

Equable climates

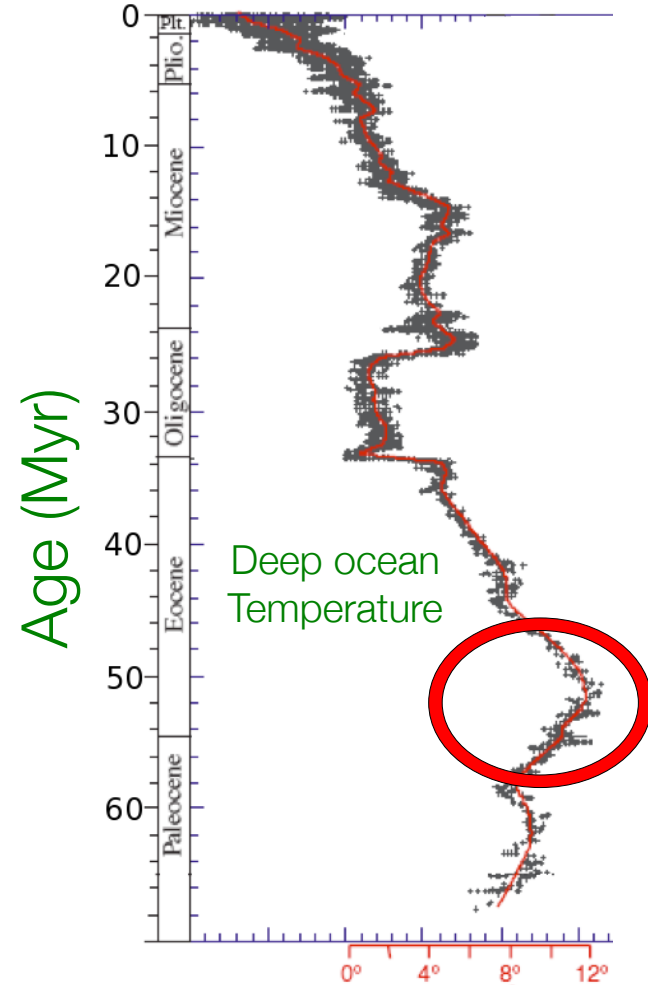
EPS 231 Climate dynamics
Eli Tziperman

56 to 34 Myr ago: Eocene

EON	ERA	PERIOD	EPOCH	Ma		
Phanerozoic	Cenozoic	Quaternary	Holocene	0.01		
			Pleistocene	Late	0.8	
				Early	1.8	
		Tertiary	Neogene	Pliocene	Late	3.6
					Early	5.3
					Late	11.2
			Miocene		Middle	16.4
					Early	23.7
					Late	28.5
		Oligocene		Early	33.7	
			Eocene		Late	41.3
					Middle	49.0
				Early	54.8	
		Paleogene	Paleocene		Late	61.0
					Early	65.0
					99.0	
		Mesozoic	Cretaceous		Late	99.0
					Early	144
			Jurassic		Late	159
				Middle	180	
	Triassic			Early	206	
				Late	227	
	Permian			Middle	242	
				Early	248	
	Paleozoic			Late	256	
				Early	290	
				Pennsylvanian	323	
				Mississippian	354	
			Devonian		Late	370
					Middle	391
				Early	417	
		Silurian		Late	423	
				Early	443	
Ordovician			Late	443		
		Middle	458			
		Early	470			
Cambrian		D	490			
		C	500			
		B	512			
		A	520			
		A	543			
Precambrian	Proterozoic		Late	900		
			Middle	1600		
			Early	2500		
	Archean		Late	3000		
			Early	3800?		

Warm climates
146–34 Myr

Gradual cooling over past 55 Myr



[Zachos et al., 2001]

Equable Climates



Frost-intolerant species in high-latitude continental climate regions

Cretaceous Coastal Environment



Hadrosaurus - Cretaceous



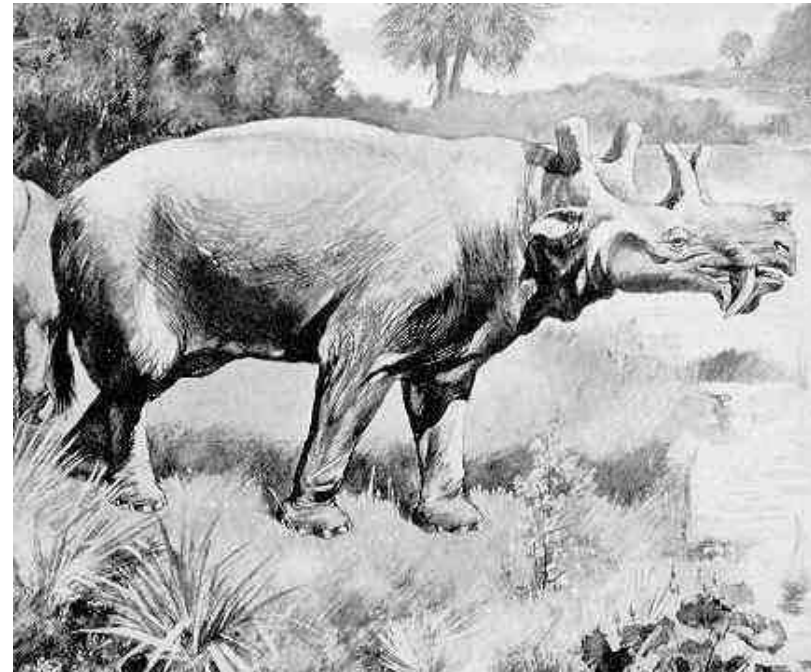
Artist: Karen Carr

Cretaceous Marine Environment



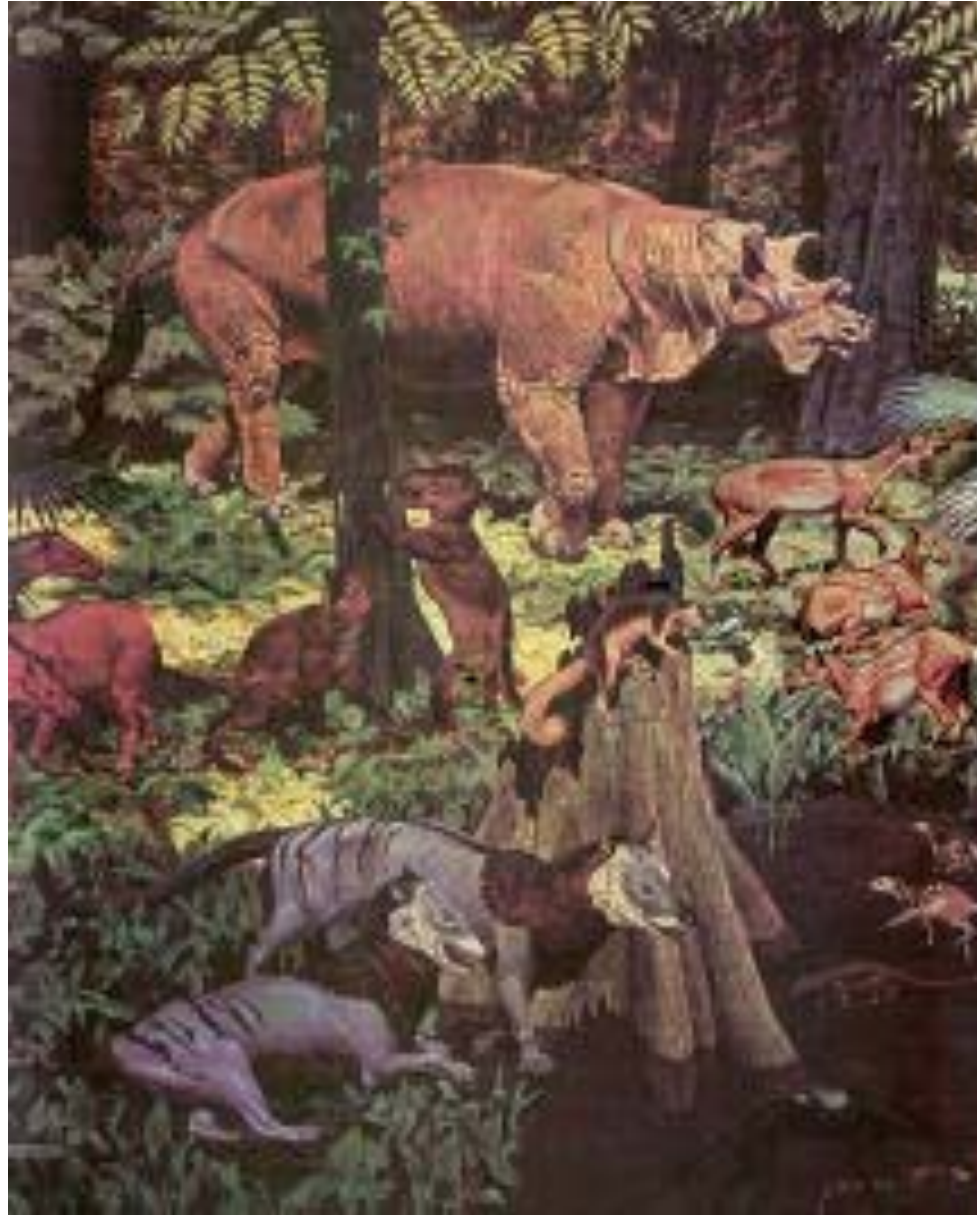
Artist: Karen Carr

Eobasileus - Eocene



Artist: Charles R. Knight

Eocene Mammals



Artist: Jay Matternes

“Equable” climate

1. Surface temperatures at the poles were closer to surface temperatures at the equator.
2. The high latitude seasonal cycle was smaller: winter and surface temperature were closer.

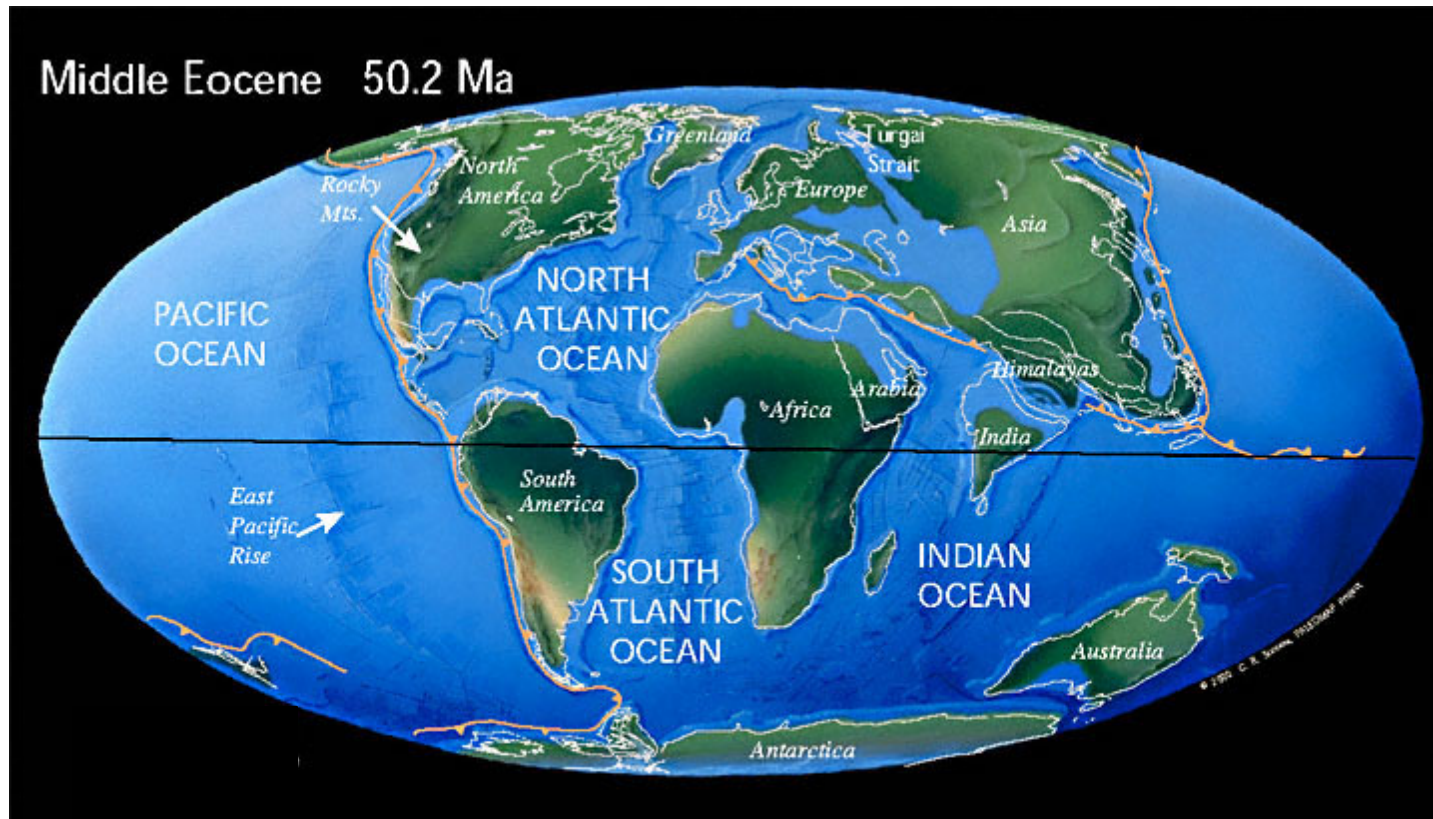
“Hothouse/Equable” climates ~146–34 Ma

Cretaceous

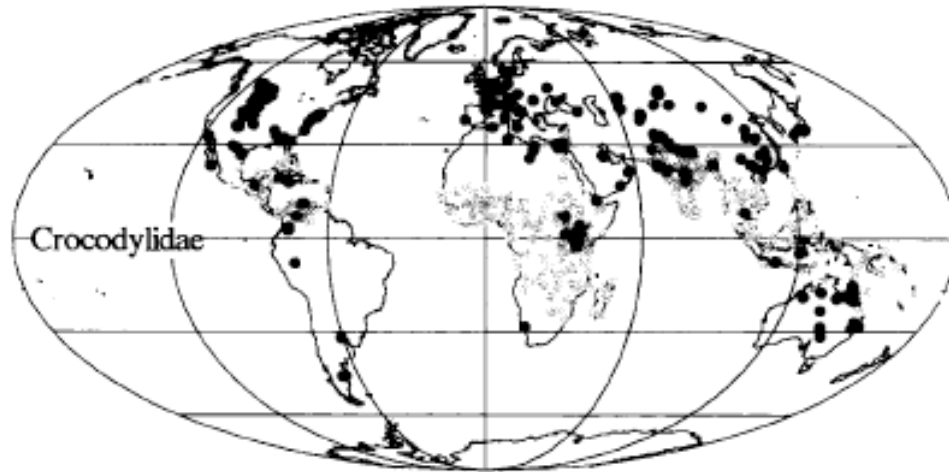
Paleocene

Eocene

- Higher global mean temperature
- Lower equator-to-pole temperature diff.
- Less high latitude seasonality
- No significant ice
- Tropical SSTs $>\approx$ modern
- Warm deep ocean
- $\text{CO}_2=500\text{--}2,000$ ppm?



Plant and animal fossils

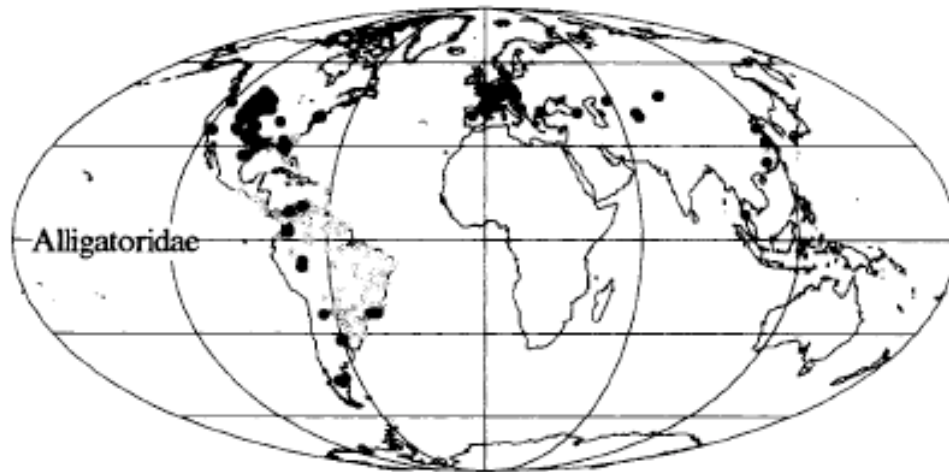


Crocodyles & Alligators today
need:

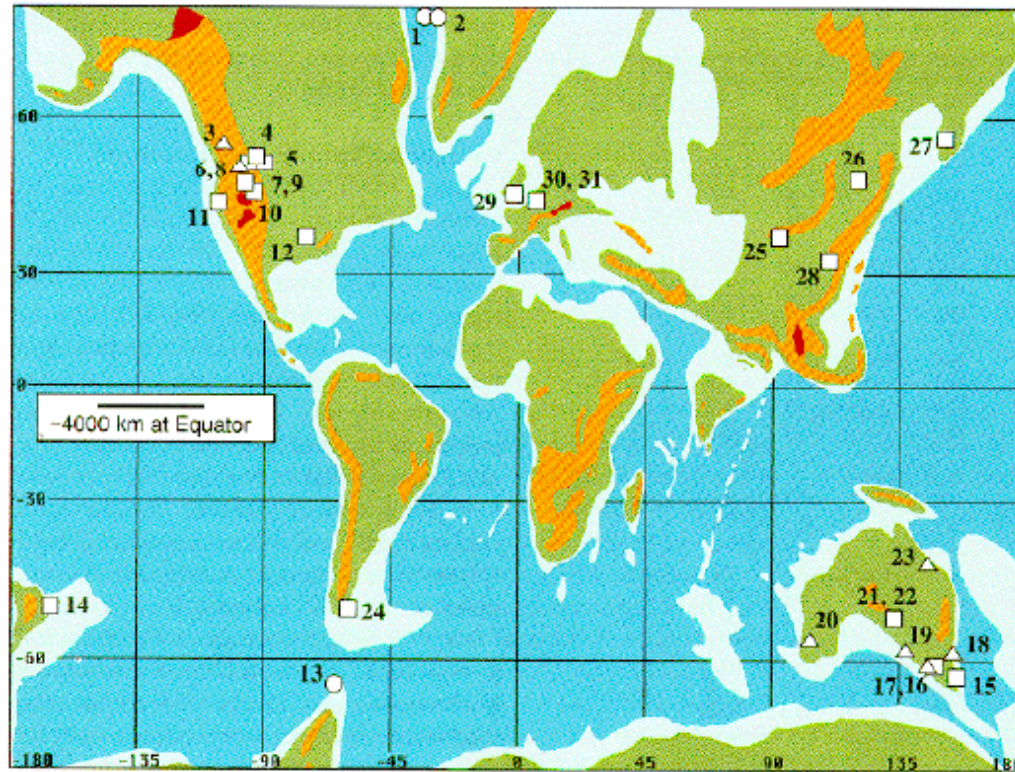
$$\text{MAT} > 14.2^{\circ}\text{C} + \text{CMM} > 5.5^{\circ}\text{C}$$

MAT: mean annual temperature

CMM: cold month mean



Eocene near living relative (NLR) Analysis



[Greenwood and Wing, 1995]

□ - palms

△ - cycads, gingers, tree ferns

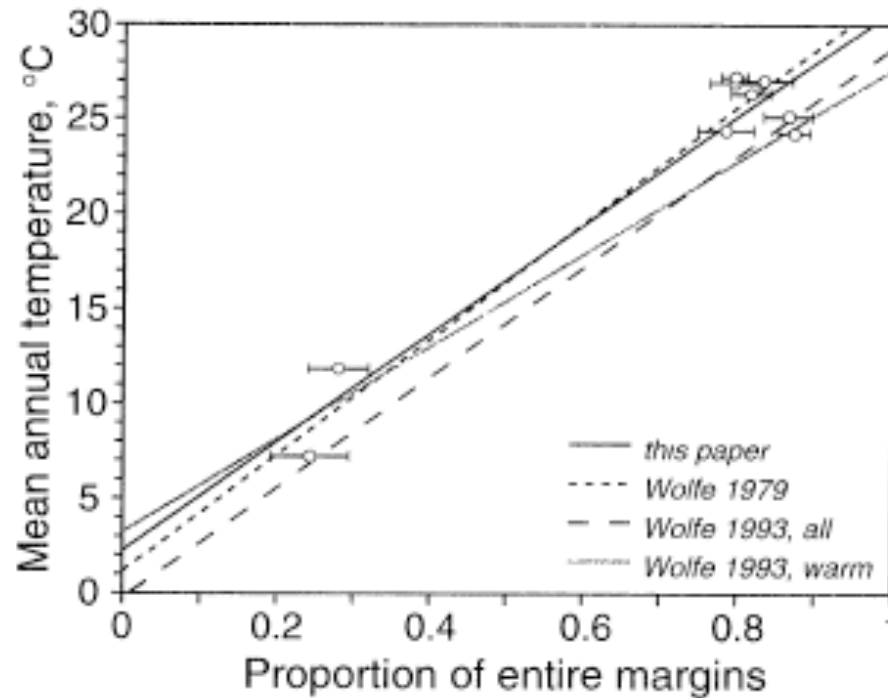
○ - no frost intolerant plants

■ - lowlands

■ - uplands

■ - higher uplands

Leaf Margin Analysis (LMA)



[Wilf, 1997]



