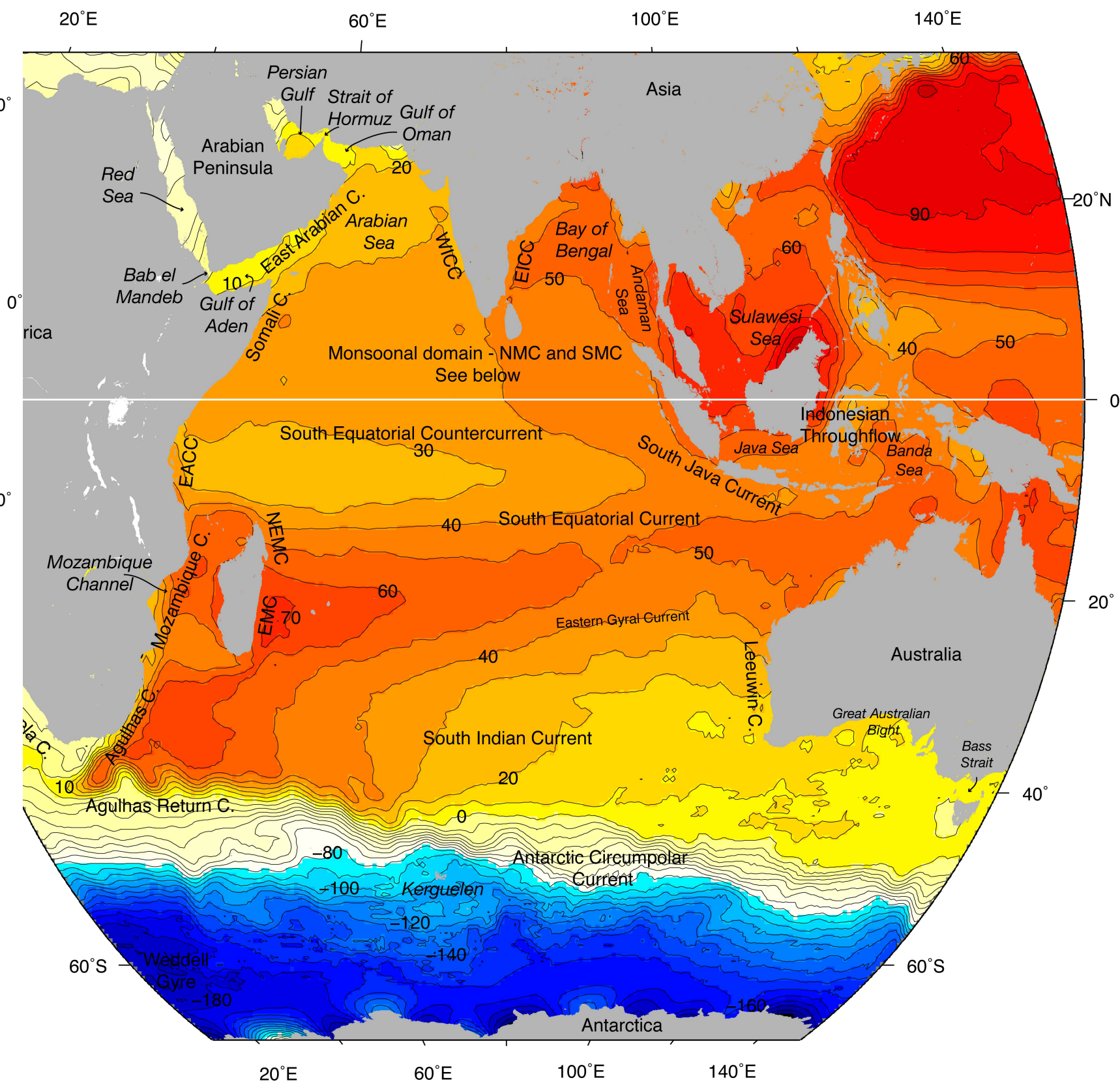
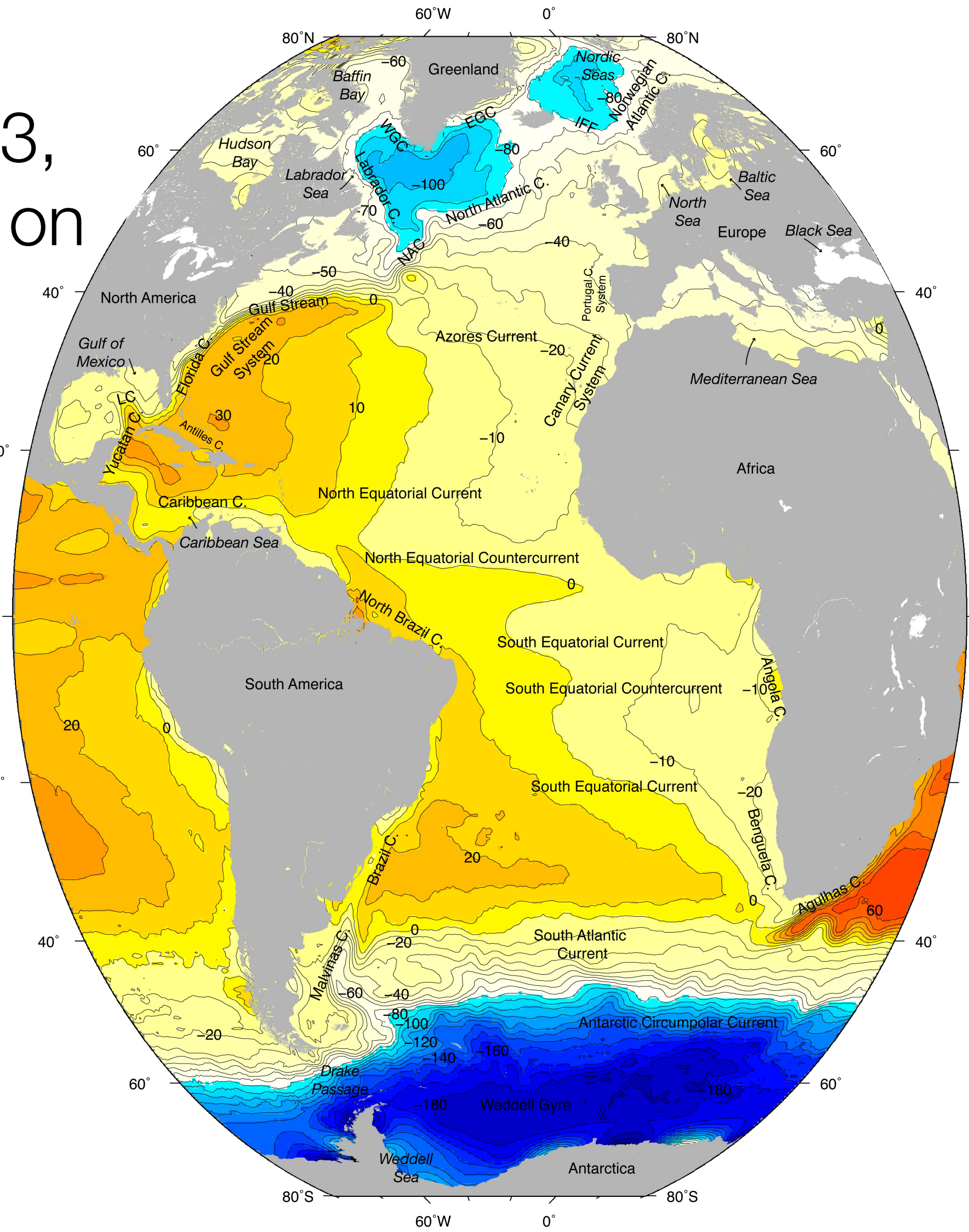