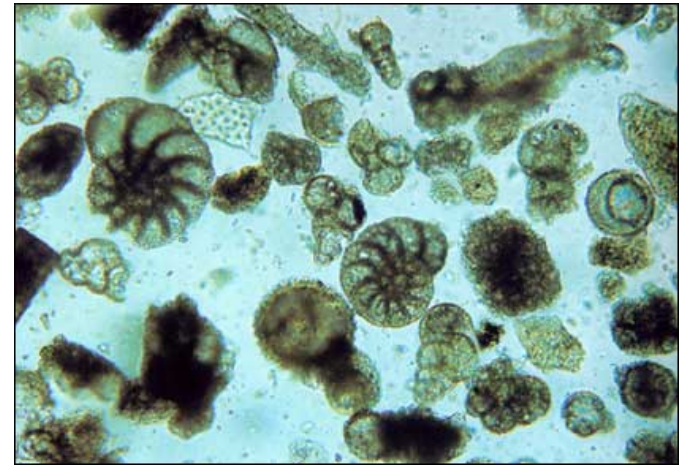
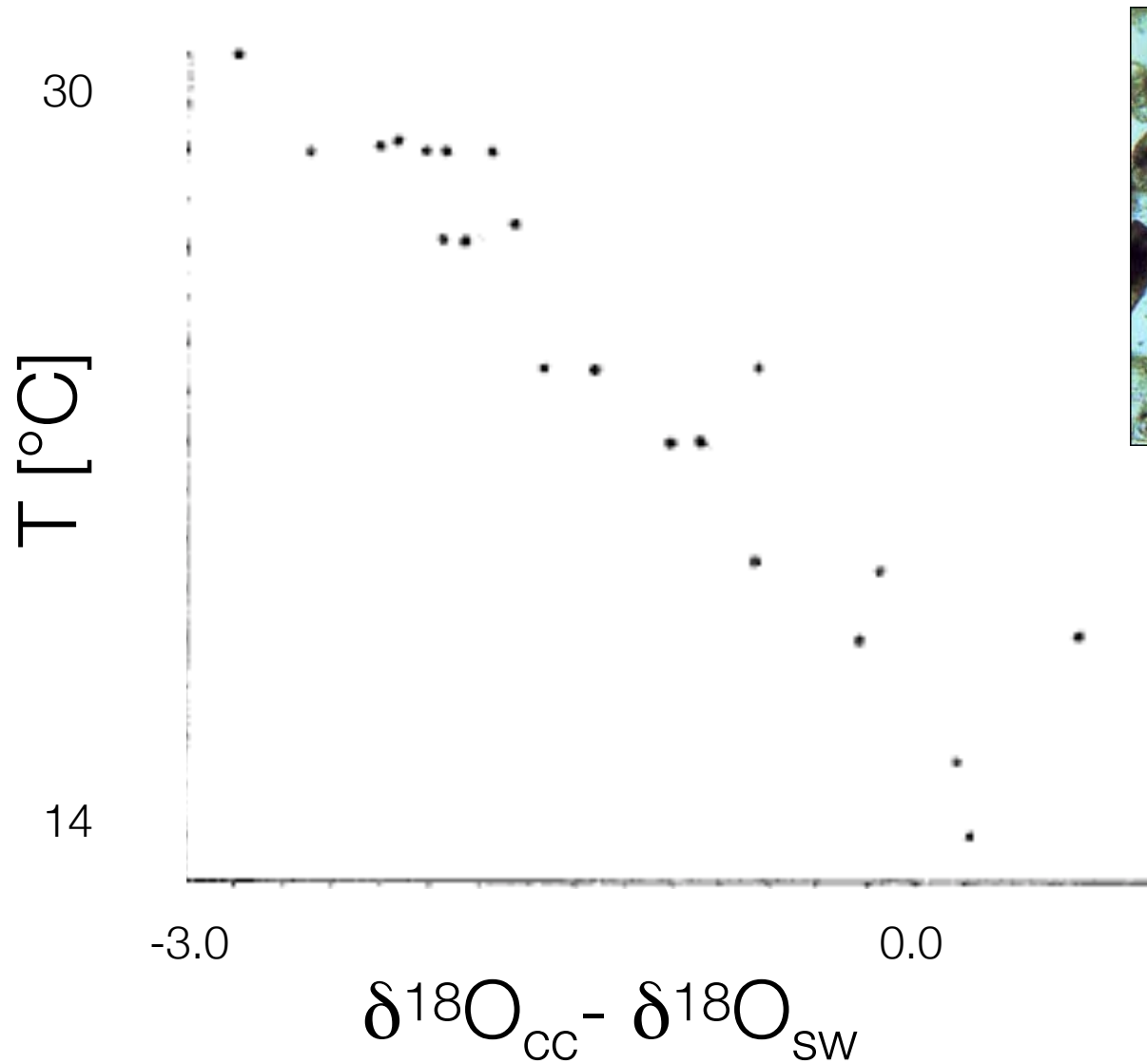
Eastern Redbud -
 Untoothed
 (Entire Margin)

American Elm - Toothed



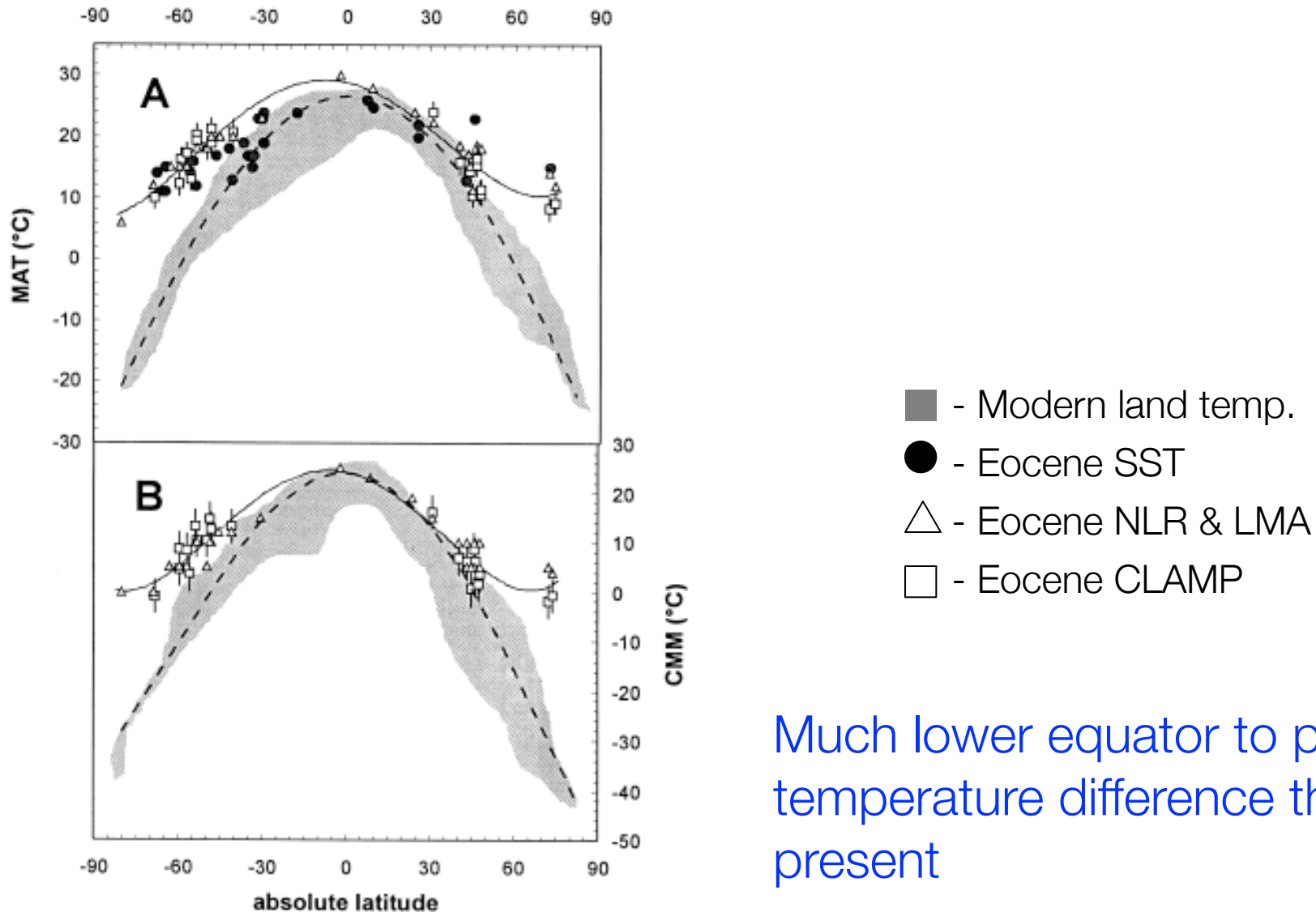
“The physiological basis for the MAT vs. leaf-margin correlation has never been adequately demonstrated.”
 [Wilf, 1997]

$\delta^{18}\text{O}$ Temperature reconstruction



[Erez and Luz, 1983]

Latitudinal temperature distribution



Much lower equator to pole temperature difference than at present

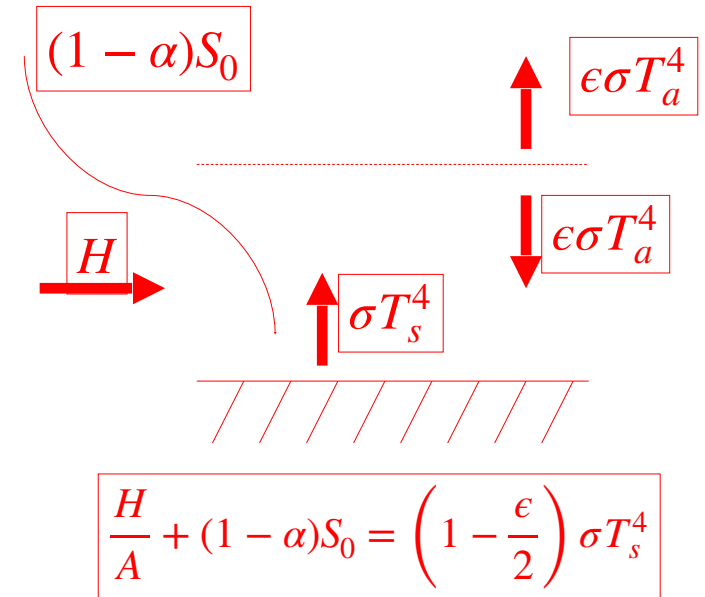
In-class workshop

Consider an energy balance model for the Arctic:

Modern climate:

S_0 (W/m^2)	H [PW]	ϵ	α
200	3.5	0.60	0.55

A =area north of 60N



- 1) Calculate the present-day Arctic temperature from this energy balance.
- 2) Calculate the changes to the mid-latitude heat transport required to increase the high latitude temperature by 20 °C

Energy balance for the Arctic: Back of the envelope...

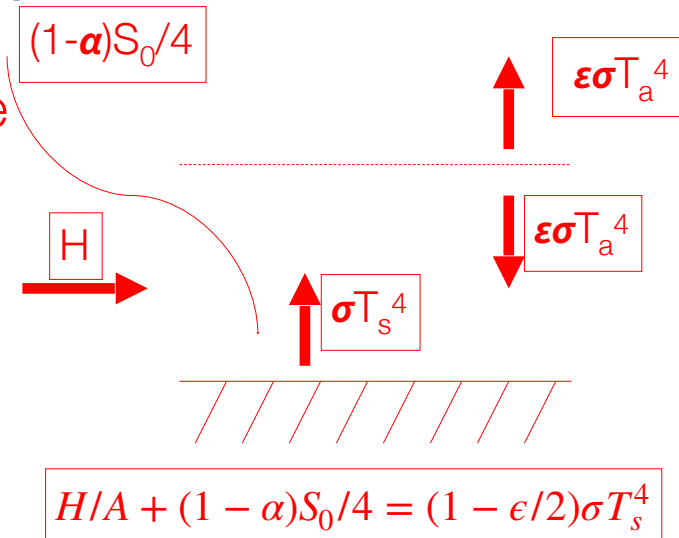


Changes required to reduce equator-to-pole temperature gradient by increasing CO₂ or meridional heat fluxes or albedo or long-wave emissivity (clouds!):

Modern climate:

T [C]	H [PW]	ϵ	α
-8.0	3.5	0.60	0.55

Energy-balance model



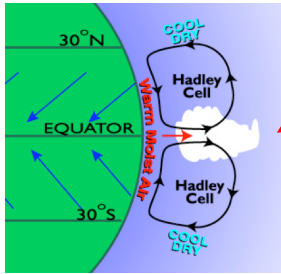
Changes required to increase high latitude temperature:

ΔT [C]	ΔH [PW]	$\Delta \epsilon$	[CO ₂] _{dry} [ppm]	[CO ₂] _{wet} [ppm]	$\Delta \alpha$
10.0	1.1	0.20	X2 ⁵ ≈9x10 ³	x2 ^{2.5} ≈2x10 ³	-0.15
15.0	1.7	0.28	x2 ^{7.5} ≈5x10 ⁴	x2 ^{3.75} ≈4x10 ³	-0.23

Proposed mechanisms

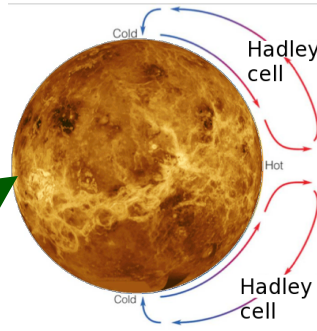
Equator-to-pole Hadley cell:

(1)



Today

Eocene?
(Like Venus...)

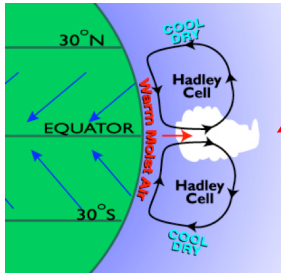


(B. Farrell, 1990)

Proposed mechanisms

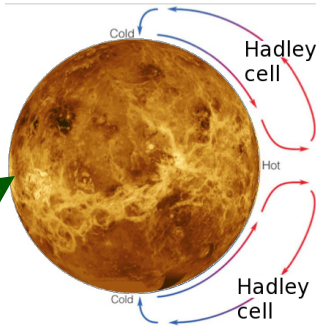
Equator-to-pole Hadley cell:

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(B. Farrell, 1990)



Polar Stratospheric Clouds (PSCs, 15-25 km)

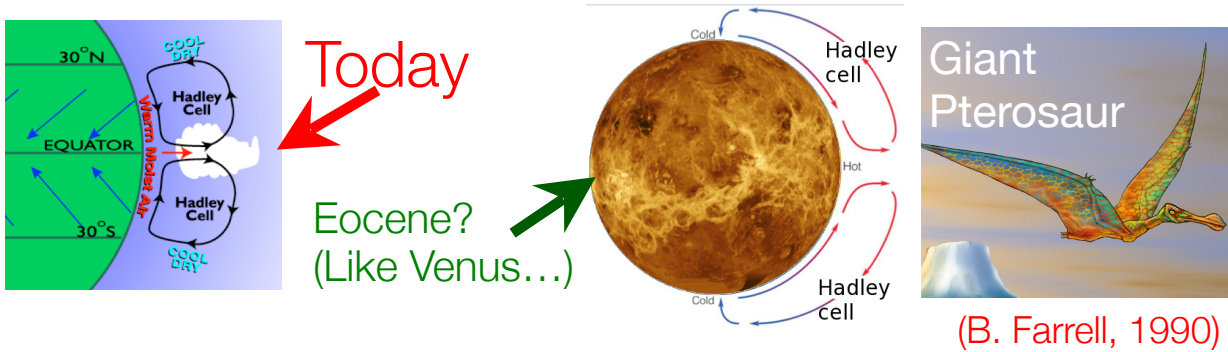
← PSCs at dusk over Arctic Sweden
due to methane: Sloan 1992;
weakening Brewer-Dobson circulation:
Kirk-Davidoff et al. 2002

(2)

Proposed mechanisms

Equator-to-pole Hadley cell:

(1)



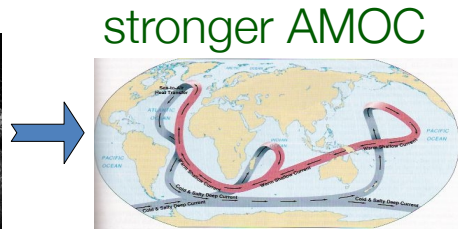
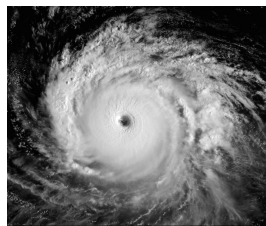
Polar Stratospheric Clouds (PSCs, 15-25 km)

← PSCs at dusk over Arctic Sweden
 due to methane: Sloan 1992;
 weakening Brewer-Dobson circulation:
 Kirk-Davidoff et al. 2002

(2)

Stronger hurricanes

(3)



Warmer high latitudes

(K. Emanuel, 2002)

Proposed mechanisms

Breakup of subtropical stratocumulus cloud decks at high SST

Causing albedo decrease and warming of mid-latitudes

Schneider et al 2019, (Bretherton et al)



(4)

<https://www.shutterstock.com/image-photo/aerial-view-layer-stratocumulus-clouds-369408491>

Proposed mechanisms

Breakup of subtropical stratocumulus cloud decks at high SST



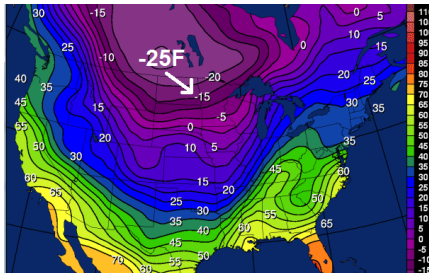
(4)

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Schneider et al 2019, (Bretherton et al)

<https://www.shutterstock.com/image-photo/aerial-view-layer-stratocumulus-clouds-369408491>

(5)



Arctic air suppression over high latitude land

By low cloud forming due to moisture arriving from over warmer ocean

Cronin & Tziperman 2015

Proposed mechanisms

Breakup of subtropical stratocumulus cloud decks at high SST



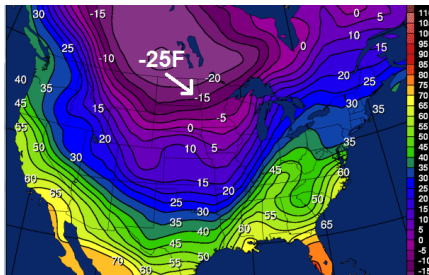
(4)

Causing albedo decrease and warming of mid-latitudes

Schneider et al 2019, (Bretherton et al)

<https://www.shutterstock.com/image-photo/aerial-view-layer-stratocumulus-clouds-369408491>

(5)



Arctic air suppression over high latitude land

By low cloud forming due to moisture arriving from over warmer ocean

Cronin & Tziperman 2015

Arctic convective cloud feedback

wintertime
deep Arctic
convection



high cloud
emissivity/
greenhouse
effect

Warmer
winter Arctic

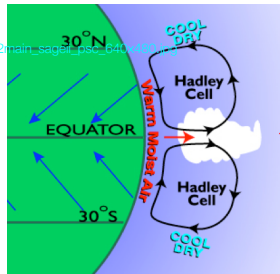
(6)

Abbot & Tziperman 2008

Equator-to-pole Hadley cell:

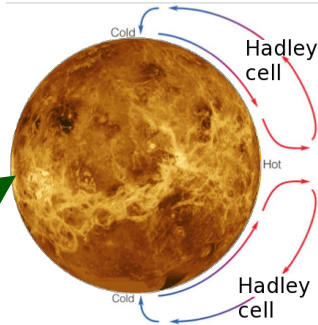
www.nasa.gov/images/content/65932main_sag_01_03_04_044.jpg

(1)



Today

Eocene?
(Like Venus...)



(B. Farrell, 1990)

notes:

- Hadley cell Held/Hou model from Vallis.
- Heuristic equator-to-pole Hadley cell idea based on Farrell (1990).

2986

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Equable Climate Dynamics

BRIAN F. FARRELL

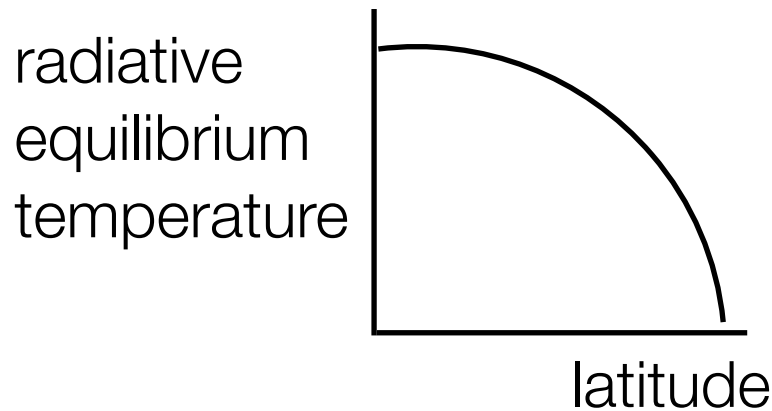
Department of Earth and Planetary Sciences, Harvard University, Cambridge, Massachusetts

In-class workshop

Use angular momentum conservation to calculate the subtropical jet speed at 30N

Equator-to-pole Hadley cell in class workshop

Consider the radiative-convective equilibrium temperature profile:



Draw the expected temperature profile including the effects of atmospheric heat transport



Polar Stratospheric Clouds (PSCs, 15-25 km)

← PSCs at dusk over Arctic Sweden
due to methane: Sloan 1992;
weakening Brewer-Dobson circulation:
Kirk-Davidoff et al. 2002

(2)

[www.nasa.gov/images/content/
65932main_sageii_psc_640x480.jpg](http://www.nasa.gov/images/content/65932main_sageii_psc_640x480.jpg)

Polar stratospheric clouds

PSCs form at very low temperatures, below $-78\text{ }^{\circ}\text{C}$, at 15–30 km height, during winter, in polar areas, within polar stratospheric vortex



wikipedia



PSC, Elverum, Norway.

A type II (water) PSC showing iridescence

Due to their high altitude & Earth [surface curvature](#), PSCs receive sunlight from below the horizon & reflect it to the ground, shining brightly well before [dawn](#) or after [dusk](#)

Composition: water ice, sulfuric acid H_2SO_4 ; nitric acid (HNO_3)

Polar stratospheric clouds in equable climate 1.0

Possible methane-induced polar warming in the early Eocene

**L. Cirbus Sloan, James C. G. Walker, T. C. Moore Jr,
David K. Rea & James C. Zachos 1992**

The proposed feedback:

warmer climate

- ➔ higher methane CH_4 emissions by anaerobic bacteria from swamps
- ➔ greenhouse effect in the troposphere & — unlike water — able to make it to the stratosphere (liquid only at $-161.5\text{ }^\circ\text{C}$ at 1 atm)
- ➔ oxidizes into CO_2 and H_2O ($\text{CH}_4 + 2\text{O}_2 = \text{CO}_2 + 2\text{H}_2\text{O}$)
- ➔ H_2O forms PSCs
- ➔ further warms the poles.

PSCs: stratospheric temperature & circulation

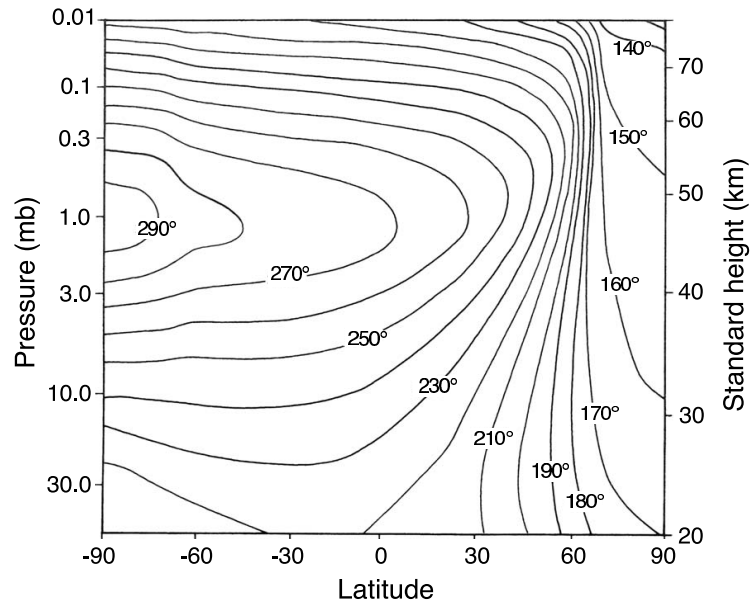


Fig. 13.11 The zonally-averaged radiative-equilibrium temperature in in January. The downwards solar radiation at the top of the atmosphere is given, and the upwards radiative flux into the stratosphere is based on observed properties, including temperature, of the troposphere.¹⁸

PSCs: stratospheric temperature & circulation

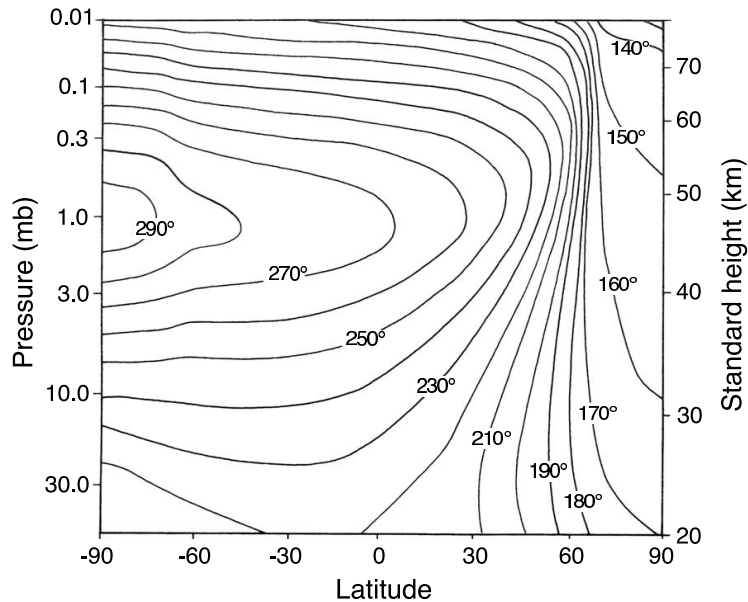


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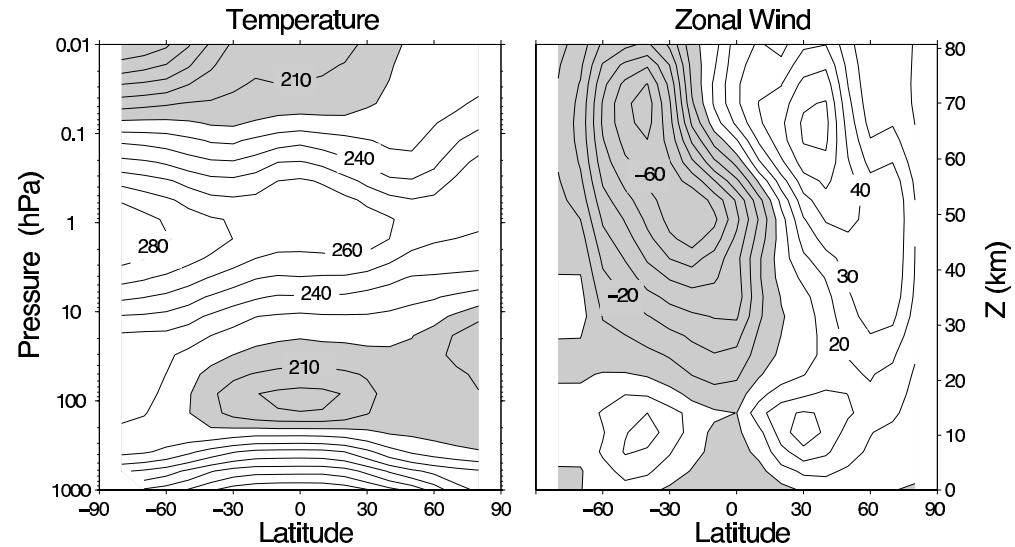


Fig. 13.12 The zonally averaged temperature and zonal wind in January. Temperature contour interval is 10 K, and values less than 220 K are shaded. Zonal wind contours are 10 m s^{-1} and negative (westward) values are shaded.¹⁹

PSCs: stratospheric temperature & circulation

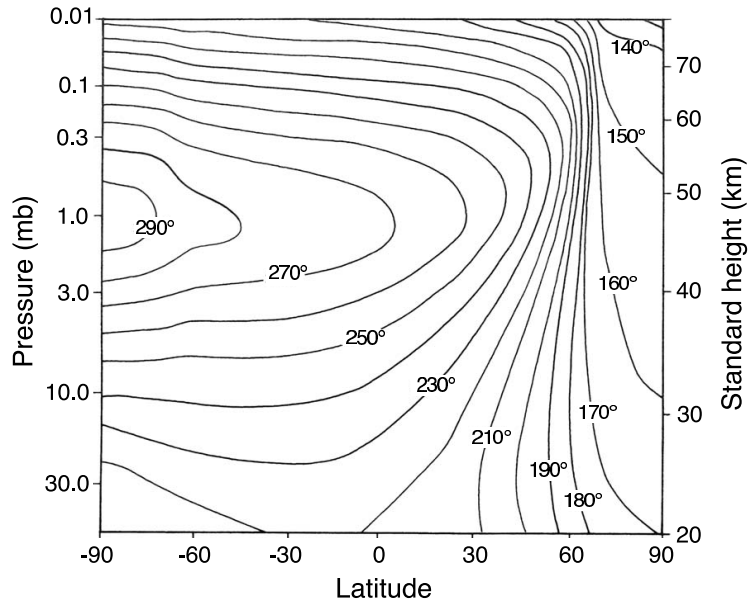


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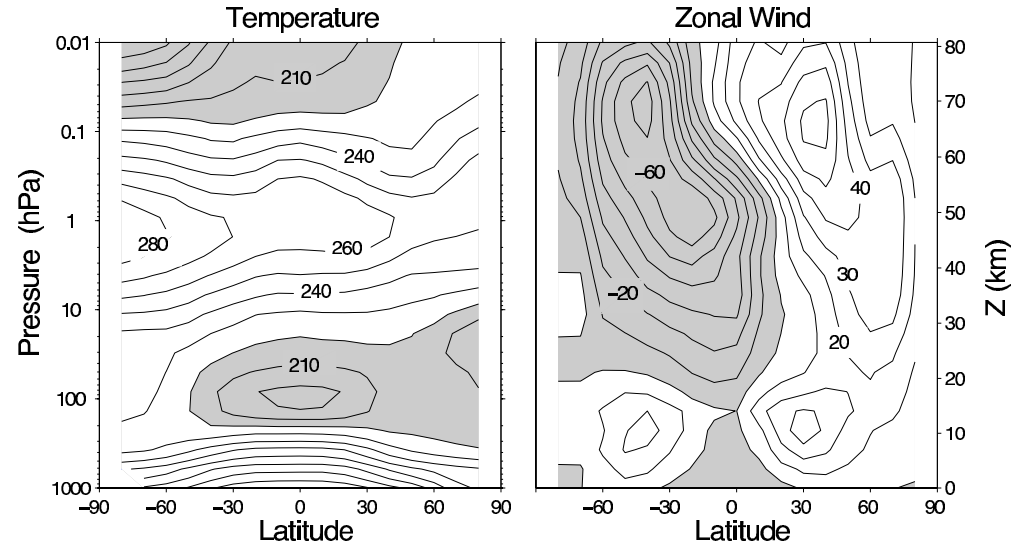
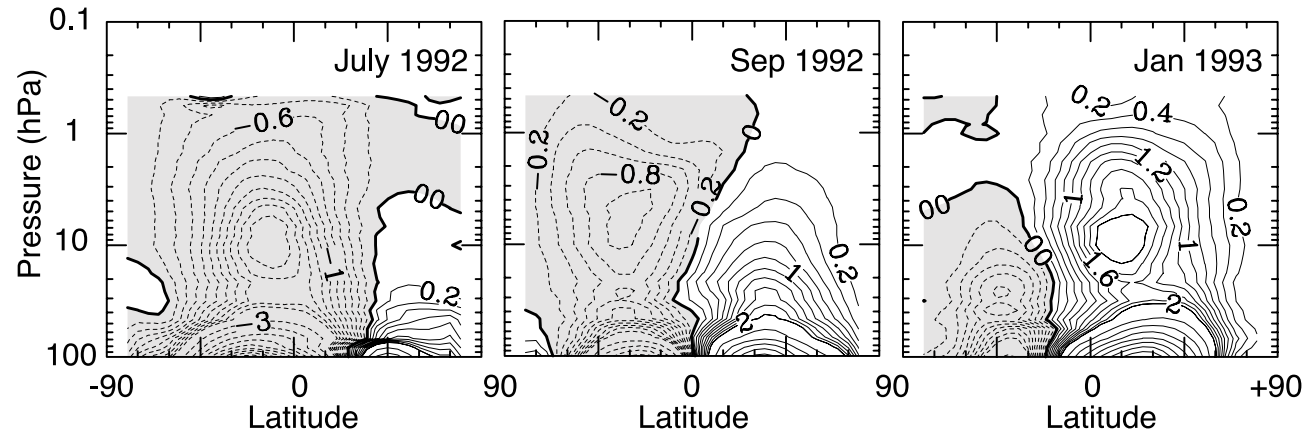


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Brewer Dobson circulation

Fig. 13.13 The observed mass-weighted streamfunction in the stratosphere, in Sverdrups (10^9 kg s^{-1}). The circulation is clockwise where the contours are solid. Note the stronger circulation in the winter hemispheres, whereas the equinoctial circulation (September) is more inter-hemispherically symmetric.²¹



Polar stratospheric clouds in equable climate 2.0

On the feedback of stratospheric clouds on polar climate

Daniel B. Kirk-Davidoff, Daniel P. Schrag, and James G. Anderson **2002**

The propose feedback:

warmer climate,

- ➔ warmer troposphere in polar areas
- ➔ lower equator-to-pole temperature difference
- ➔ weaker mid-latitude weather systems
- ➔ weaker wave propagation into the stratosphere
- ➔ weaker Brewer-Dobson circulation
- ➔ colder poles in Stratosphere
- ➔ more PSC
- ➔ warmer troposphere in polar areas

Polar stratospheric clouds: TEM and B-D circulation

$$q = \beta y + \left[\nabla^2 + \frac{\partial}{\partial z} \left(\frac{f_0^2}{N^2} \frac{\partial}{\partial z} \right) \right] \psi.$$

$$\frac{\partial q}{\partial t} + J(\psi, q) = 0, \quad \zeta = \nabla^2 \psi, \quad b = f_0 \frac{\partial \psi}{\partial z},$$

**Understanding the driving of
the B-D circulation by wave flux**

Polar stratospheric clouds: TEM and B-D circulation

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$$\overline{v'q'} = -\frac{\partial}{\partial y} \overline{u'v'} + \frac{\partial}{\partial z} \left(\frac{f_0}{N^2} \overline{v'b'} \right)$$

**Understanding the driving of
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$$\mathcal{F} \equiv -\overline{u'v'} \mathbf{j} + \frac{f_0}{N^2} \overline{v'b'} \mathbf{k}$$

$$\overline{v'q'} = \nabla_x \cdot \mathcal{F},$$

Eliaassen-Palm
flux

Understanding the driving of
the B-D circulation by wave flux

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$$\overline{v'q'} = \nabla_x \cdot \mathcal{F},$$

← Eliassen-Palm flux

$$\overline{v}^* = \overline{v} - \frac{\partial}{\partial z} \left(\frac{1}{N^2} \overline{v'b'} \right)$$

residual velocities

$$\overline{w}^* = \overline{w} + \frac{\partial}{\partial y} \left(\frac{1}{N^2} \overline{v'b'} \right)$$

Understanding the driving of the B-D circulation by wave flux

Polar stratospheric clouds: TEM and B-D circulation

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$$\frac{\partial b}{\partial t} + J(\psi, b) + w N^2 = J,$$

$$\frac{\partial \bar{v}^*}{\partial y} + \frac{\partial \bar{w}^*}{\partial z} = 0.$$

$$\frac{\partial \bar{u}}{\partial t} = f_0 \bar{v}^* + \overline{v'q'} + \bar{F}$$

$$\frac{\partial \bar{b}}{\partial t} = -N^2 \bar{w}^* + \bar{J}$$

$$\overline{v'q'} = -\frac{\partial}{\partial y} \overline{u'v'} + \frac{\partial}{\partial z} \left(\frac{f_0}{N^2} \overline{v'b'} \right)$$

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Understanding the driving of the B-D circulation by wave flux

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$$\frac{\partial \bar{b}}{\partial t} = -N^2 \bar{w}^* + \bar{J}$$

$$\overline{v'q'} = -\frac{\partial}{\partial y} \overline{u'v'} + \frac{\partial}{\partial z} \left(\frac{f_0}{N^2} \overline{v'b'} \right)$$

$$\mathcal{F} \equiv -\overline{u'v'} \mathbf{j} + \frac{f_0}{N^2} \overline{v'b'} \mathbf{k}$$

$$\overline{v'q'} = \nabla_x \cdot \mathcal{F},$$

← Eliassen-Palm flux

$$\bar{v}^* = \bar{v} - \frac{\partial}{\partial z} \left(\frac{1}{N^2} \overline{v'b'} \right)$$

residual velocities

$$\bar{w}^* = \bar{w} + \frac{\partial}{\partial y} \left(\frac{1}{N^2} \overline{v'b'} \right)$$

Understanding the driving of the B-D circulation by wave flux

Polar stratospheric clouds: TEM and B-D circulation

$$q = \beta y + \left[\nabla^2 + \frac{\partial}{\partial z} \left(\frac{f_0^2}{N^2} \frac{\partial}{\partial z} \right) \right] \psi.$$

$$\frac{\partial q}{\partial t} + J(\psi, q) = 0, \quad \zeta = \nabla^2 \psi, \quad b = f_0 \frac{\partial \psi}{\partial z},$$

$$\frac{\partial b}{\partial t} + J(\psi, b) + w N^2 = J,$$

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$$\frac{\partial \overline{v}^*}{\partial y} + \frac{\partial \overline{w}^*}{\partial z} = 0.$$

~~$$\frac{\partial \overline{v}}{\partial t} = f_0 \overline{v}^* + \overline{v'q'} + \overline{F}$$~~

$$\frac{\partial \overline{b}}{\partial t} = -N^2 \overline{w}^* + \overline{J}$$

wave forcing

$$-f_0 \overline{v}^* \approx \overline{v'q'}, > 0$$

Understanding the driving of the B-D circulation by wave flux

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wave forcing

$$-f_0 \bar{v}^* \approx \overline{v'q'}, > 0$$

Eddy q' flux is down gradient, $d\bar{q}/dy \approx \beta > 0$, which means equatorward: $\overline{v'q'} < 0$

➔ $\bar{v}^* > 0$ in NH

➔ poleward B-D circulation

Understanding the driving of the B-D circulation by wave flux

In-class workshop

$$q = \beta y + \left[\nabla^2 + \frac{\partial}{\partial z} \left(\frac{f_0^2}{N^2} \frac{\partial}{\partial z} \right) \right] \psi. \quad \frac{\partial \bar{u}}{\partial t} = f_0 \bar{v}^* + \overline{v'q'} + \bar{F}$$

given the above, and the fact that the eddy flux of PV is from high to low values of \bar{q} because it is a conserved quantity, what is the direction of the Brewer-Dobson circulation

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Considering more carefully vertical wave propagation
in equable climate (Korty and Emanuel)

Polar stratospheric clouds: vertical wave propagation

$$q = \nabla^2 \psi + f + \frac{f_0^2}{\rho_R} \frac{\partial}{\partial z} \left(\frac{\rho_R}{N^2} \frac{\partial \psi}{\partial z} \right)$$

$$\frac{\partial q}{\partial t} + J(\psi, q) = 0, \quad \zeta = \nabla^2 \psi,$$

$$\rho_R = \rho_0 e^{-z/H}$$

$$\psi = -\bar{u}(z)y + \psi',$$

$$\frac{\partial q'}{\partial t} + \bar{u} \frac{\partial q'}{\partial x} + v' \frac{\partial \bar{q}}{\partial y} = 0,$$

$$\frac{\partial \bar{q}}{\partial y} = \beta - \frac{f_0^2}{\rho_R} \frac{\partial}{\partial z} \left(\frac{\rho_R}{N^2} \frac{\partial \bar{u}}{\partial z} \right)$$

$$\left(\frac{\partial}{\partial t} + \bar{u} \frac{\partial}{\partial x} \right) \left[\nabla^2 \psi' + \frac{f_0^2}{\rho_R} \frac{\partial}{\partial z} \left(\frac{\rho_R}{N^2} \frac{\partial \psi'}{\partial z} \right) \right] + \frac{\partial \psi'}{\partial x} \left[\beta - \frac{f_0^2}{\rho_R} \frac{\partial}{\partial z} \left(\frac{\rho_R}{N^2} \frac{\partial \bar{u}}{\partial z} \right) \right] = 0.$$

Polar stratospheric clouds: vertical wave propagation

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surface b.c $w = \mathbf{u} \cdot \nabla h_b$

$$\psi' = \text{Re } \tilde{\psi}(z) \sin ly e^{ik(x-ct)},$$

$$\left[\frac{f_0^2}{\rho_R} \frac{\partial}{\partial z} \left(\frac{\rho_R}{N^2} \frac{\partial \tilde{\psi}}{\partial z} \right) \right] = \tilde{\psi} \left(K^2 - \frac{\partial \bar{q} / \partial y}{\bar{u} - c} \right)$$

Assume constant \bar{u} , N^2 and let,

$$\Phi(z) = \tilde{\psi}(z) \left(\frac{\rho_R}{\rho_R(0)} \right)^{1/2} = \tilde{\psi}(z) e^{-z/2H}$$

$$\left(\frac{\partial}{\partial t} + \bar{u} \frac{\partial}{\partial x} \right) \left[\nabla^2 \psi' + \frac{f_0^2}{\rho_R} \frac{\partial}{\partial z} \left(\frac{\rho_R}{N^2} \frac{\partial \psi'}{\partial z} \right) \right]$$

$$+ \frac{\partial \psi'}{\partial x} \left[\beta - \frac{f_0^2}{\rho_R} \frac{\partial}{\partial z} \left(\frac{\rho_R}{N^2} \frac{\partial \bar{u}}{\partial z} \right) \right] = 0.$$

Polar stratospheric clouds: vertical wave propagation

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$$\rightarrow \frac{d^2 \Phi}{dz^2} + m^2 \Phi = 0,$$

$$m^2 = \frac{N^2}{f_0^2} \left(\frac{\beta}{\bar{u} - c} - K^2 - \gamma^2 \right),$$

$$\gamma^2 = f_0^2 / (4N^2 H^2) = 1 / (2L_d)^2$$

vertical propagation: if $m^2 > 0$

Vallis AOFD

Polar stratospheric clouds: vertical wave propagation

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vertical propagation: if $m^2 > 0$

stationary waves: $c = 0$

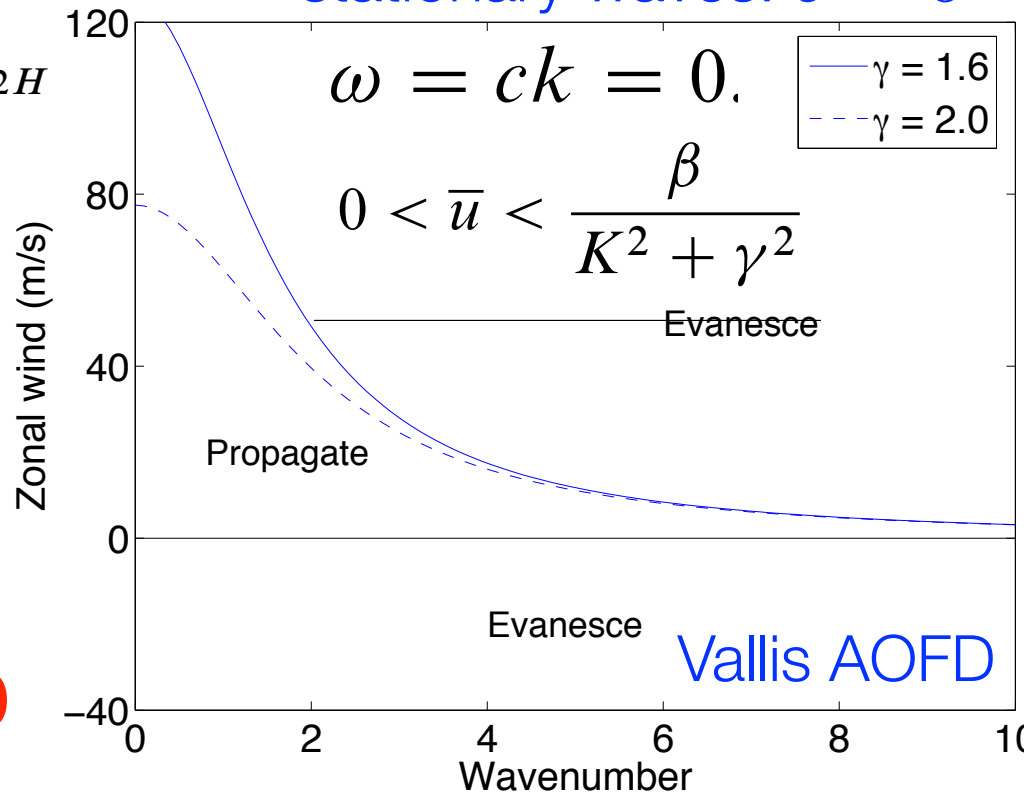


Figure 13.7 The boundary between propagating and evanescent waves as a function of zonal wind & wavenumber, using (13.61), for $N=2 \times 10^{-2} \text{s}^{-1}$, $\gamma = 1.6$ ($\gamma = 2$) corresponding to a scale height of 7 km (5.5 km); deformation radius NH/f of 1,400 km (1,100 km).

vertical propagation in class workshop

Consider the equation

$$\frac{d^2 \Phi}{dz^2} + m^2 \Phi = 0,$$

$$m^2 = \frac{N^2}{f_0^2} \left(\frac{\beta}{\bar{u} - c} - K^2 - \gamma^2 \right),$$

$$\gamma^2 = f_0^2 / (4N^2 H^2) = 1 / (2L_d)^2$$

- A. Analytically: for what values of \bar{u} do we expect vertical propagation, assuming stationary waves ($\omega = 0$)
- B. Suppose $N = 2 \times 10^{-2} \text{ s}^{-1}$; $H = 7 \text{ km}$, and $\bar{u} = 40 \text{ m/s}$, f_0 at 60N . what values of k propagate? We want that in units of n , where $n = kL_x / 2\pi$ and L_x is the length of the equator.

PSCs: surprising wave propagation into stratosphere in equable climate

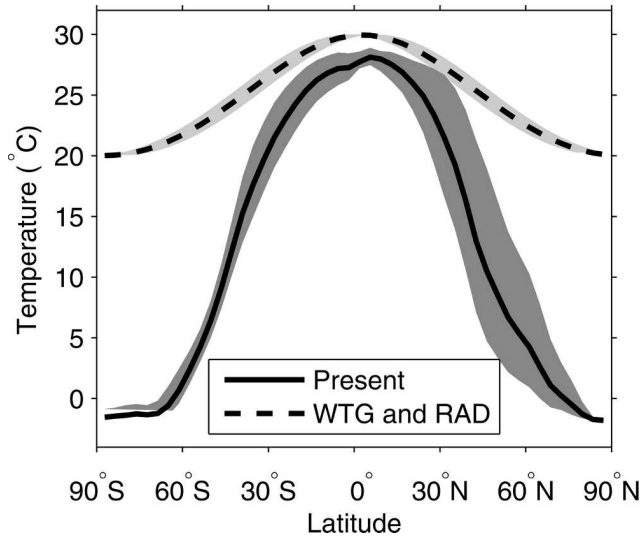
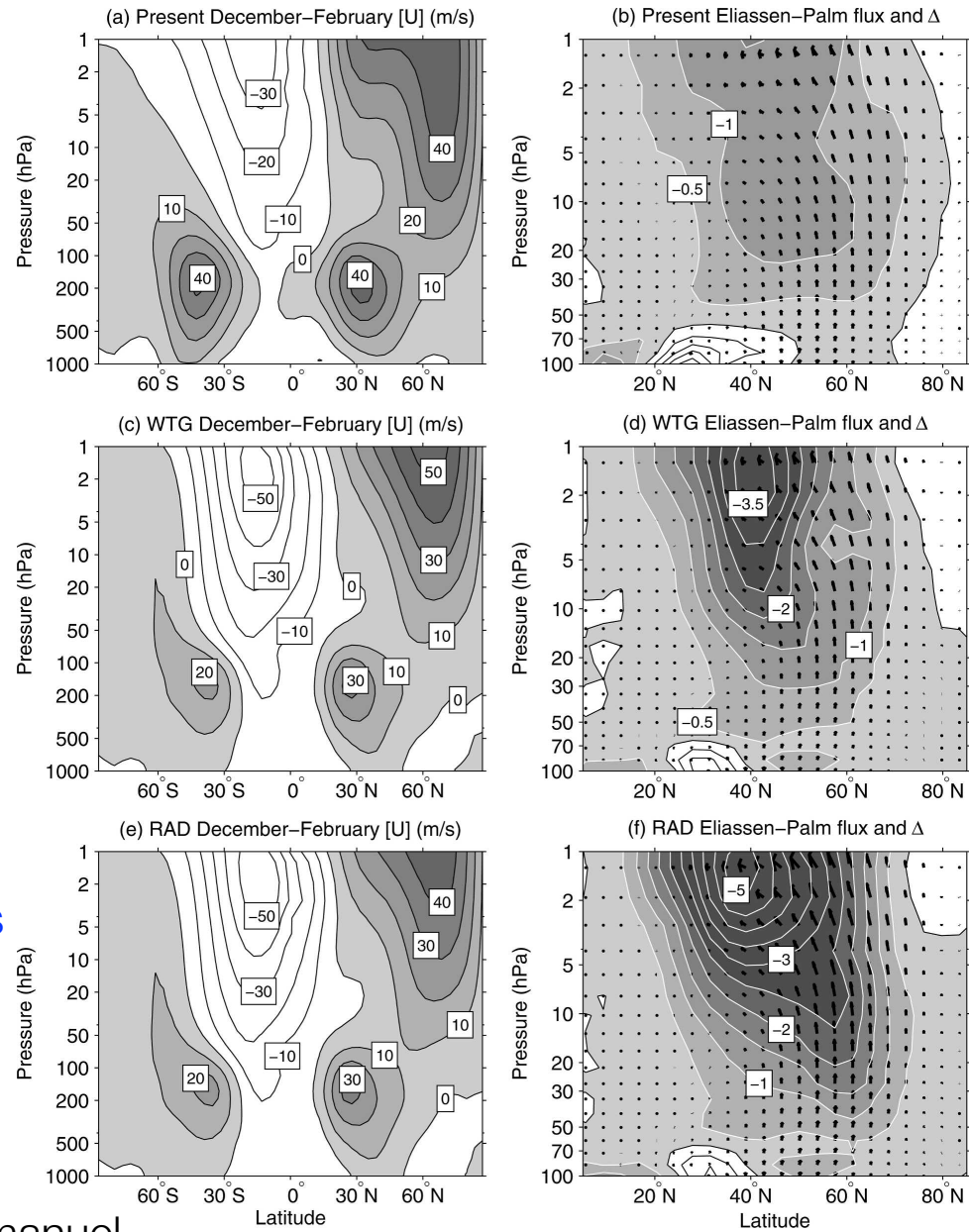


FIG. 1. Zonal- & annual-mean SSTs prescribed in the simulations. Gray bands show temporal range of zonal mean SST.