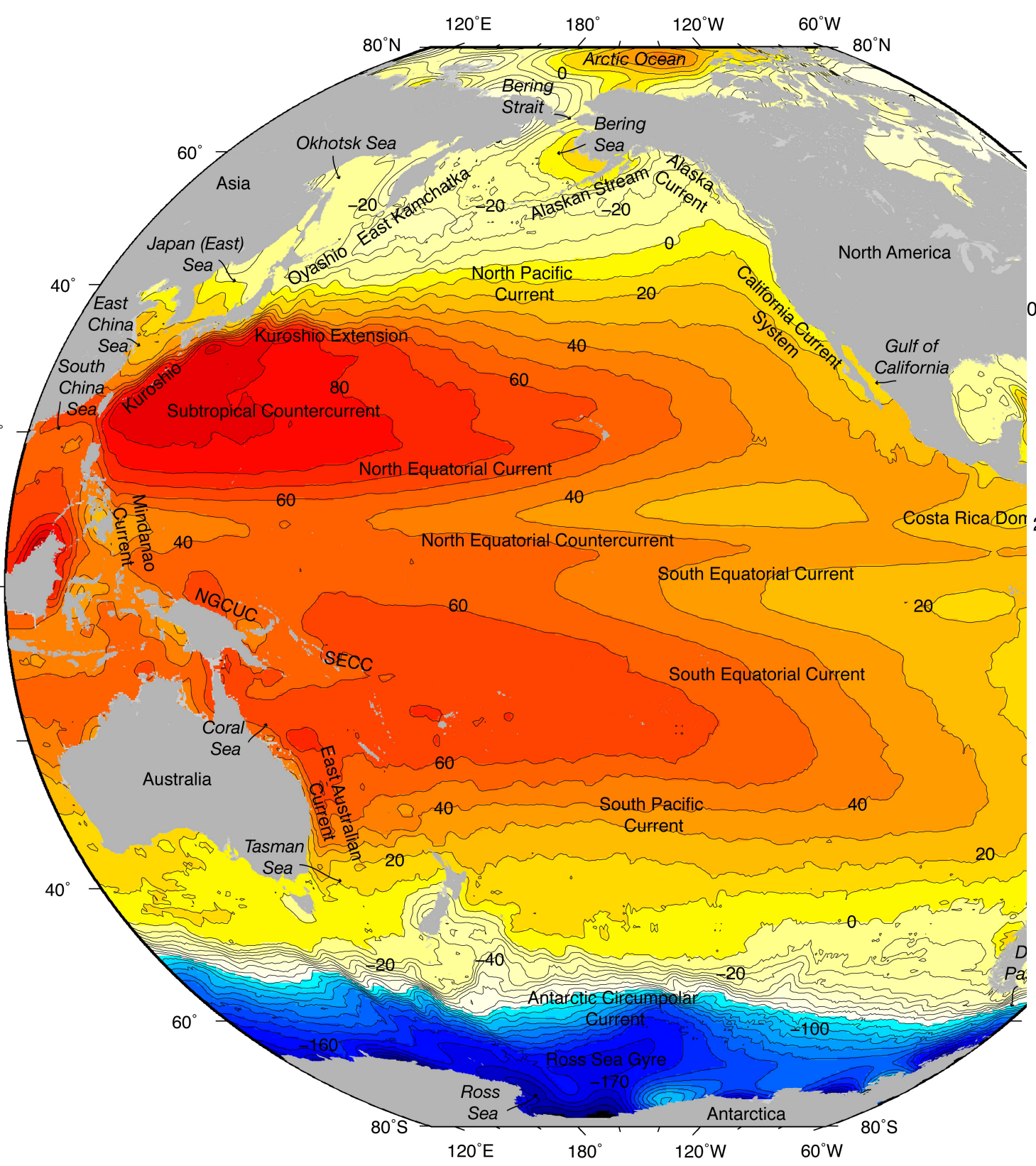
Notes

6 sea level vs stratification in a stratified geostrophic flow such as the Gulf Stream



7 Calculating currents from temperature & sea level

“Sea surface height (Using Niiler et al., 2003, surface heights based on drifters)”(*)



(*)From [http://talleylab.ucsd.edu/ltalley/sio210/dynamics rotation/lecture dynamics geostrophy.pdf](http://talleylab.ucsd.edu/ltalley/sio210/dynamics%20rotation/lecture%20dynamics%20geostrophy.pdf)

RAPID: monitoring the Atlantic Meridional Overturning Circulation at 26.5°N (motivation for calculating currents from T,S and sea surface height)

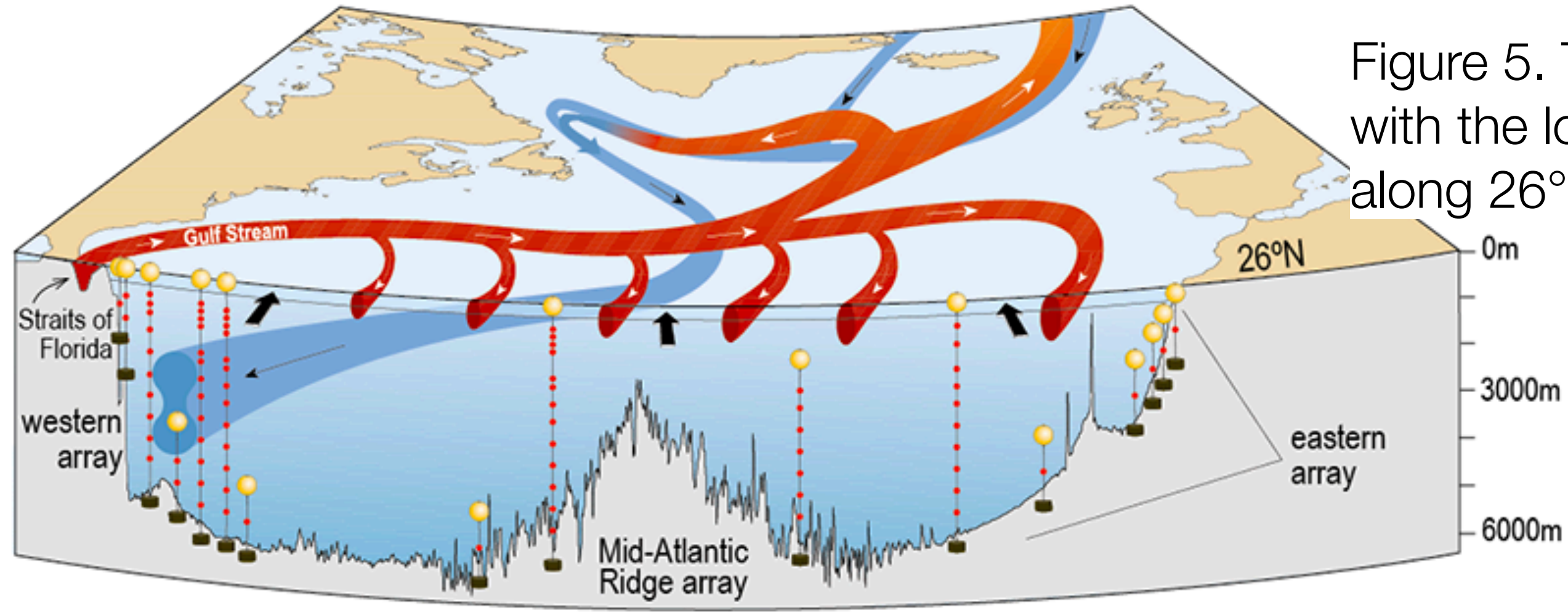


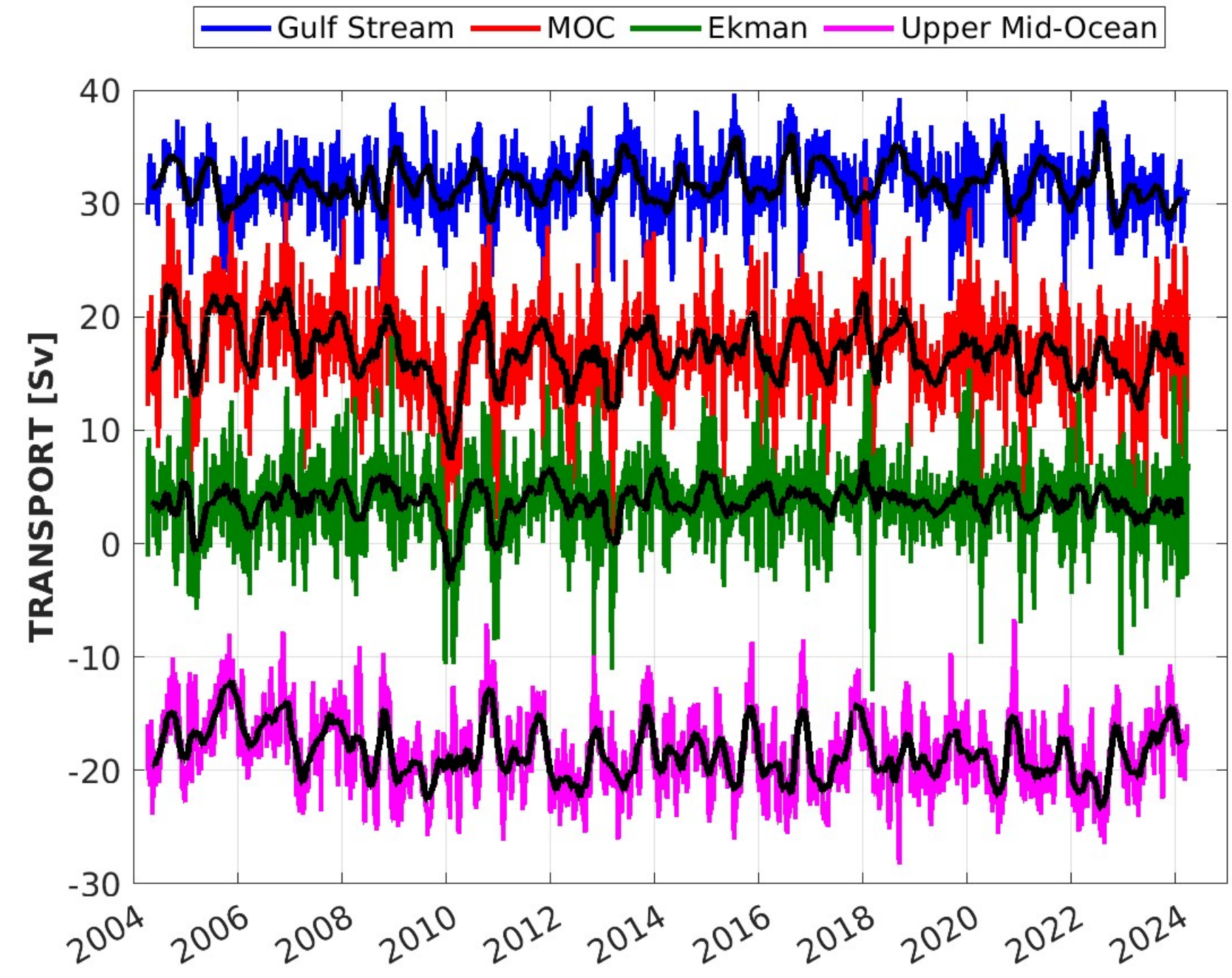
Figure 5. The North Atlantic overturning circulation with the location of the RAPID array moorings along 26°N. Modified from Church, 2007.