3 runs: present-day, WTG with present-day CO_2 , WTG with high CO_2 (RAD)

FIG. 3. (a) Zonal-mean zonal wind averaged over the last 5 DJF of Present; westerly winds are shaded. (b) EP (arrows) & its divergence Δ (contours) in Northern Hemisphere stratosphere @ Present; Δ units: 10^{15} m^3 . As in (a), (b) but for (c), (d) WTG and (e), (f) RAD.



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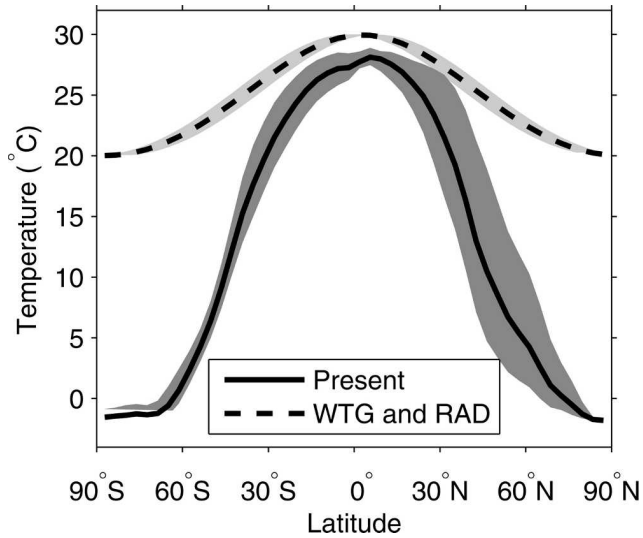
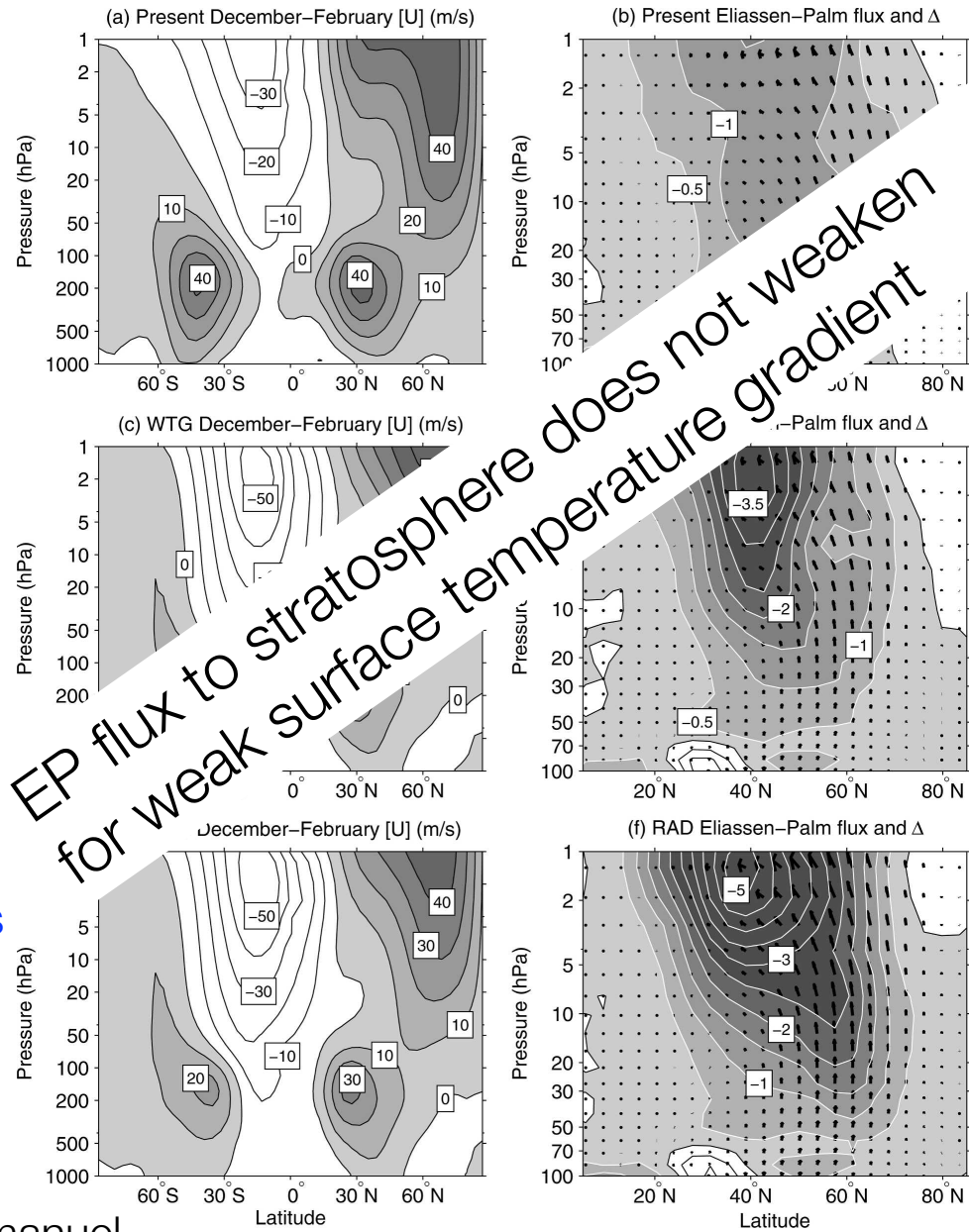


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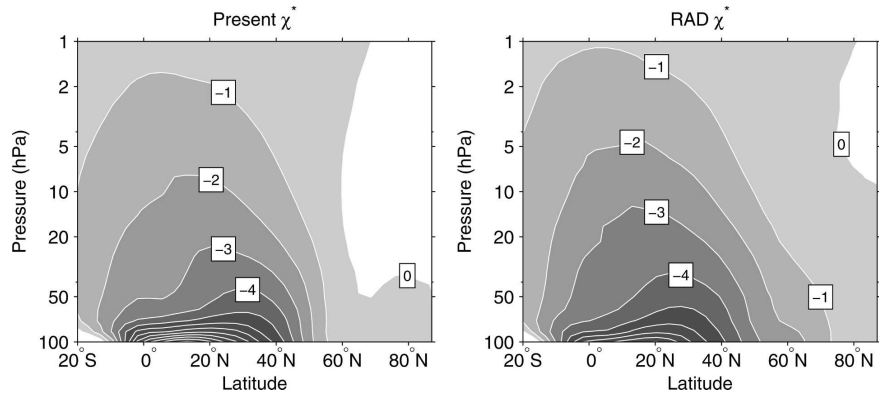
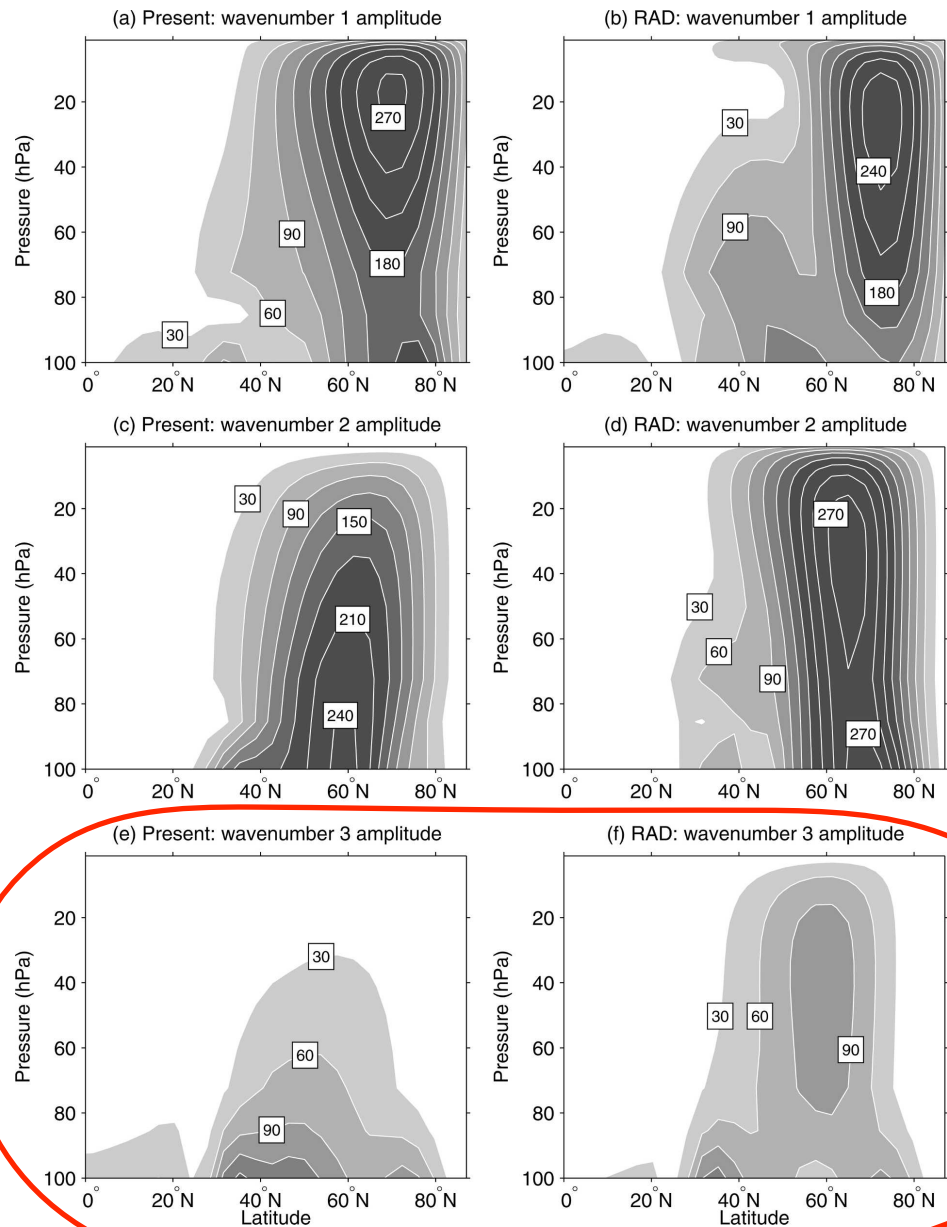


FIG. 5. The residual mean circulation in the stratosphere for (a) Present and (b) RAD. The flow circulates clockwise around negative contours. Contours are plotted and labeled every 10^9 kg s^{-1} .

FIG. 4. Amplitude of wavenumber 1 (normalized by $\sqrt{p/p_o}$ to compensate for increasing amplitudes with decreasing density) in (a) Present; (b) RAD from data averaged over last five DJFs; units=m. As in (a), (b) but for (c), (d) wavenumber 2 and (e), (f) wavenumber 3.



PSCs: surprising wave propagation into stratosphere in equable climate

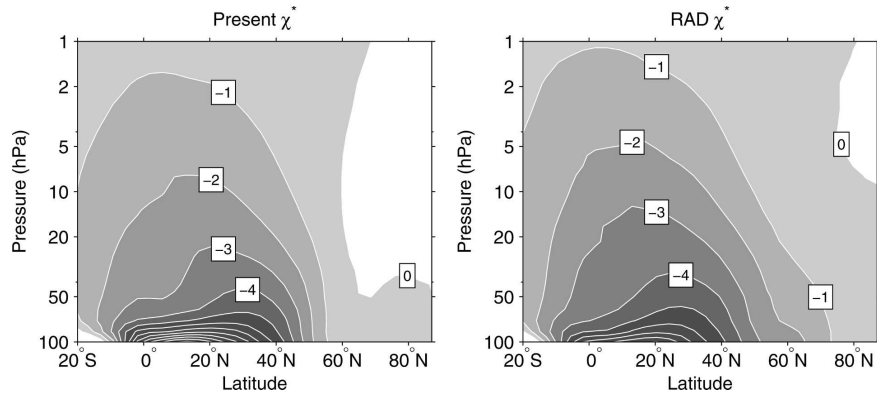
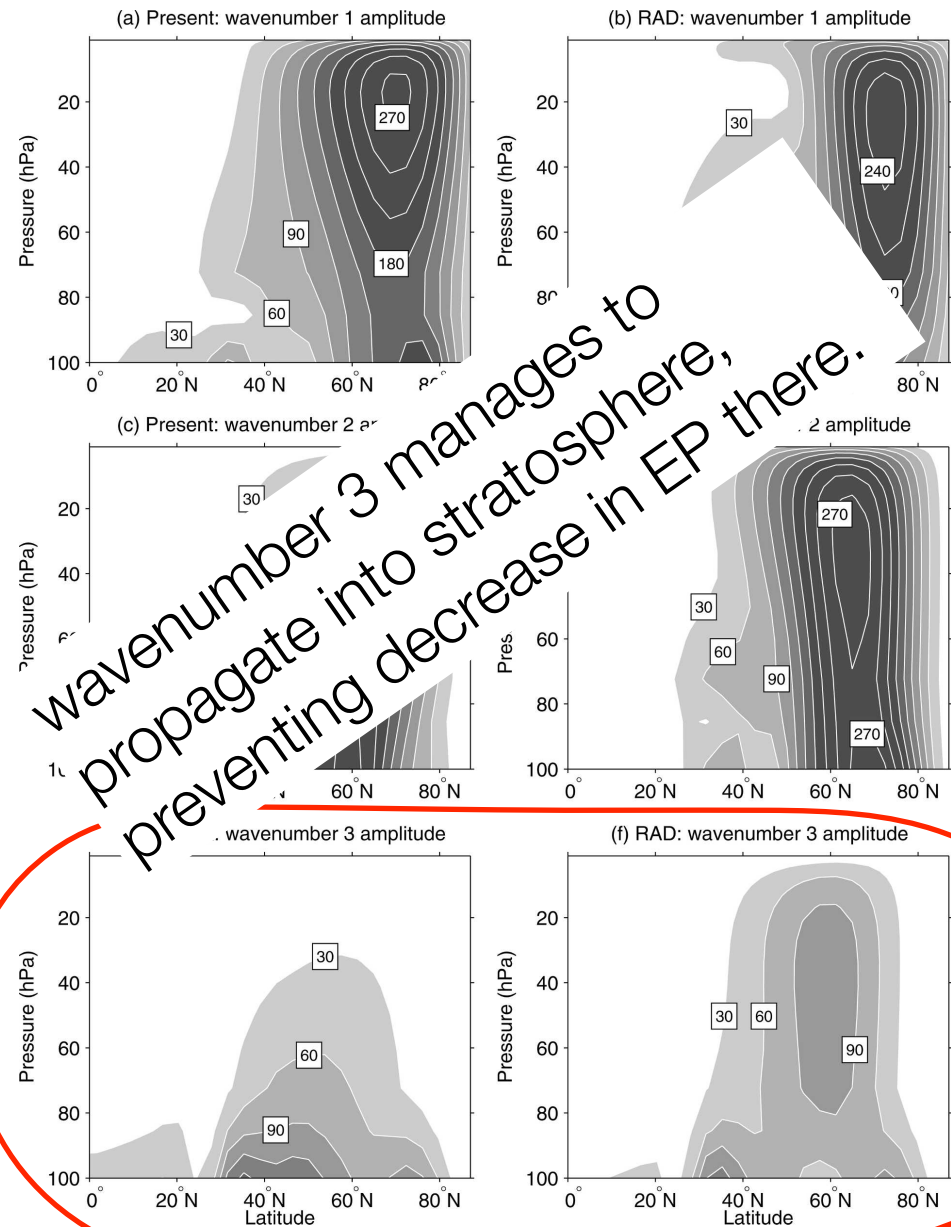


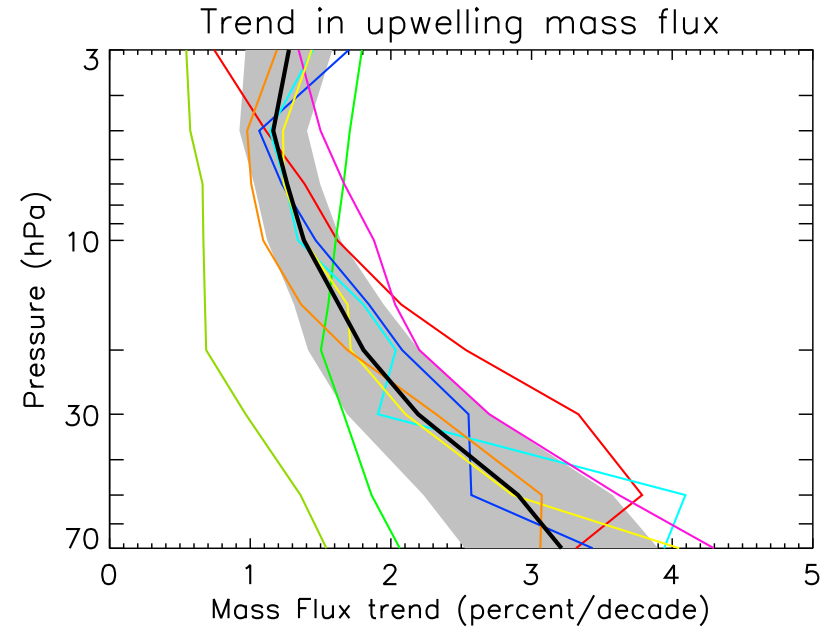
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Brewer-Dobson circ. projected to **strengthen** in a future warmer climate

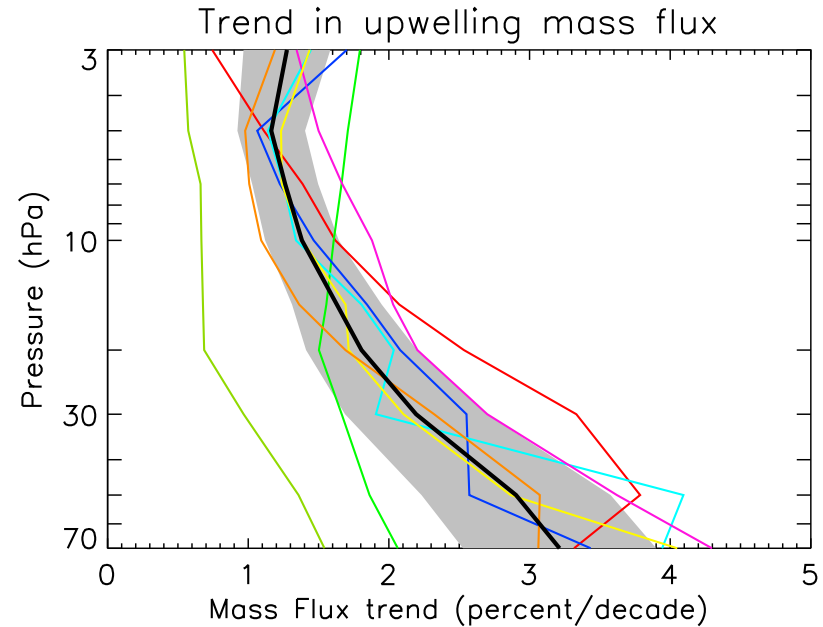
Figure 8. Projected trends in tropical upwelling in percent per decade based on a linear fit to the years 2006–2099 from RCP8.5 scenario simulations of eight stratosphere-resolving GCMs. The black line is the multi-model mean with the shading showing the inter-model standard error, scaled to represent a 95% confidence interval.



- Changes in the Brewer-Dobson circulation are mainly a response to the tropospheric warming, including the accompanying SST changes, and not the direct radiative effect of increasing GHG amounts cooling the stratosphere.

Brewer-Dobson circ. projected to **strengthen** in a future warmer climate

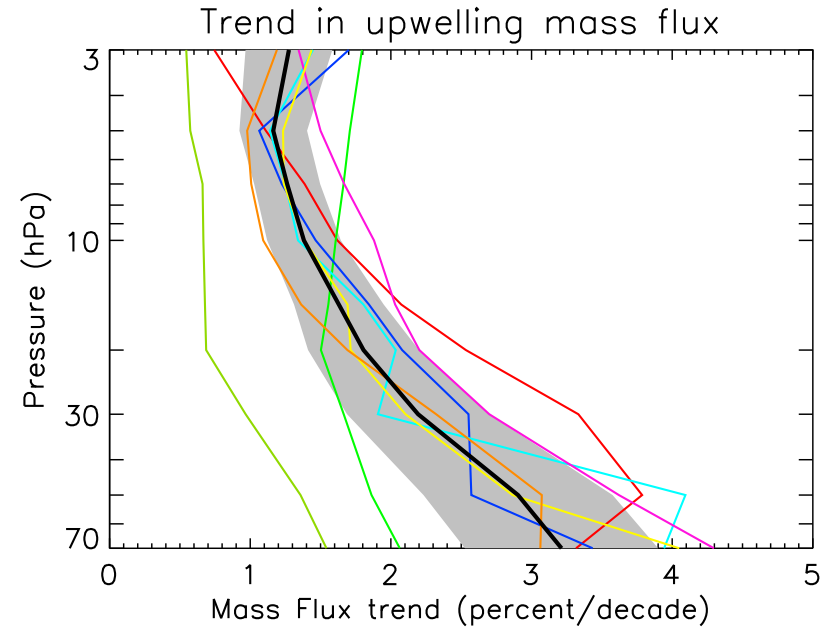
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1. Changes in the Brewer-Dobson circulation are mainly a response to the tropospheric warming, including the accompanying SST changes, and not the direct radiative effect of increasing GHG amounts cooling the stratosphere.
2. Both resolved & parameterized unresolved gravity waves drive a stronger BD circulation in RCP-type model projections.

Brewer-Dobson circ. projected to **strengthen** in a future warmer climate

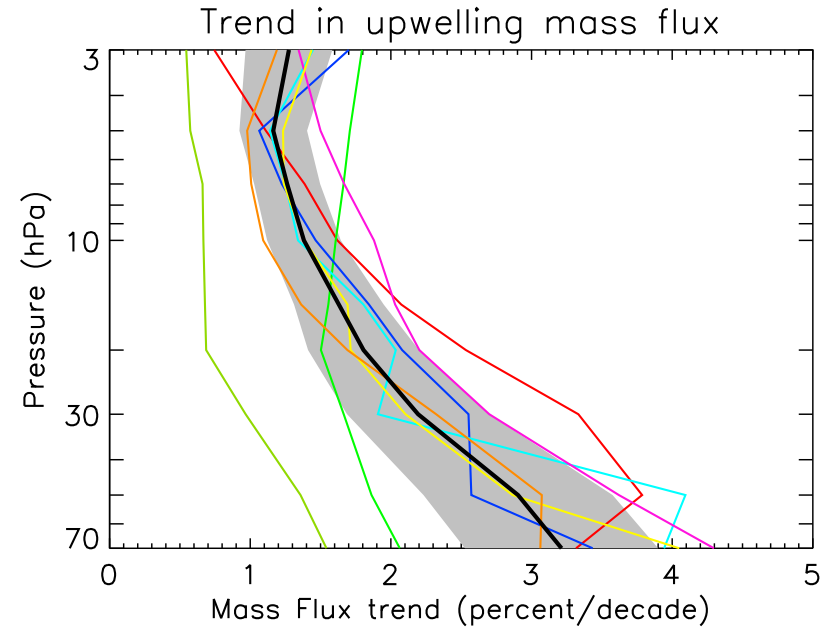
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3. Currently, there is no consensus on the mechanism of the increase in stratospheric wave drag from resolved planetary & synoptic-scale Rossby waves.

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3. Currently, there is no consensus on the mechanism of the increase in stratospheric wave drag from resolved planetary & synoptic-scale Rossby waves.
4. The mechanism may be related to a shift in critical layer where wave breaking occurs, due to eastward acceleration & upward movement of the subtropical jets

Summary of obstacles for Polar Stratospheric Clouds dynamical feedback idea

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- EP flux into the stratosphere may not decrease even for very weak meridional surface temperature gradient, although synoptic-scale wave forcing is weaker

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- Also: future warm climate projections show a strengthening of the Brewer-Dobson circulation.

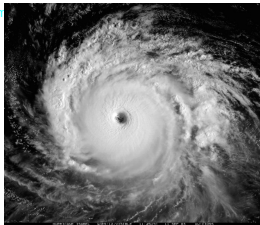
Summary of obstacles for Polar Stratospheric Clouds dynamical feedback idea

- EP flux into the stratosphere may not decrease even for very weak meridional surface temperature gradient, although synoptic-scale wave forcing is weaker
- The reason is that wavenumber #3 may be able to propagate vertically
- ➔ B-D circulation would then not weaken.
- Also: future warm climate projections show a strengthening of the Brewer-Dobson circulation.
- ➔ Dynamical feedback that was proposed to cool the Arctic polar stratosphere and allow PSCs to develop is running into difficulties.

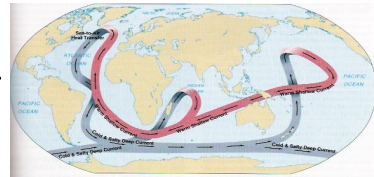
Stronger hurricanes

www.nasa.gov/images/content/65932n

(3)



stronger AMOC



Warmer high latitudes

(K. Emanuel, 2002)

Hurricanes and ocean mixing

The proposed feedback:

warmer climate, stronger Hurricanes

- ➔ stronger internal waves forced at the ocean surface
- ➔ propagate into deep ocean interior and break
- ➔ stronger deep ocean diapycnal mixing
- ➔ Stronger meridional overturning circulation
- ➔ Higher meridional heat flux into arctic
- ➔ Warmer Arctic, tropics warm less due to high CO₂

notes

Potential intensity:

Estimating hurricane strength from SST

Hurricanes and ocean mixing

Entropy reminder

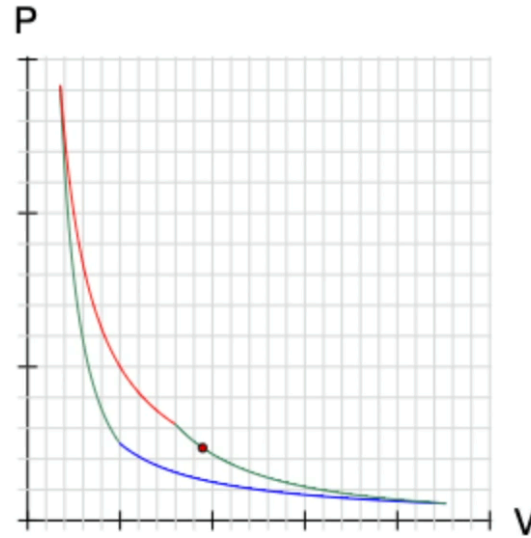
Consider a container with fluid, divided into two equal parts with temperatures $T_H > T_C$. Removing the divider, the temperature will eventually be homogenized to $(T_C + T_H)/2$. During the process, the infinitesimal change in entropy due to the transfer of an infinitesimal amount of heat $dQ > 0$ between the two systems leads to a gain dQ for the cold system and a loss of dQ for the hot system (gain of $-dQ$); thus the entropy change is

$$dS = \frac{dQ}{T_C} + \frac{-dQ}{T_H} = dQ \frac{T_H - T_C}{T_H T_C} > 0,$$

so the increase in entropy is because heat flows from the hot reservoir to the cold one.

Hurricanes and ocean mixing

notes: Carnot engine



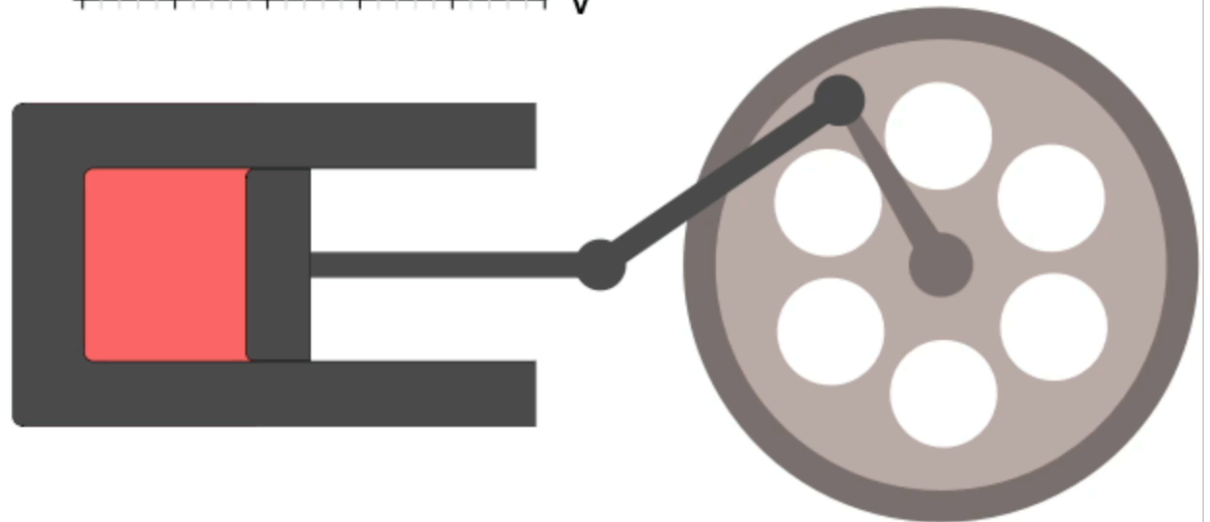
Isothermal Expansion

Adiabatic Expansion

Isothermal Compression

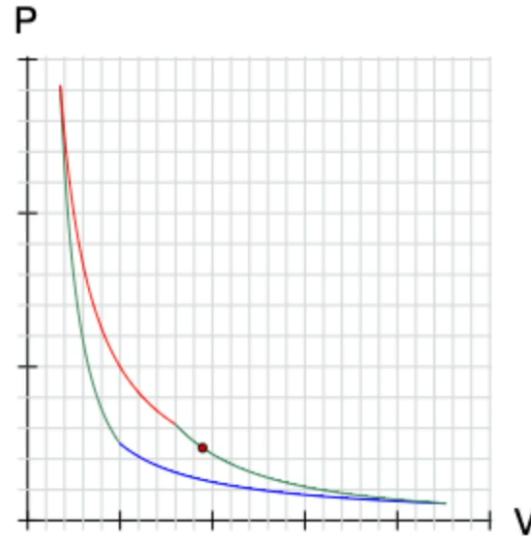
Adiabatic Compression

No heat exchange



Hurricanes and ocean mixing

notes: Carnot engine



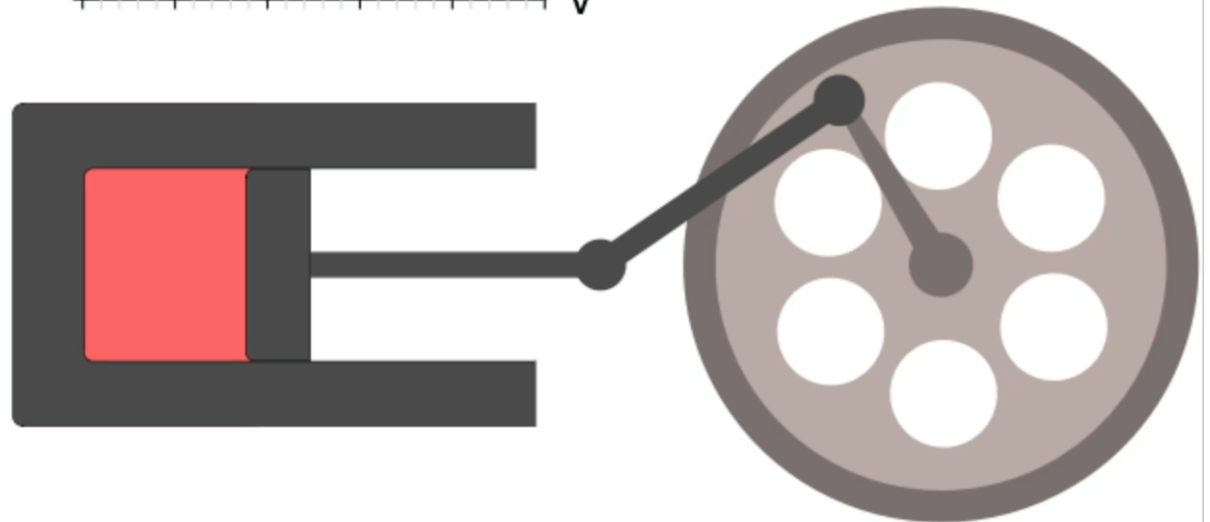
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Hurricanes and ocean mixing

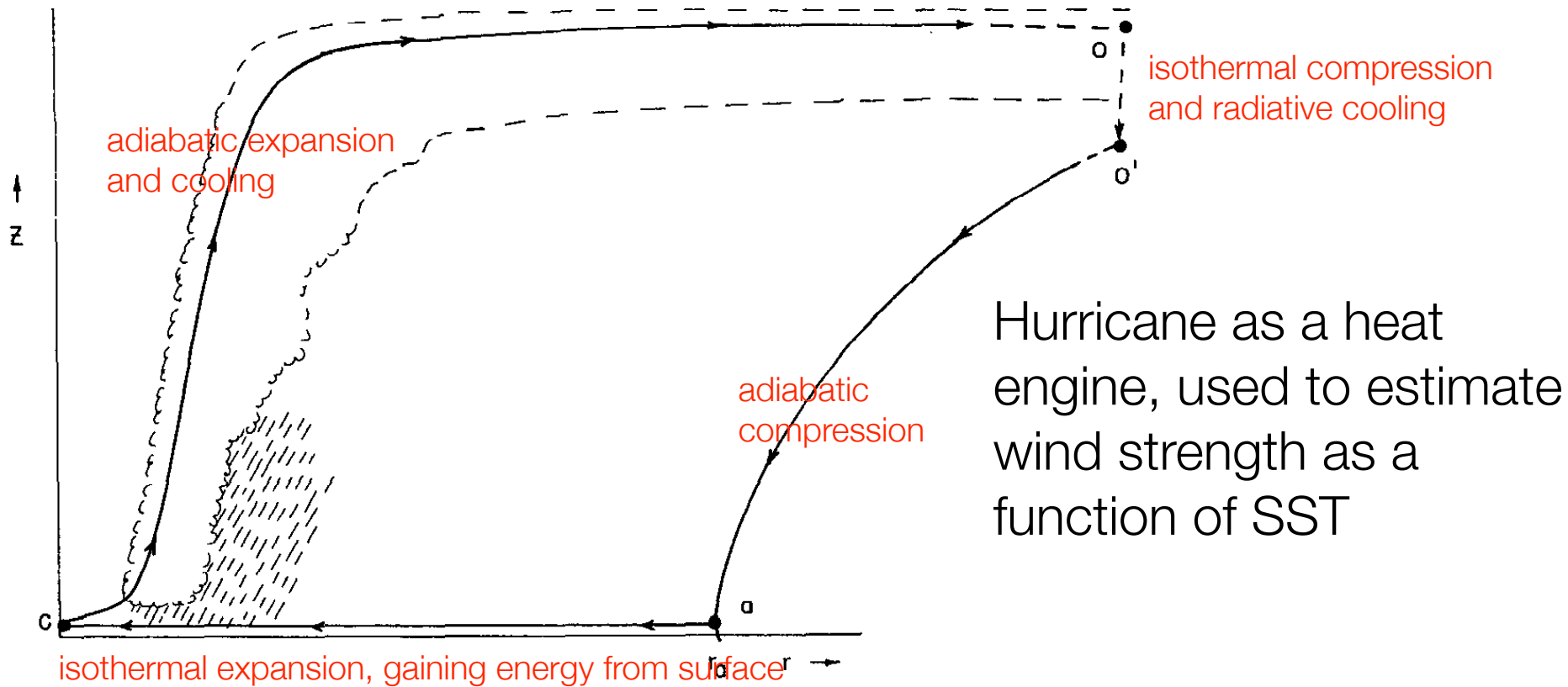


Figure 1 The hurricane Carnot cycle. Air begins spiraling in toward the storm center at point a , acquiring entropy from the ocean surface at fixed temperature T . It then ascends adiabatically from point c , flowing out near the storm top to some large radius, denoted symbolically by point o . The excess entropy is lost by export or by electromagnetic to space between o and o' at a much lower temperature T_o . The cycle is closed by integrating along an absolute vortex line between o' and a . The curves $c-o$ and $o'-a$ also represent surfaces of constant absolute angular momentum about the storm's axis.

Efficiency of a Carnot cycle

The first law of thermodynamics, energy conservation $dU = dQ - dW$

dU : change in the internal energy

dQ : heat gain due to exchange of heat with an outside reservoir;

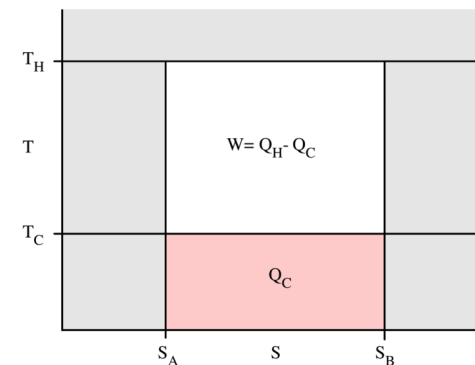
dW : is the work done by the system

Therefore:

$$W = \oint dW = \oint PdV = \oint (dQ - dU) = \oint TdS - \cancel{\oint dU} = (T_H - T_C)(S_B - S_A) \quad \text{for a Carnot engine}$$

Now, integrate $dQ = TdS$ to find that the total amount of thermal energy transferred between the hot reservoir and the engine is $Q_H = T_H(S_A - S_B)$, and with the cold reservoir $Q_C = T_C(S_A - S_B)$.

and the efficiency is $\eta = \frac{W}{Q_H} = \frac{T_H - T_C}{T_H}$.



Hurricanes and ocean mixing

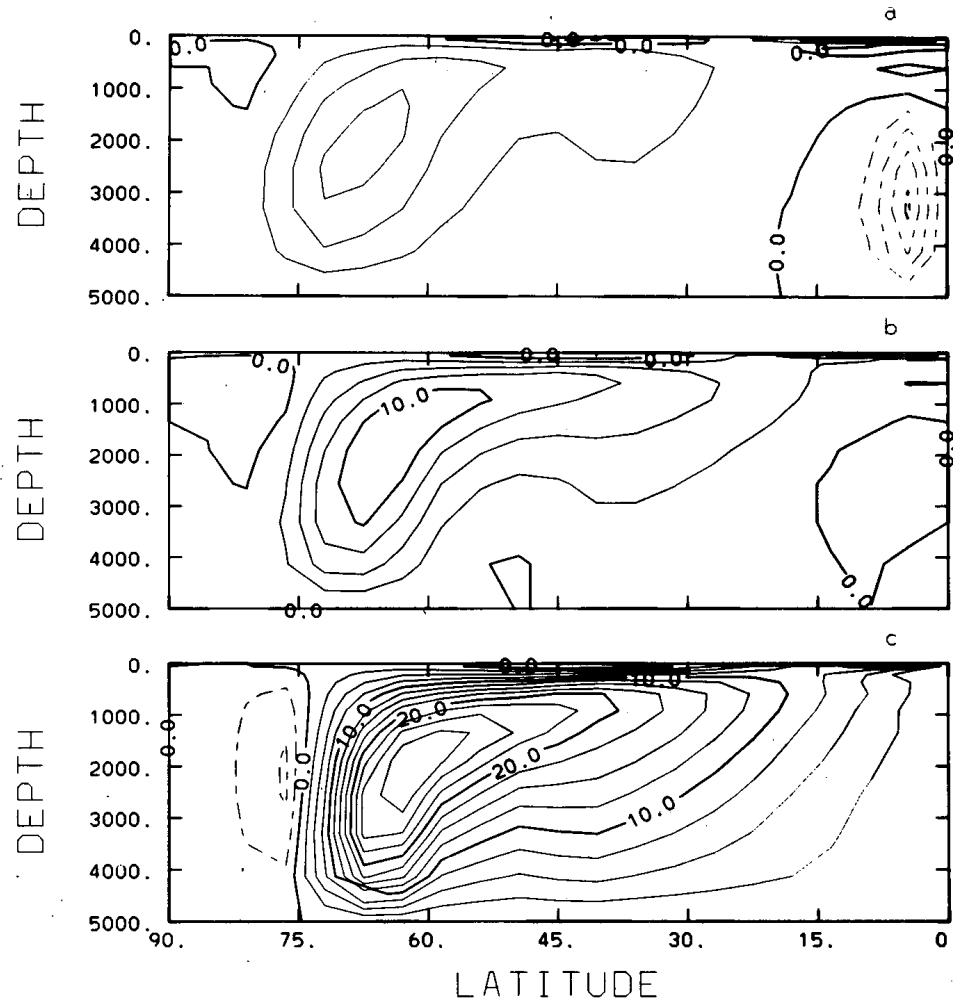


FIG. 7. Meridional overturning streamfunction for (a) $A_{HV} = 0.1$, (b) $A_{HV} = 0.5$, (c) $A_{HV} = 2.5$ (c.i. = $2.5 \times 10^6 \text{ m}^3 \text{ s}^{-1}$, solid contours indicate counterclockwise circulation).

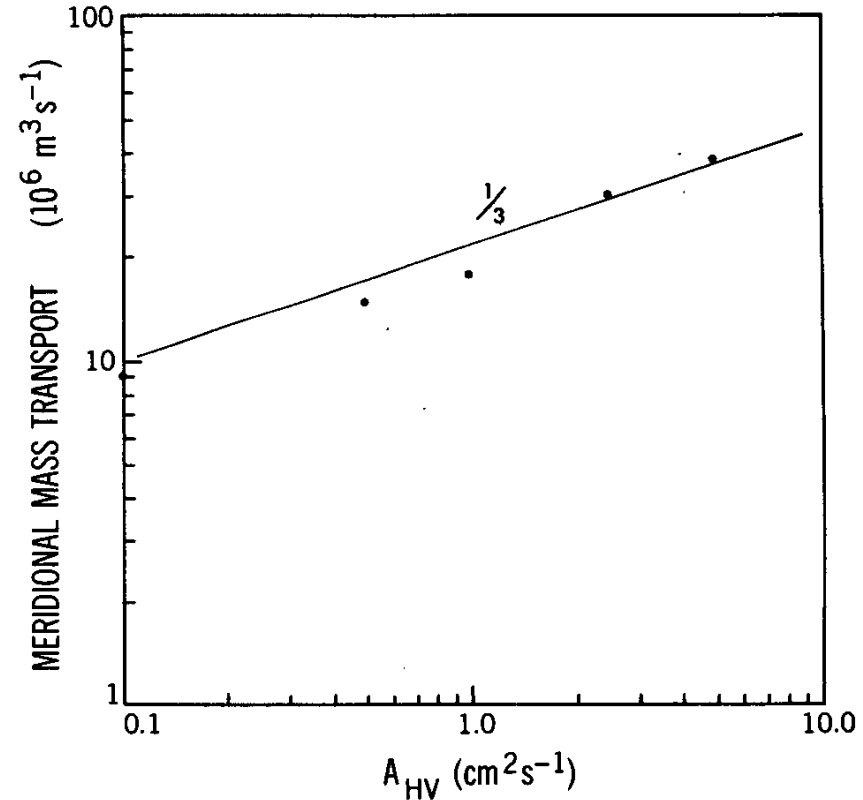


FIG. 8. Dependence of meridional overturning streamfunction on vertical diffusivity.

Frank Brian 1987

AMOC depends on vertical diapycnal mixing to the third power

Hurricanes and ocean mixing

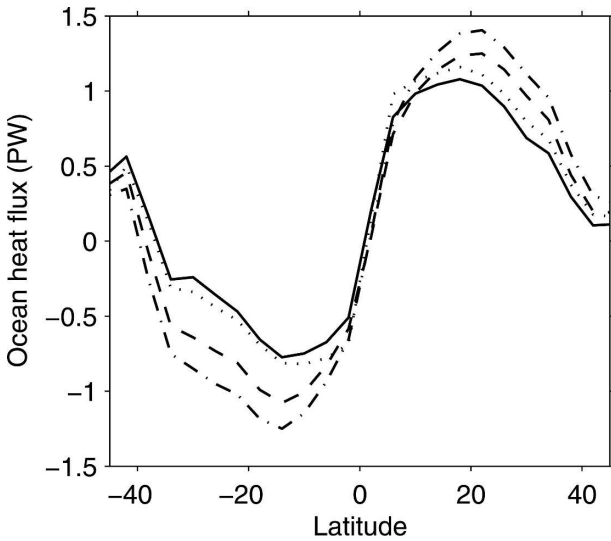


FIG. 2. Total ocean heat fluxes for simulations with uniformly weak mixing and 338 ppm CO_2 (dotted), uniformly weak mixing and 3380 ppm CO_2 (solid), elevated tropical mixing to 220 m and 3380 ppm CO_2 (dashed), and elevated tropical mixing to 360 m and 3380 ppm CO_2 (dashed-dotted).