<https://www.rapid.ac.uk/background.php>

A view of the back deck of the RRS James Cook during the RAPID cruise in April 2014.



RAPID results for AMOC:



<https://www.rapid.ac.uk/data.php>

Notes

8 Thermal wind equations and level of no motion

Miniquiz

Derive thermal wind equations

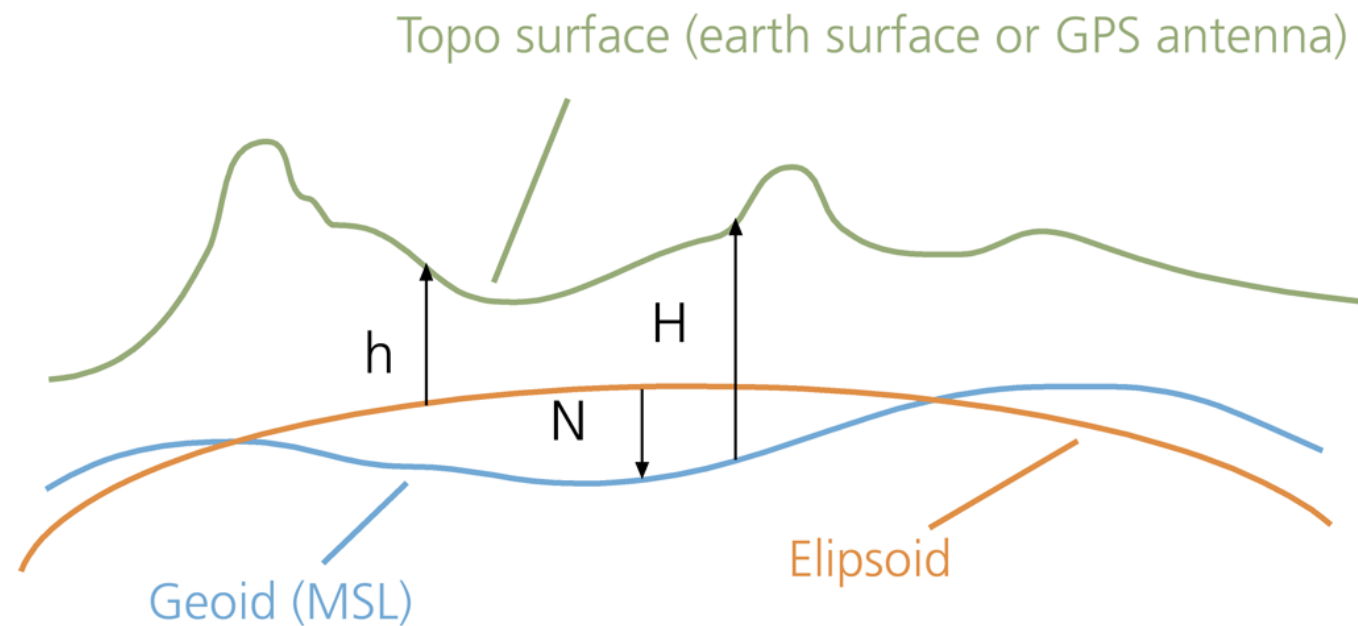
Miniquiz - calculate the depth of the level of no motion