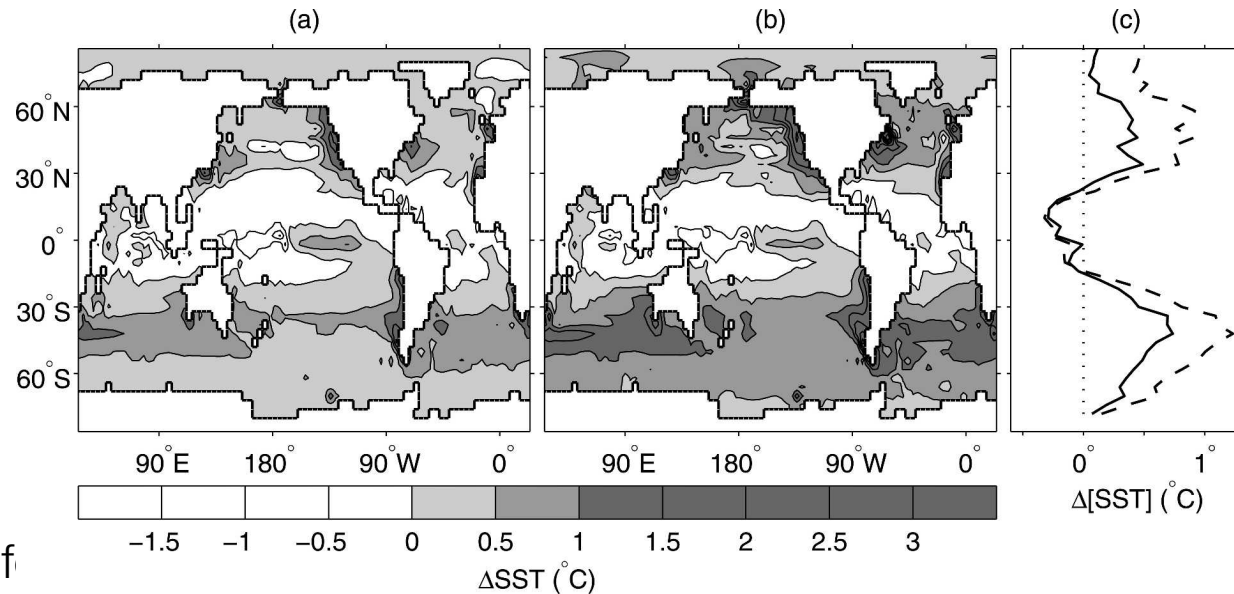


FIG. 4. Change in SSTs for runs with 3380 ppm CO_2 between (a) a simulation with elevated tropical mixing to 220 m and the control (uniformly weak mixing) and (b) a simulation with elevated tropical mixing to 360 m and the control. (c) Change in zonally averaged SST for the simulations shown in panels (a) (solid) and (b) (dashed).

Korty and Emanuel 2008

BUT: Enhanced vertical diapycnal mixing has a negligible effect on SST

Breakup of subtropical stratocumulus cloud decks at high SST

Causing albedo decrease and warming of mid-latitudes

Schneider et al 2019, (Bretherton et al)



(4)

<https://www.shutterstock.com/image-photo/aerial-view-layer-stratocumulus-clouds-369408491>

Breakdown of subtropical stratocumulus decks

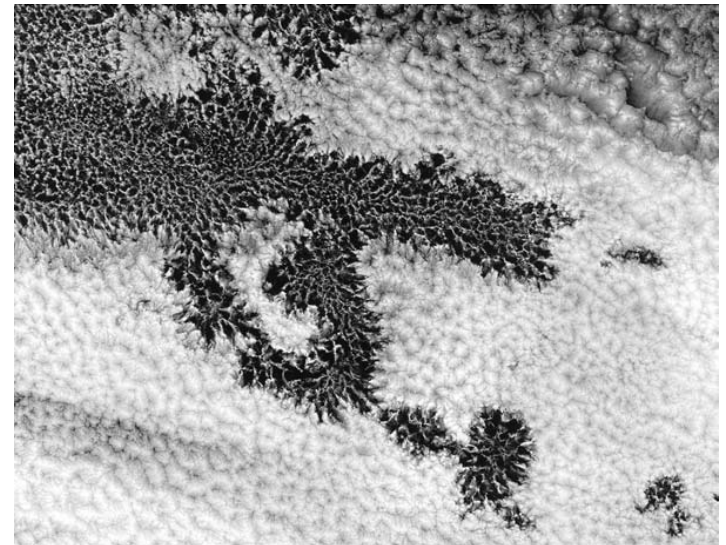
Stratocumulus clouds at present:

- Cover broad regions (6.5% of Earth area) over the subtropical oceans.
- Characterized by lines, waves, and cellular structures.
- Radiative cooling from the cloud tops drives convection to surface, that replenishes liquid water in these clouds.
- Can often be seen out of an airplane window while flying.
- **Large SW albedo, strong cooling effects on climate.**



Stratocumulus clouds from a plane

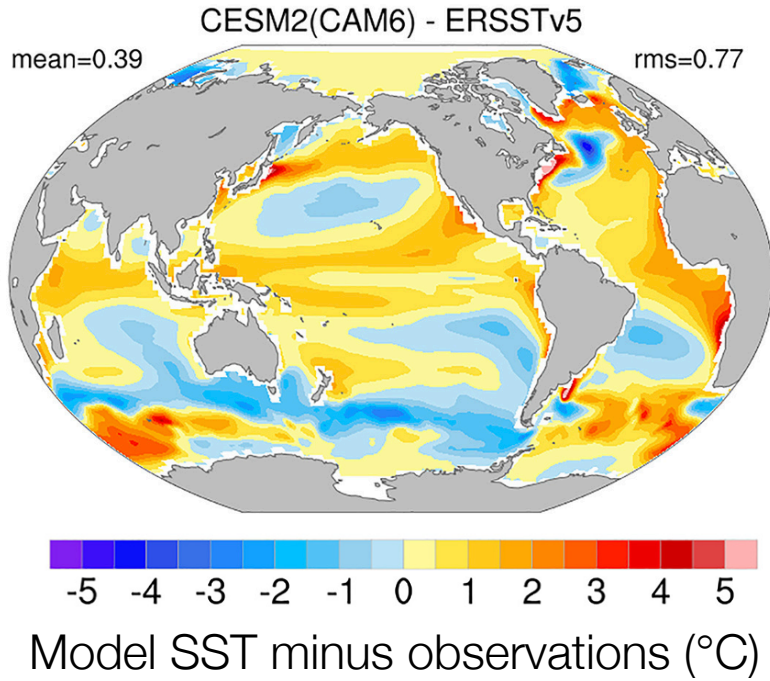
http://www.pilotfriend.com/training/flight_training/met/clouds.htm



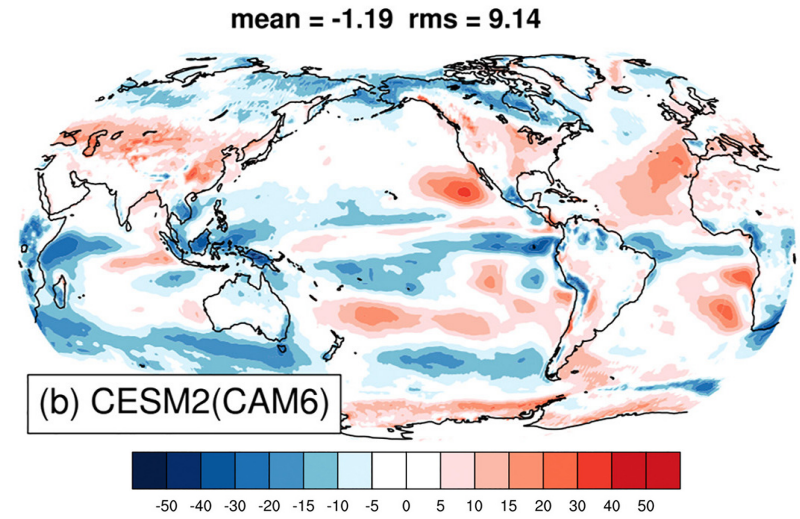
Cellular convective structures

<https://visibleearth.nasa.gov/images/98570/clouds-in-eastern-south-pacific-ocean?size=small>

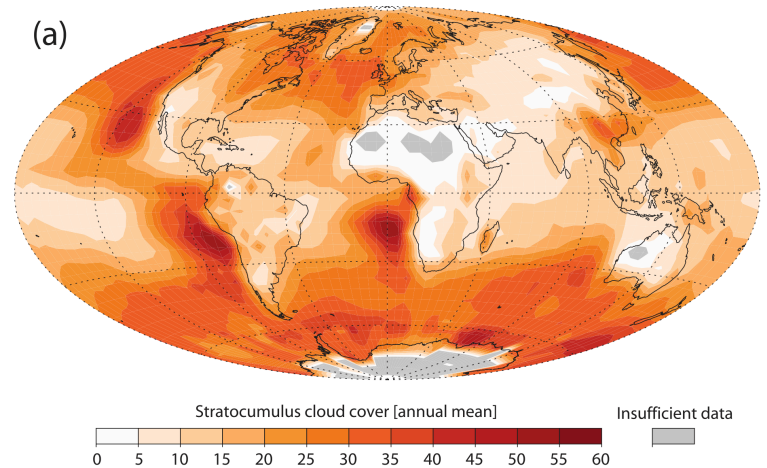
Stratocumulus cloud model bias leads to significant SST errors



G. Danabasoglu et al 2020,
<https://agupubs.onlinelibrary.wiley.com/doi/10.1029/2019MS001916>



shortwave CRF: model Wm^{-2} minus observations



observed stratocumulus cloud fraction (%)

SST error (difference between model and observations) is large, $\sim 2.5C$ in regions with underestimated stratocumulus cloud cover

Stratocumulus clouds: mechanism

Driving mechanism:

- Upward LW cooling at top of cloud layer because cloud layer is optically thick
- Cooling drives convective motions from surface to cloud layer
- Convection transports moisture to cloud layer and sustains it
- Convective motions also lead to uniform vertical distribution of moisture, forming a mix-layer

Opposing processes:

- Entrainment with dry air from cap-inversion layer
- Warming by downward LW radiation from the free troposphere toward top of cloud layer

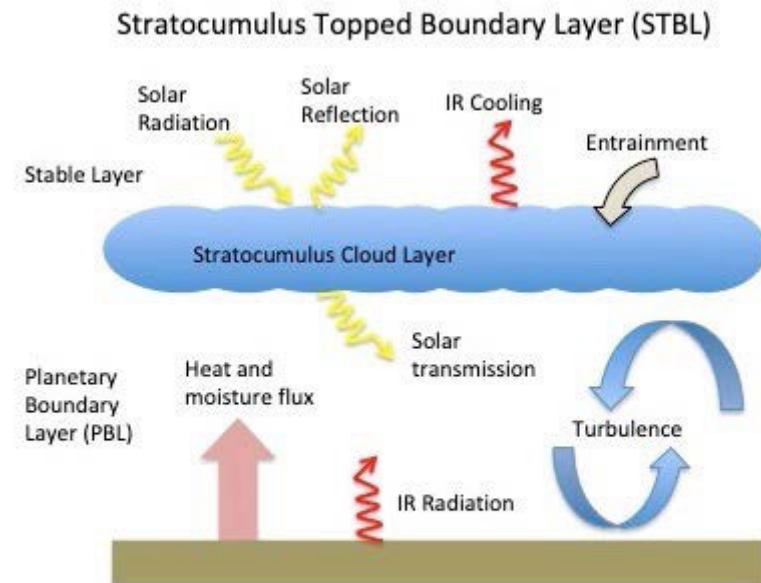
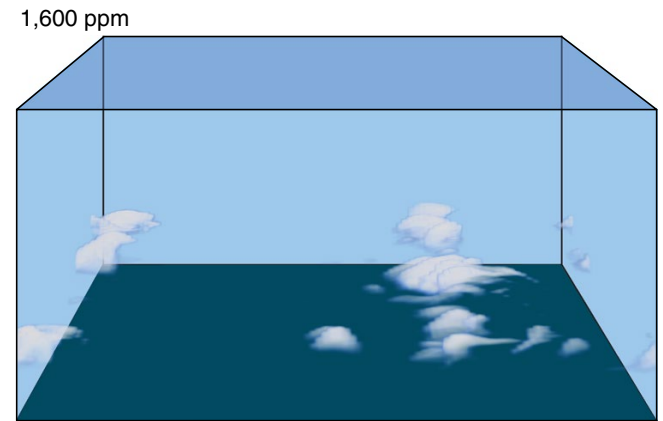
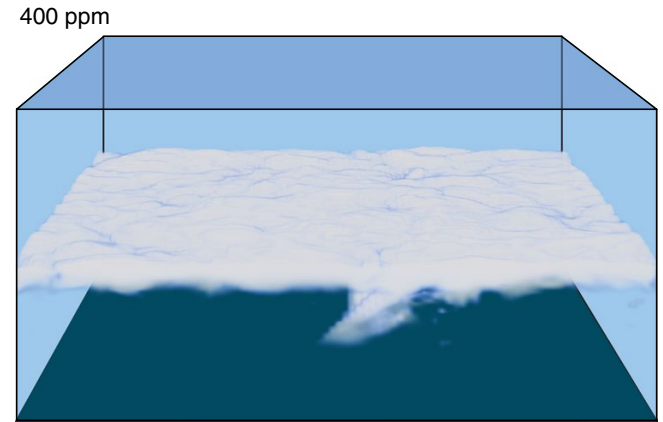


Fig. 3 Schematic diagram showing important dynamic and radiative features of the stratocumulus-topped boundary layer (STBL.) Adapted from Wood 2012

<https://www.amsweatherband.org/weatherband/articles/a-day-in-the-life-of-stratocumulus/>

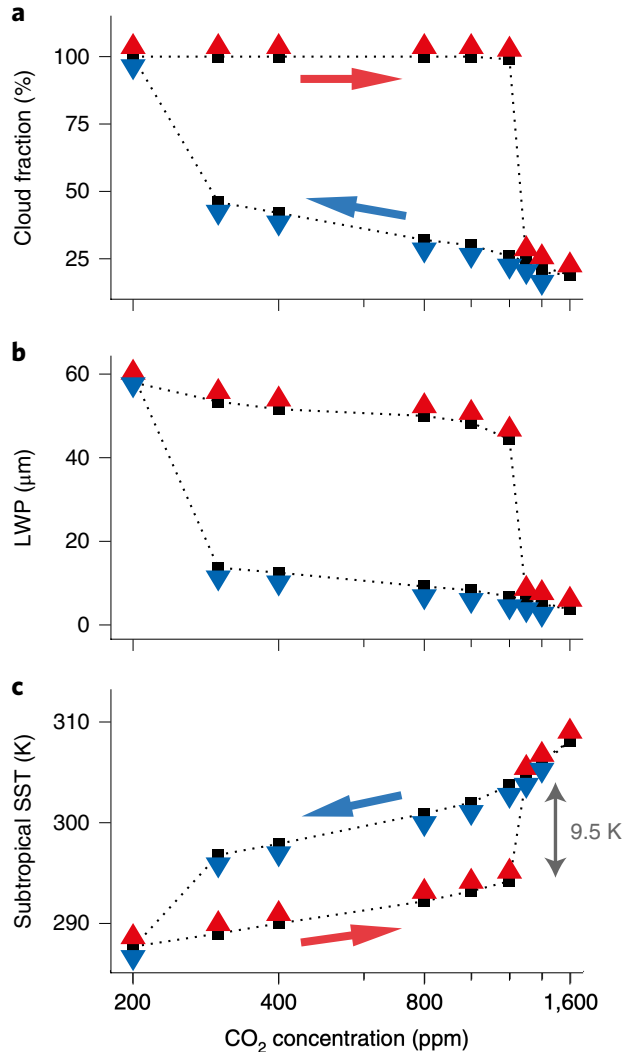
Breakdown of subtropical stratocumulus decks

Cloud
resolving
simulation:
stratocumulus
decks break
at high CO₂

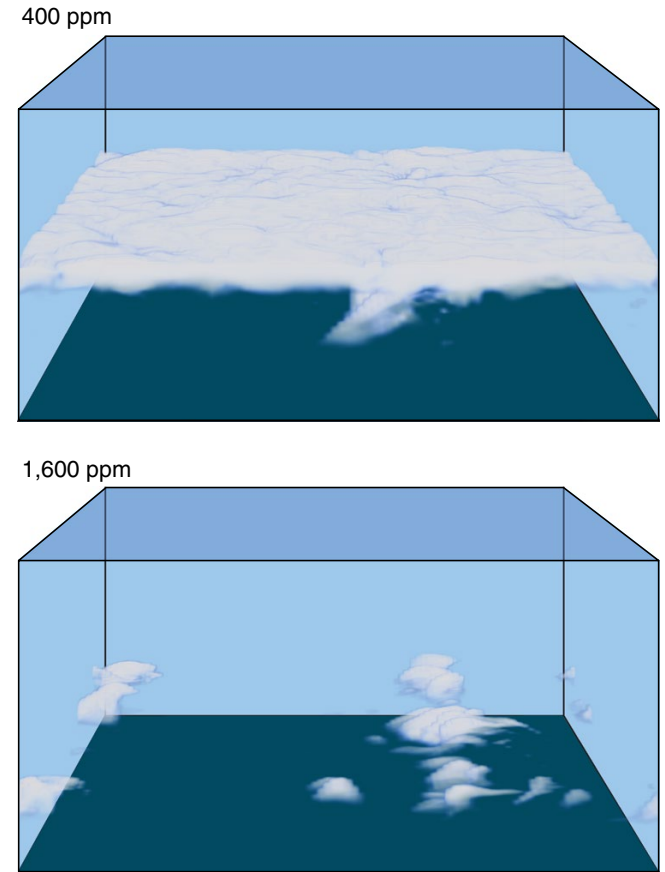


Possible climate transitions from breakup of stratocumulus decks under greenhouse warming

Breakdown of subtropical stratocumulus decks



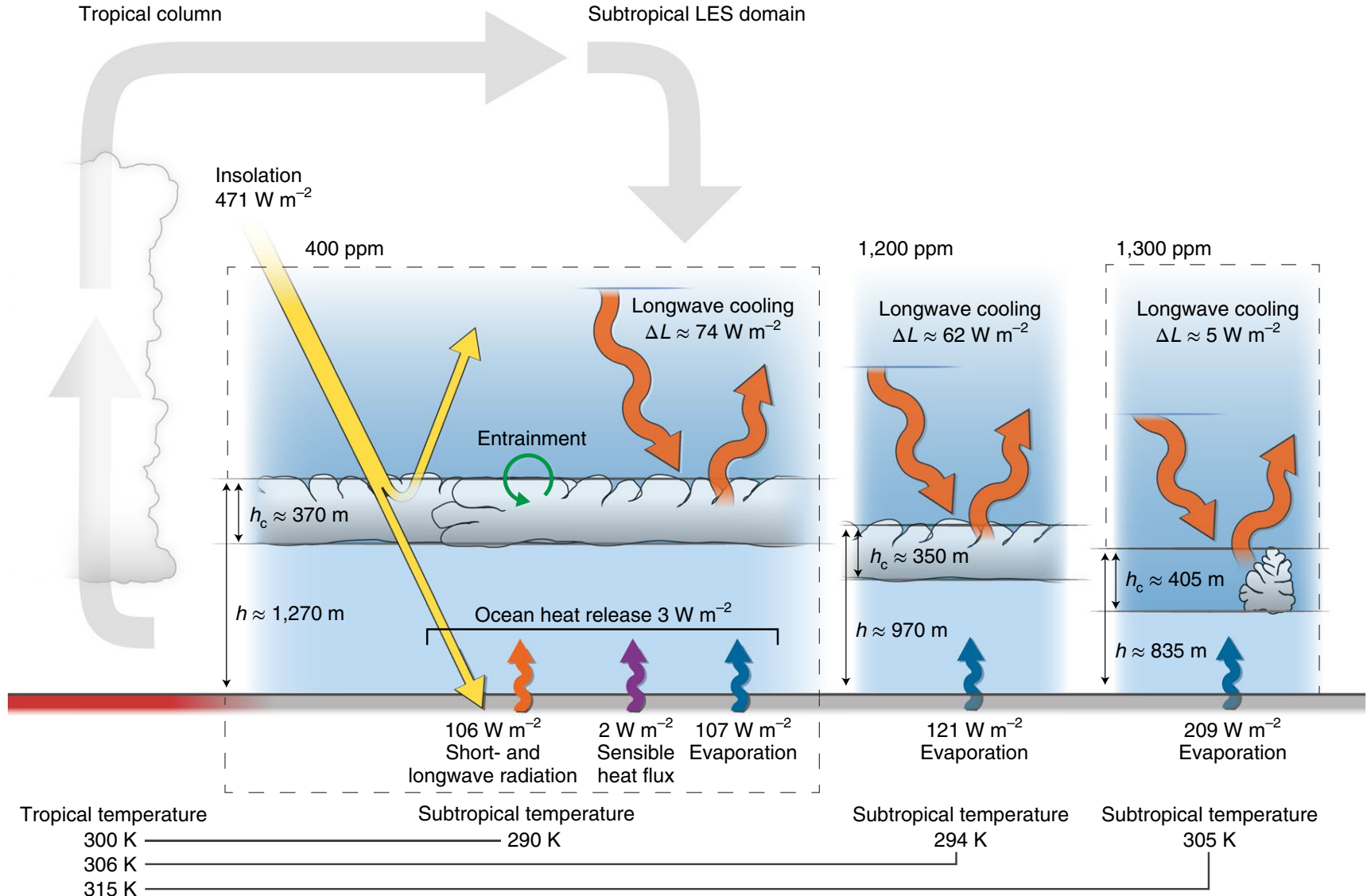
Cloud resolving simulation: stratocumulus decks break at high CO₂



Hysteresis as a function of CO₂

Possible climate transitions from breakup of stratocumulus decks under greenhouse warming

Breakdown of subtropical stratocumulus decks

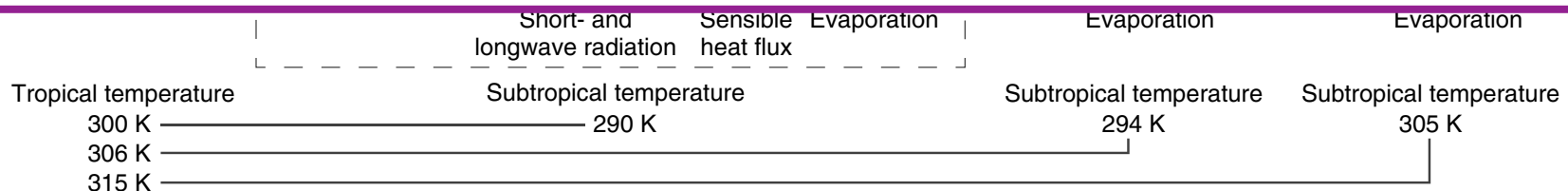


Breakdown of subtropical stratocumulus decks

Tropical column

Subtropical LES domain

Fig. 1 | Simulated subtropical clouds for 400 ppm CO₂, 1,200 ppm, and after breakup (1,300 ppm). In stratocumulus clouds, LW cooling of cloud tops propels air parcels downward, convectively coupling clouds to surface moisture source. Turbulence entrains warm & dry air across the inversion, counteracting radiative cooling & convective moistening of cloud layer. At high CO₂ (& H₂O) LW cooling of cloud tops weakens, bec downwelling LW arrives from lower levels/ higher temperatures ➔ decks break up into cumulus clouds, leading to dramatic albedo change & surface warming. Evaporation increases & LW cooling at cloud tops drops to < 10%.



Breakdown of subtropical stratocumulus decks

Mechanism of breakup at high CO₂:

Higher CO₂: ➡ downwelling LW toward cloud tops ↑ (increased atm emissivity ➡ ↑ LW coming from lower/warmer altitudes)

➡ decreased cloud top cooling ➡ decoupling from surface

➡ clouds dissipate

Breakdown of subtropical stratocumulus decks

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[paper mentions a 2nd mechanism: high T ➡ enhanced evaporation ➡ more turbulence at cloud level due to latent heat release ➡ more entrainment ➡ warming/drying & decoupling;

But: with clouds gone, is there still latent heat release?]