optional, time permitting:

9 Dynamic height derived from geostrophy

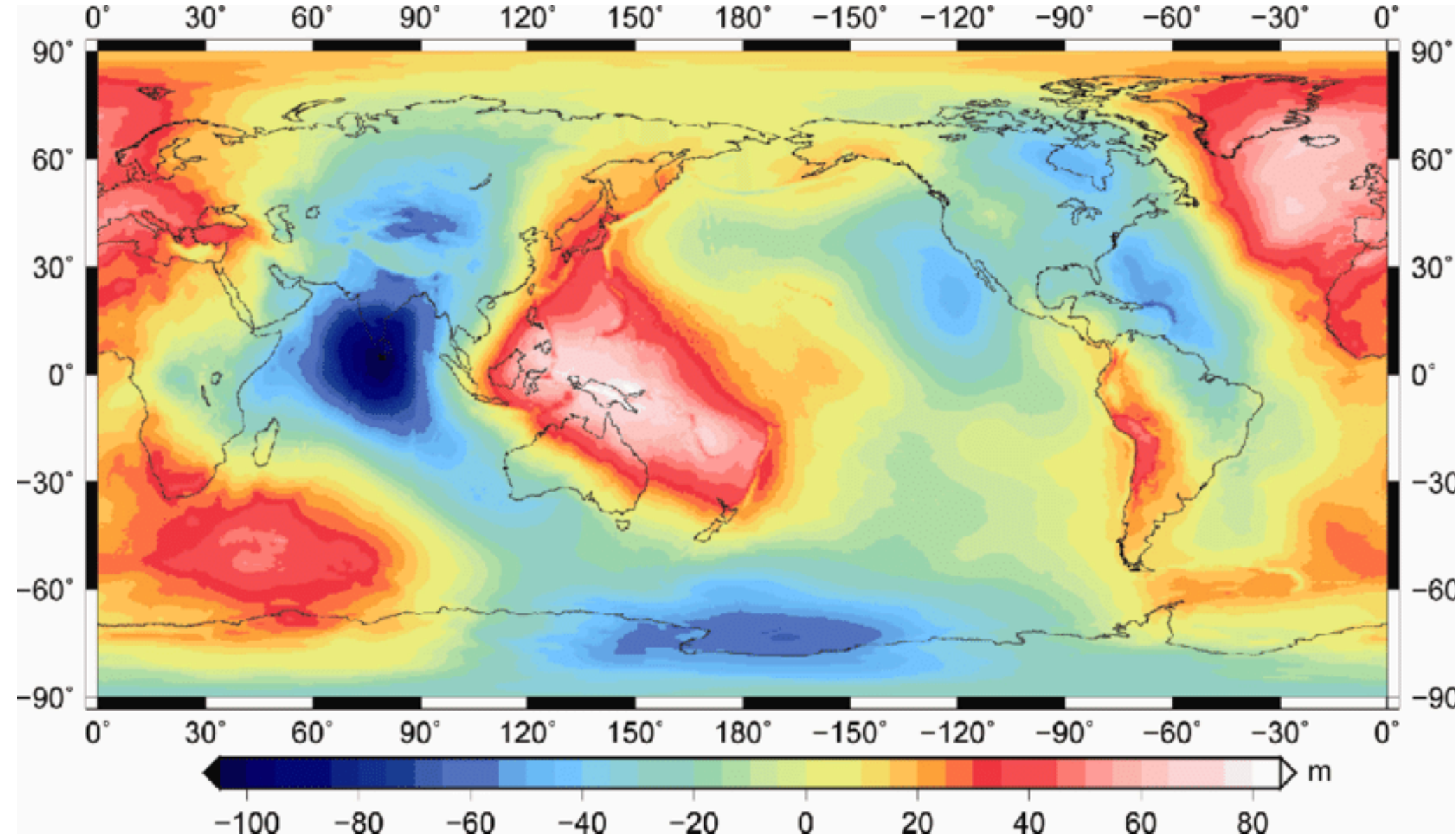
Geoid vs sea surface height

$$h=H+N$$



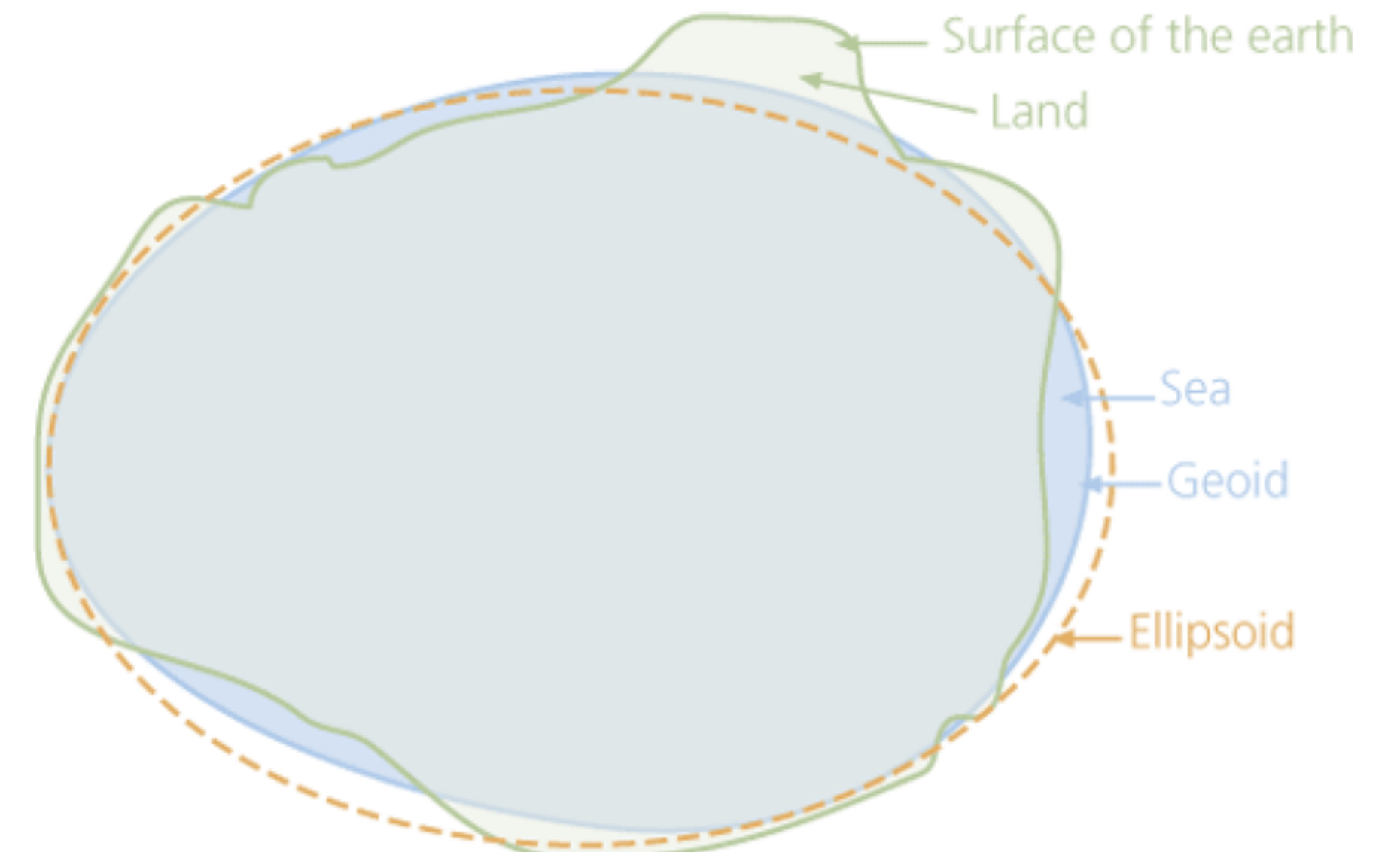
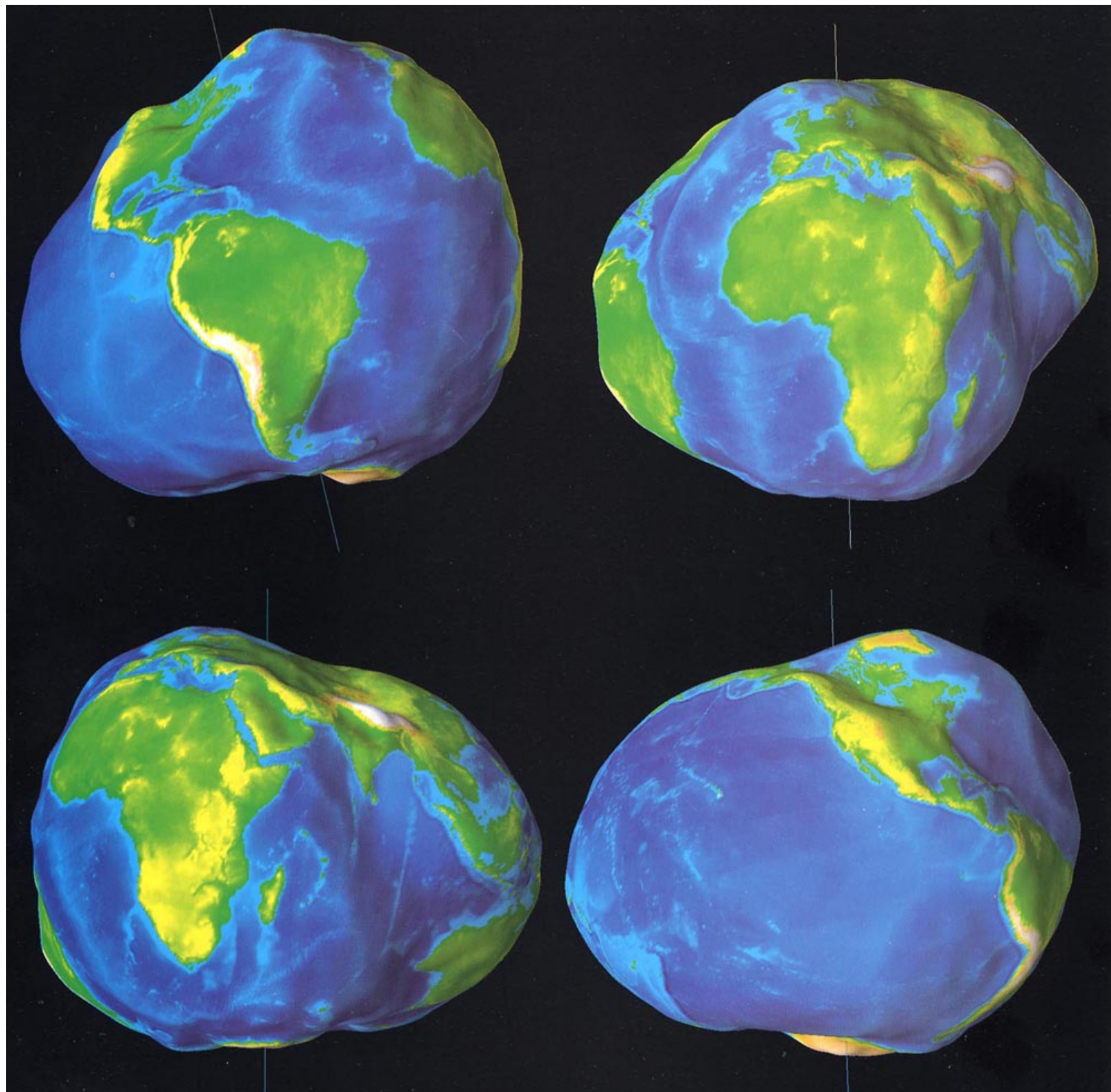
<http://www.dspmuranchi.ac.in/pdf/Blog/Basic%20Geodesy.pdf>

h=elipsoid height
H=orthometric height
N=geoid height



https://www.researchgate.net/figure/Global-geoid-from-EGM-2008-model-137_fig1_316255397

The geoid varies by hundreds of m from place to place, dynamic sea height typically varies by 1 m at most



http://geoide.es/pageID_3506376_3.html

<https://www.esri.com/news/arcuser/0703/geoid1of3.html>

The End