Breakdown of subtropical stratocumulus decks

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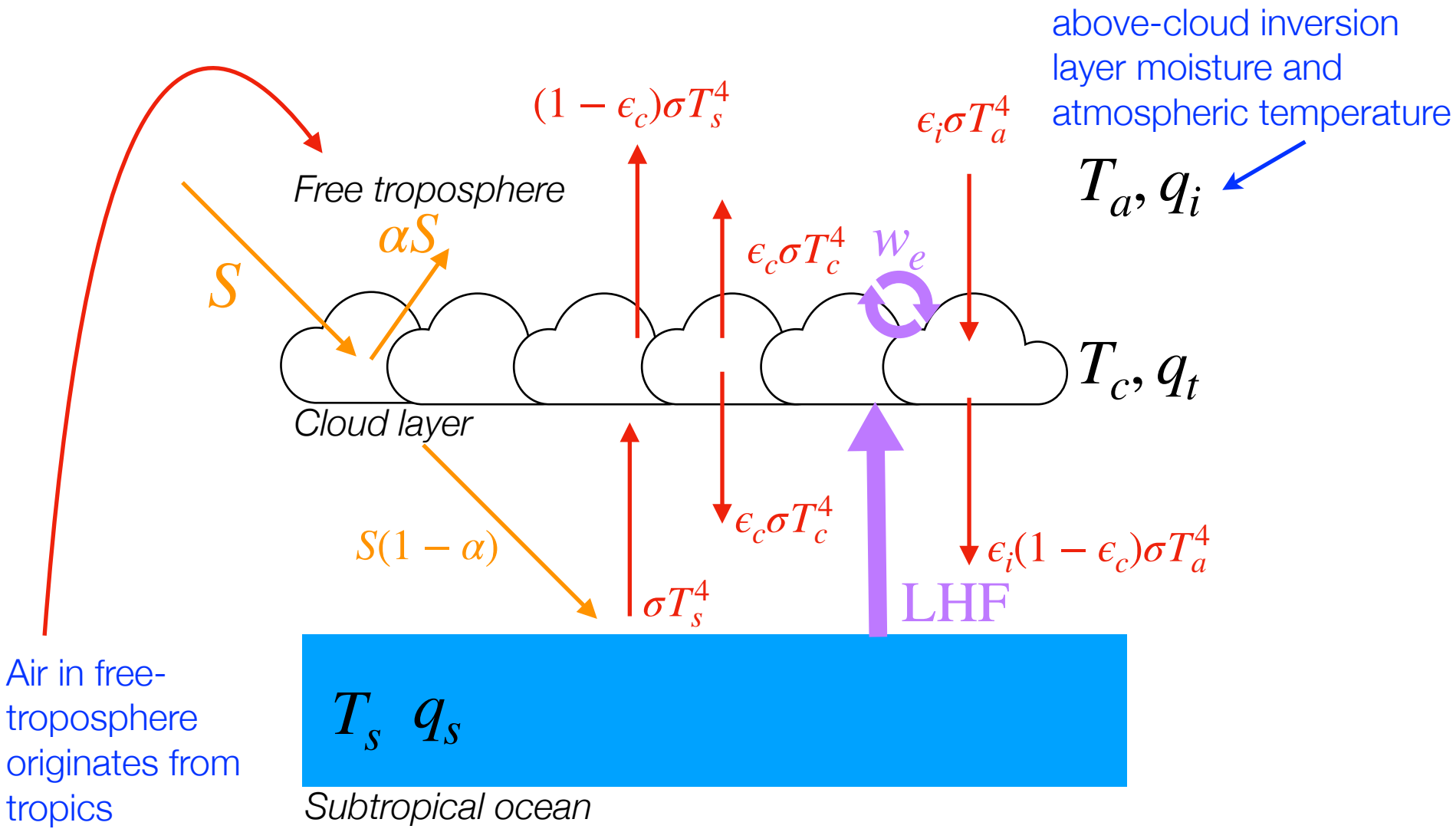
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But: with clouds gone, is there still latent heat release?]

Consequences of stratocumulus breakup:

Subtropical SST jumps by 10K. Subtropical marine stratocumulus clouds cover ~6.5% of Earth's surface & reduce absorbed SW by $\sim 110 \text{ W m}^{-2}$, compared to $\sim 10 \text{ W m}^{-2}$ by scattered cumulus. With climate sensitivity of $1.2 \text{ K (Wm}^{-2}\text{)}^{-1}$ (4.8 K/CO₂ doubling; high for current GCMs) implies $(110-10) \text{ Wm}^{-2} \times 6.5\% \times 1.2 \text{ K (Wm}^{-2}\text{)}^{-1} \approx 8 \text{ K}$ global-mean surface warming (stratocumulus clouds cover ~6.5% of Earth area). **This seems to assume an infinitely efficient heat transport to the rest of the globe.**

Two-box model for stratocumulus break-up



Two-box model for stratocumulus break-up

Temperature:

$$C_s \frac{dT_s}{dt} = S(1 - \alpha) - \sigma T_s^4 + \epsilon_c \sigma T_c^4 + \epsilon_i (1 - \epsilon_c) \sigma T_i^4 - \text{LHF} \quad \text{surface energy balance}$$

$$C_c \frac{dT_c}{dt} = \overbrace{-2\epsilon_c \sigma T_c^4 + \epsilon_c \sigma T_s^4 + \epsilon_i \epsilon_c \sigma T_a^4}^{\text{net longwave cooling} = LWC} + LQ + C_c w_e (T_a - T_c) \quad \text{cloud layer energy balance}$$

$$T_a = T_{a,0} + \Delta T \log_2(\text{CO}_2/280) \quad \text{free troposphere temperature}$$

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$$T_a = T_{a,0} + \Delta T \log_2(\text{CO}_2/280) \quad \text{free troposphere temperature}$$

Moisture:

$$E = C_E V (q_s - q_t), \quad \text{LHF} = L E \quad \text{Evaporation, surface latent heat flux}$$

$$q_t = q_l + q_c \quad \text{total moisture in cloud layer}$$

$$\frac{dq_t}{dt} = Q - w_e (q_t - q_i) \quad \text{cloud moisture budget}$$

$$q_c = \min[q_t, q^*(T_c)], \quad q_l = q_t - q_c$$

$$Q = \begin{cases} E \text{ coupled} \\ 0 \text{ decoupled} \end{cases} \quad \text{moisture flux into cloud layer}$$

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Decoupling criteria: $LHF/LWC > 1$

Two-box model for stratocumulus break-up

Temperature:

$$C_s \frac{dT_s}{dt} = S(1 - \alpha) - \sigma T_s^4 + \epsilon_c \sigma T_c^4 + \epsilon_i (1 - \epsilon_c) \sigma T_i^4 - \text{LHF} \quad \text{surface energy balance}$$

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$$q_t = q_l + q_c \quad \text{total moisture in cloud layer}$$

Coefficients:

$$\alpha = \alpha_c - (\alpha_c - \alpha_w) \exp(-D\kappa q_l)$$

$$\epsilon_c = 1 - (1 - \epsilon_{c,o}) \exp(-D\kappa q_l)$$

$$\epsilon_i = \epsilon_{i,0} + A \log_2(\text{CO}_2/280)$$

$$+ B \log_2(q_i/q_{i,o})$$

$$C_s = H_s c_p^w \rho_w, \quad C_c = H_c c_p^a \rho_a$$

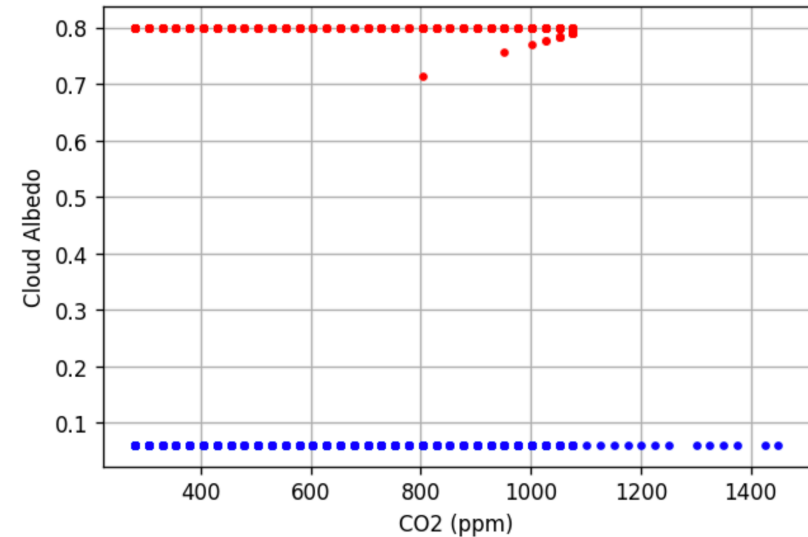
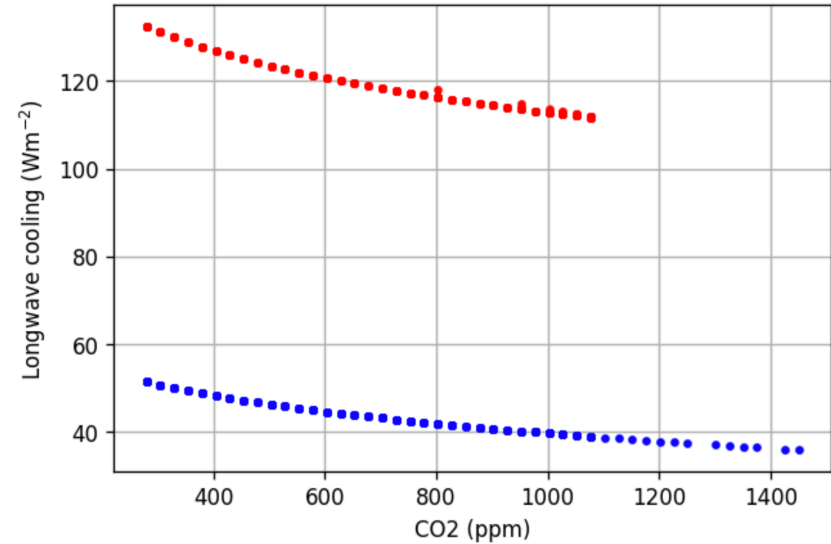
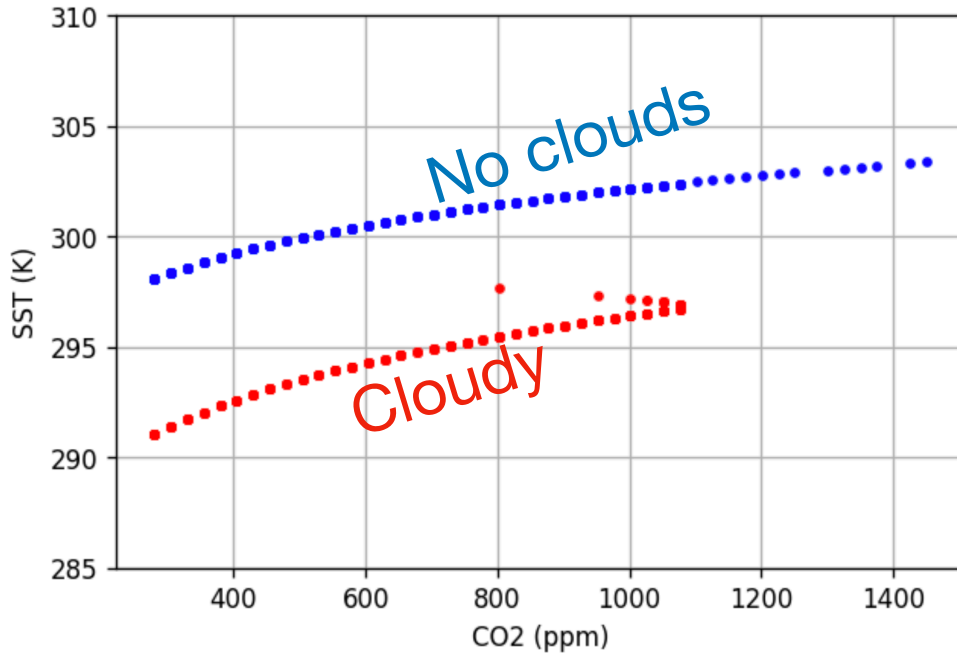
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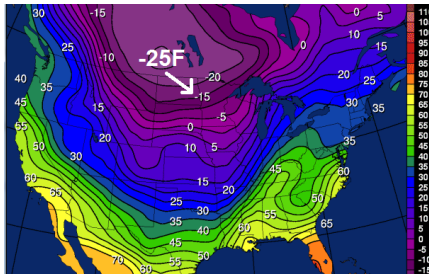
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Decoupling criteria: $LHF/LWC > 1$

Two-box model for stratocumulus break-up



➡ Hysteresis in CO₂, as in the cloud resolving model study of Schneider et al 2020.

(5)

Arctic air suppression over high latitude land

By low cloud forming due to moisture arriving from over warmer ocean

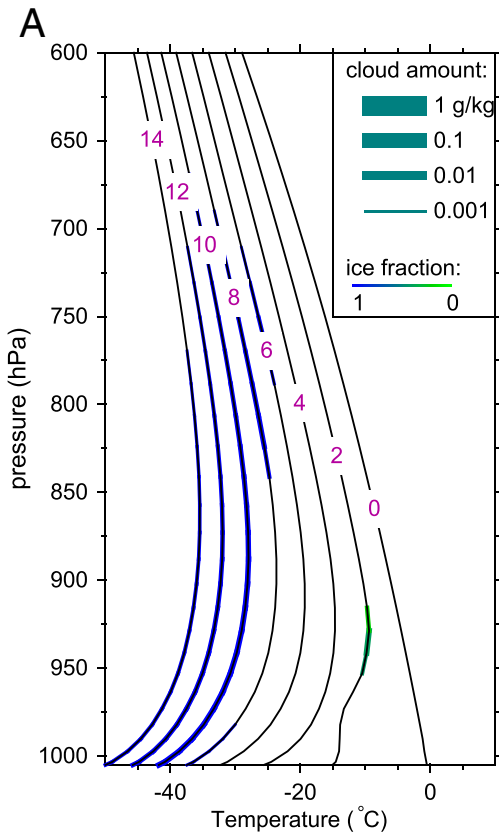
Cronin & Tziperman 2015

Arctic air suppression

Arctic air formation

Single-column model (WRF) simulation of polar air formation with initial 2-m air temperature $T_2(t=0) = 0^\circ \text{C}$. Simulating an air column going from ocean to over high-latitude land during winter, no solar forcing.

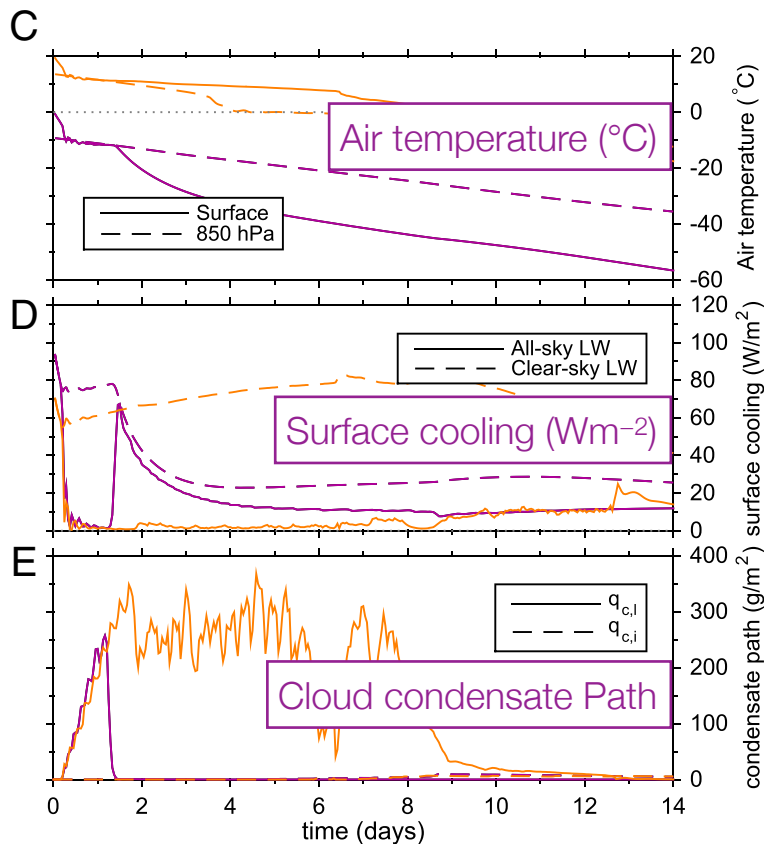
Results: surface temperature cools by about 60C in two weeks, strong inversion develops.



(following Judith Curry 1983)

Arctic air formation - mechanism

Arctic air formation for present-day initial conditions - mechanism



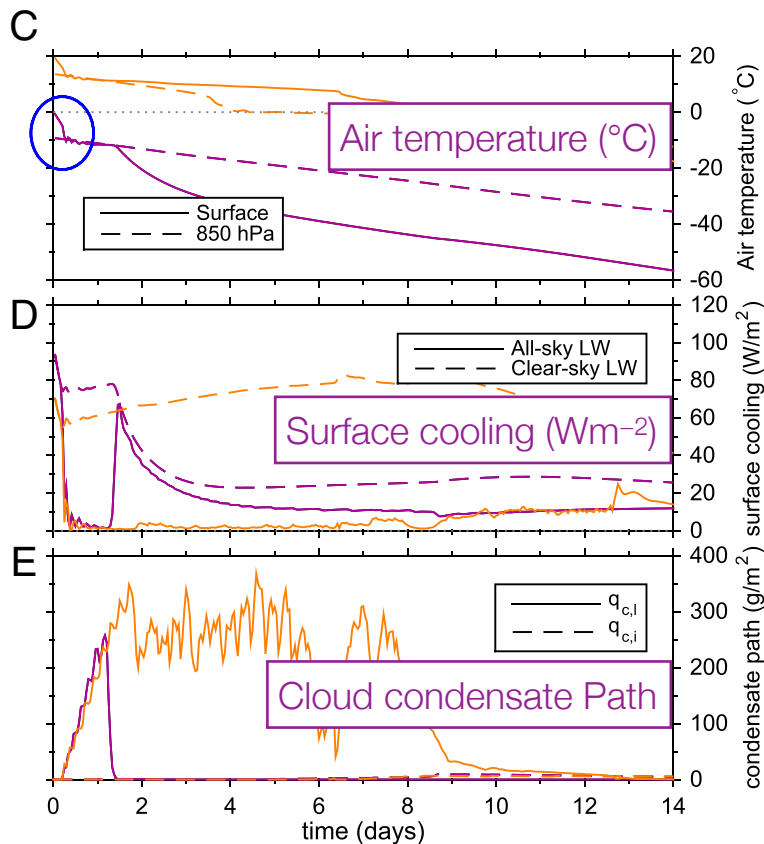
Single-column simulation of polar air formation with initial 2-m air temperature $T_2(t=0) = 0^\circ \text{C}$

Consider purple curves only:

(following Curry 1983)

Arctic air formation - mechanism

Arctic air formation for present-day initial conditions - mechanism



Single-column simulation of polar air formation with initial 2-m air temperature $T_2(t=0) = 0^\circ C$

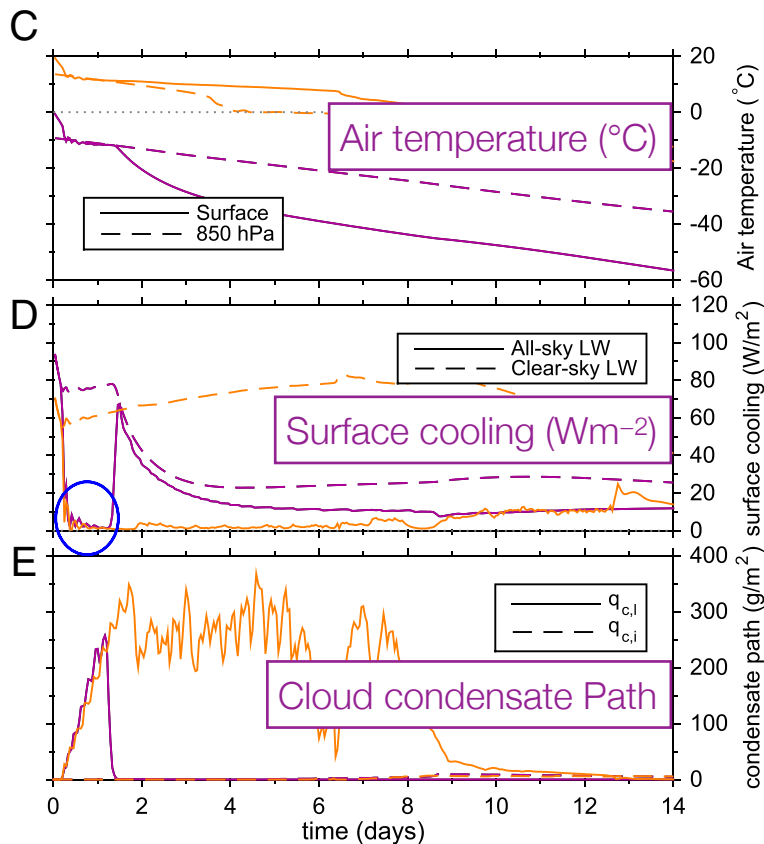
Consider purple curves only:

- Rapid initial cooling to $t=1/2$ day

(following Curry 1983)

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Arctic air formation for present-day initial conditions - mechanism



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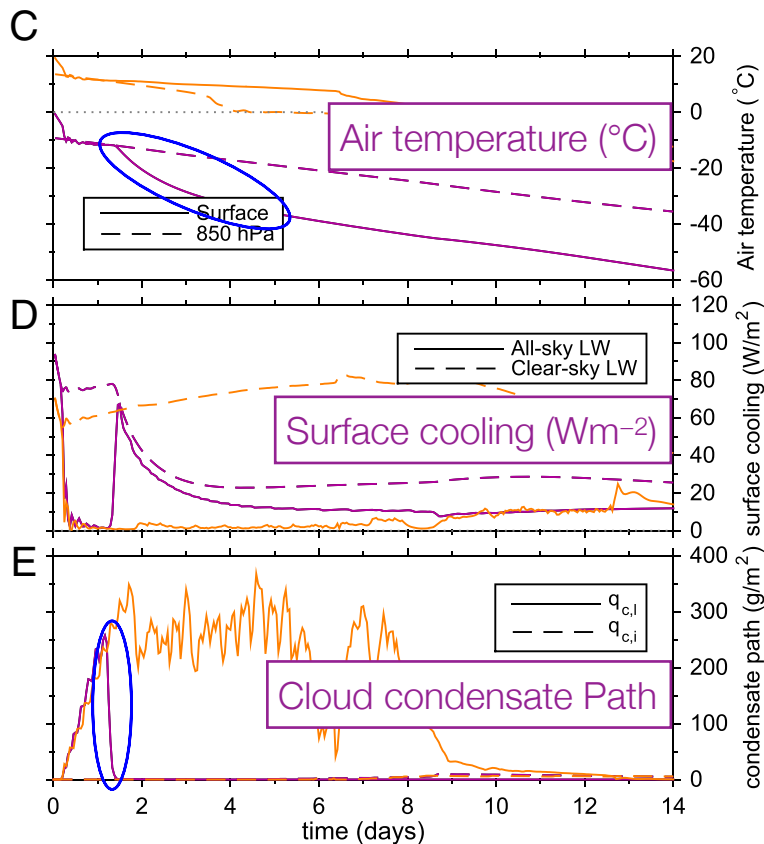
Consider purple curves only:

- Rapid initial cooling to $t=1/2$ day
- Low clouds form during day 1, slow surface cooling, allowing the mid-atmosphere to cool very rapidly

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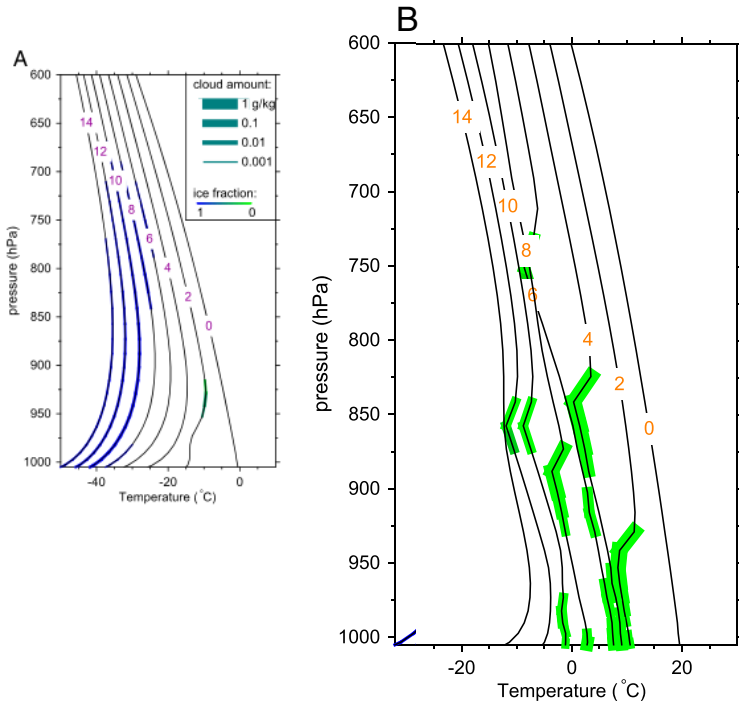
Consider purple curves only:

- Rapid initial cooling to $t=1/2$ day
- Low clouds form during day 1, slow surface cooling, allowing the mid-atmosphere to cool very rapidly
- Clouds dissipate within 1.5 days, surface cooling accelerates in the absence of LW from the mid-atmosphere.

(following Curry 1983)

Arctic air suppression

Suppression of Arctic air formation for warmer initial conditions (warmer ocean)

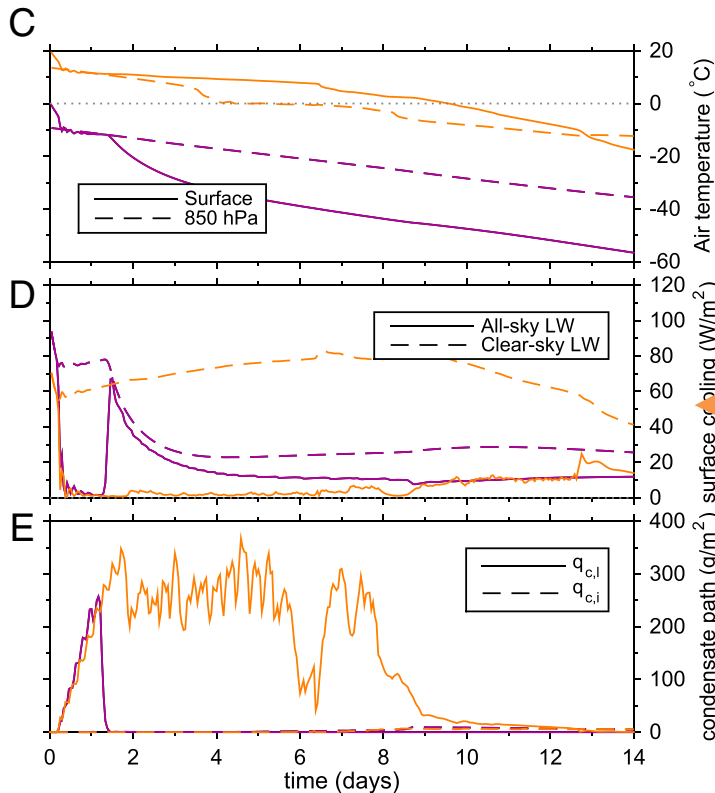


Single-column simulation of polar air formation with initial 2m air temperature $T_2(t=0) = 20^\circ \text{C}$ instead of 0°C

Day-1 cooling similar to cold initial conditions, but further surface cooling suppressed by LW effects of a liquid low cloud cloud layer!

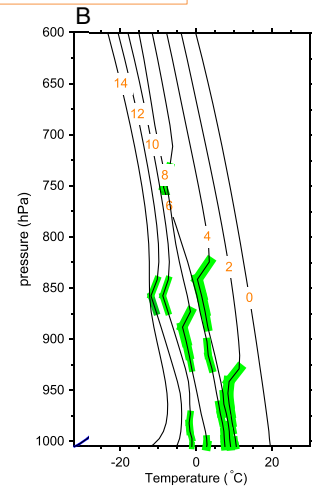
Arctic air suppression

Suppression of Arctic air formation for warmer initial conditions - mechanism



Single-column simulation of polar air formation w/initial 2-m air temperature $T_2(t=0) = 20^\circ \text{C}$

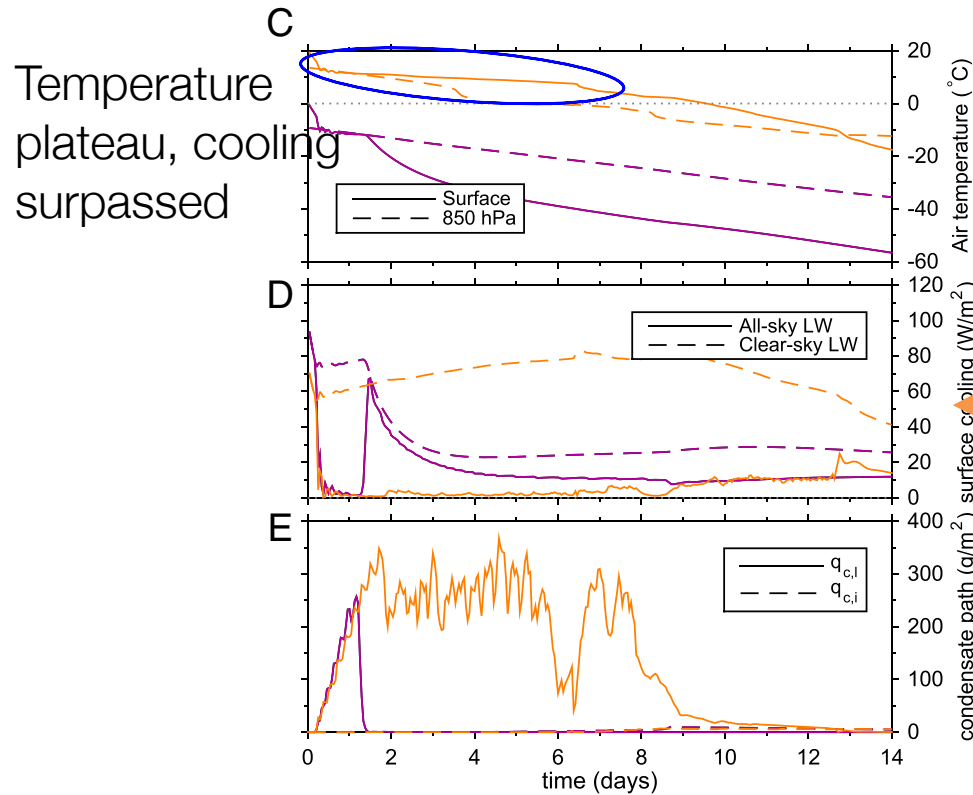
Consider orange curves



Day-1 cooling similar to cold initial conditions, but further surface cooling suppressed by LW effects of a liquid low cloud cloud layer!

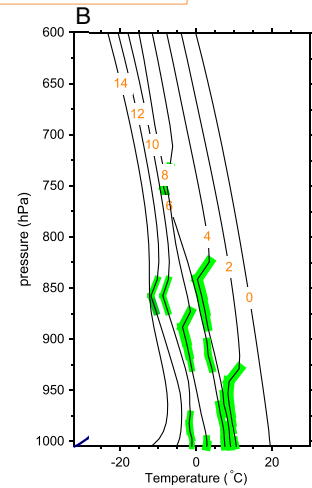
Arctic air suppression

Suppression of Arctic air formation for warmer initial conditions - mechanism



Single-column simulation of polar air formation w/initial 2-m air temperature $T_2(t=0) = 20^\circ \text{C}$

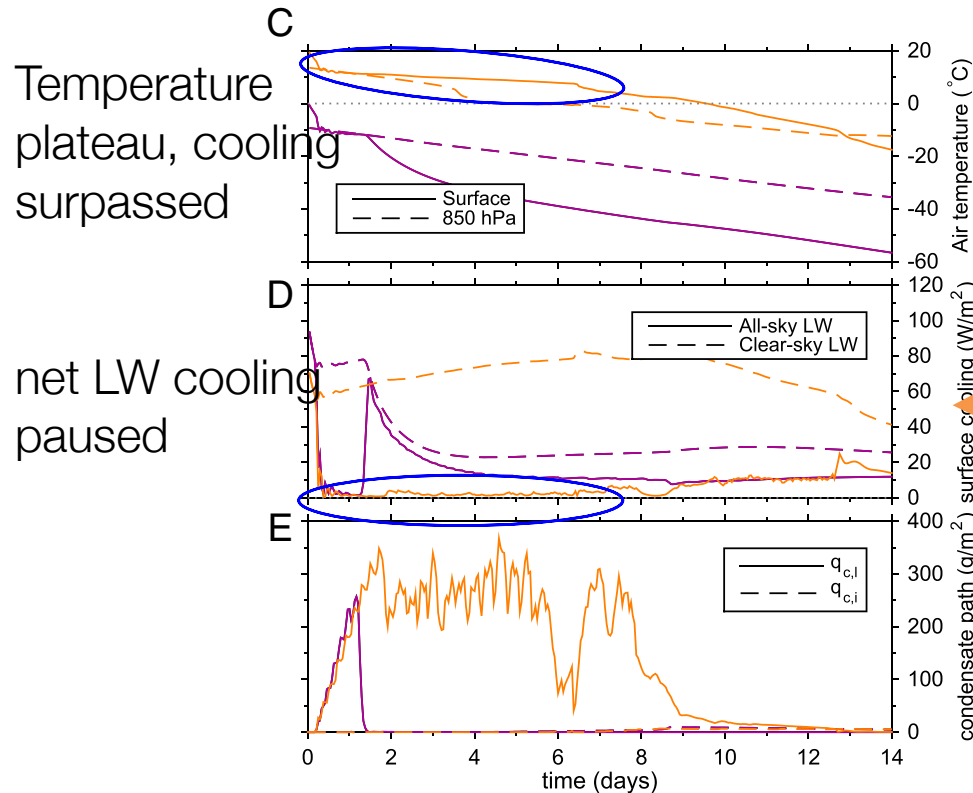
Consider orange curves



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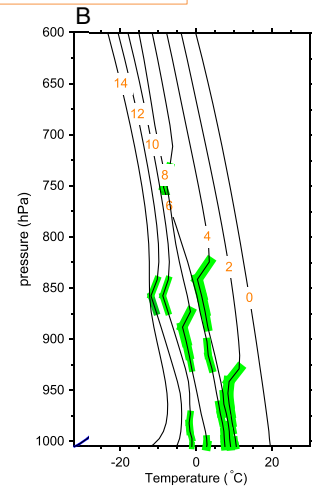
Arctic air suppression

Suppression of Arctic air formation for warmer initial conditions - mechanism



Single-column simulation of polar air formation w/initial 2-m air temperature $T_2(t=0) = 20^{\circ}\text{C}$

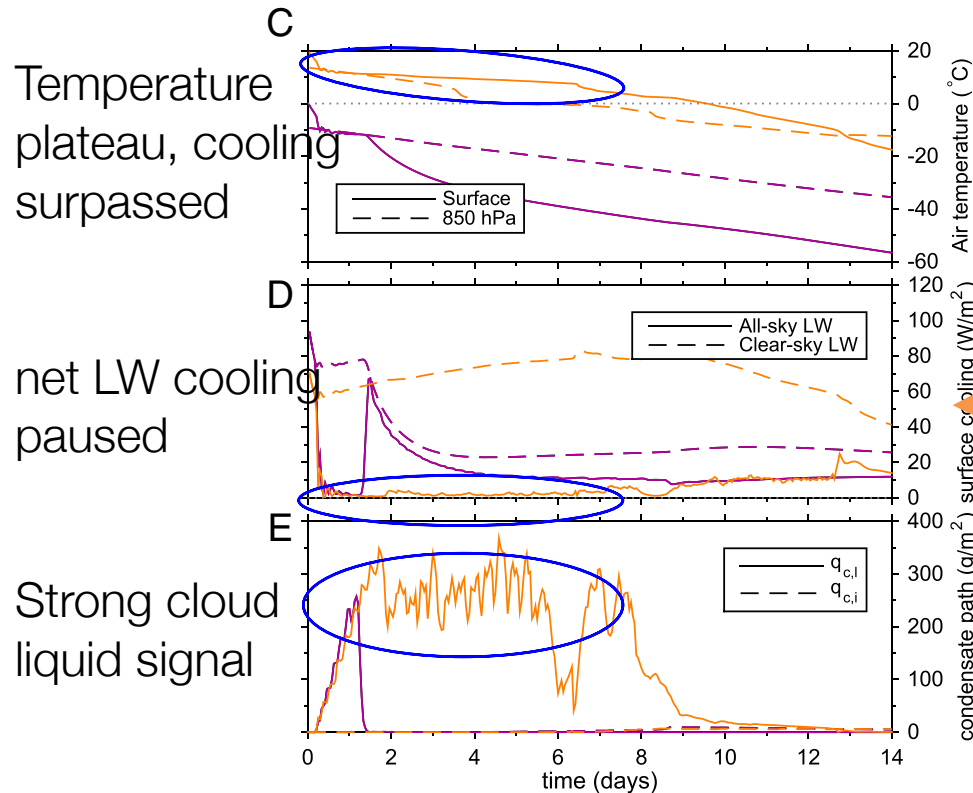
Consider orange curves



Day-1 cooling similar to cold initial conditions, but further surface cooling suppressed by LW effects of a liquid low cloud cloud layer!

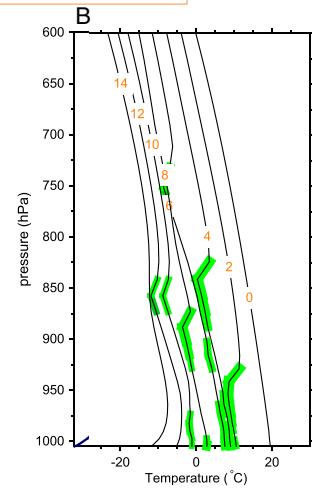
Arctic air suppression

Suppression of Arctic air formation for warmer initial conditions - mechanism



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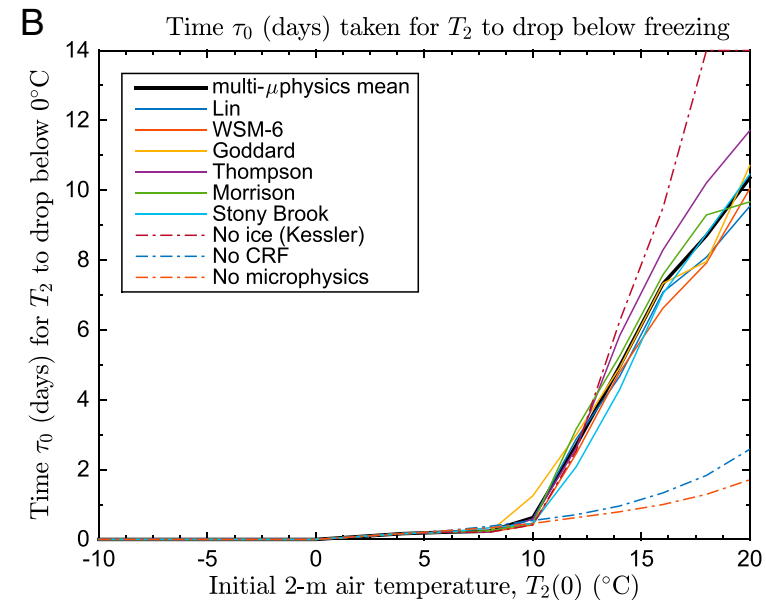
Consider orange curves



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Arctic air suppression

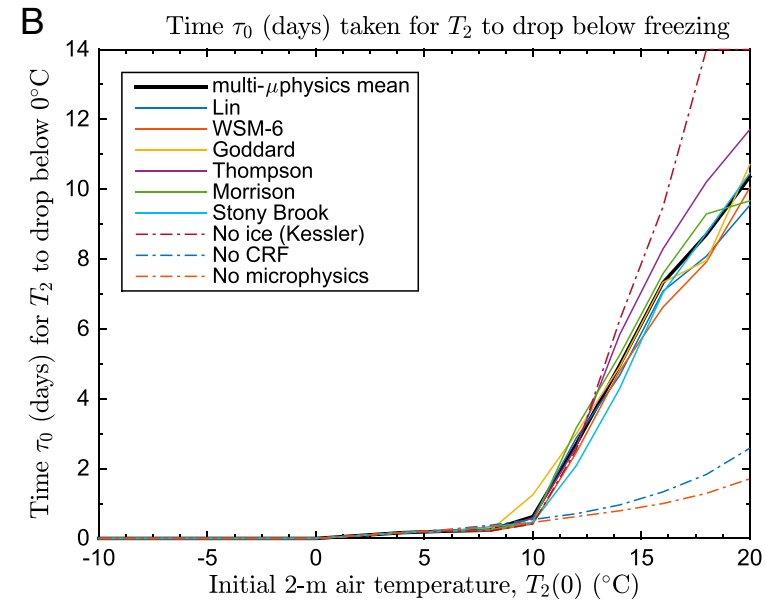
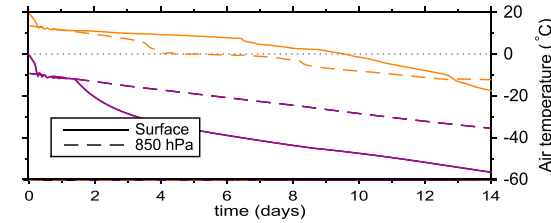
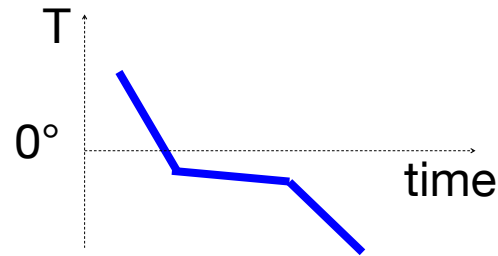
Time-to-freezing increases nonlinearly w/initial (ocean) temperature



Arctic air suppression

Time-to-freezing increases nonlinearly w/initial (ocean) temperature

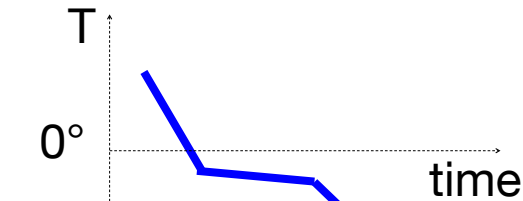
Cold initial conditions



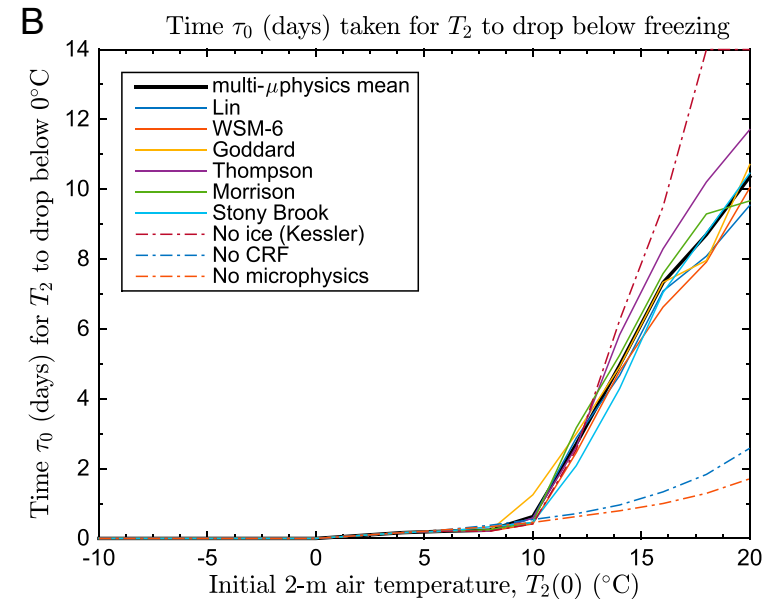
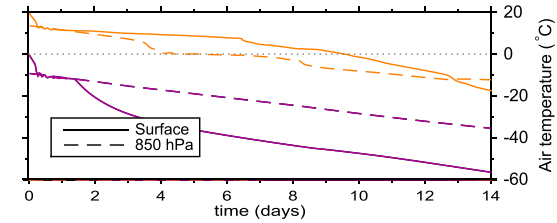
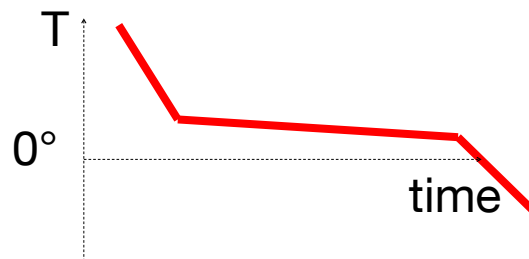
Arctic air suppression

Time-to-freezing increases nonlinearly w/initial (ocean) temperature

Cold initial conditions



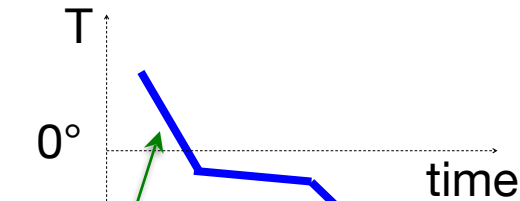
Warm initial conditions



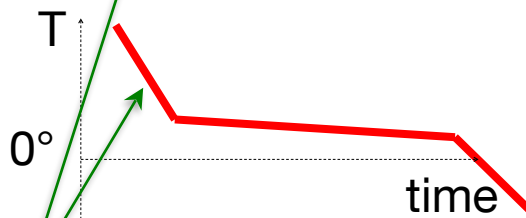
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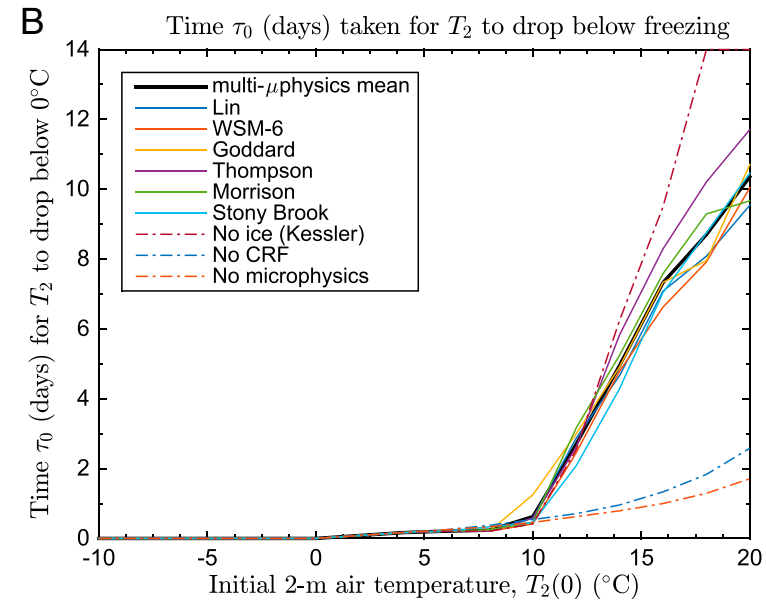
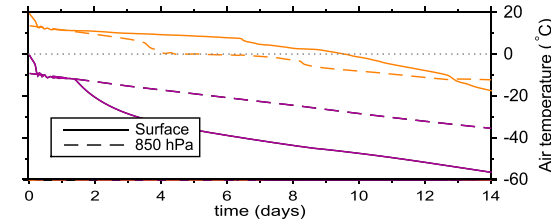
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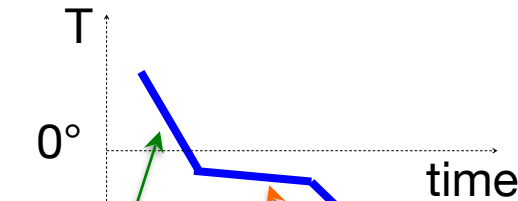
Initial cooling before low clouds



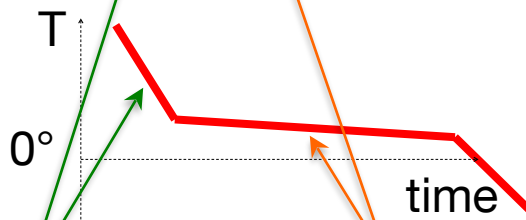
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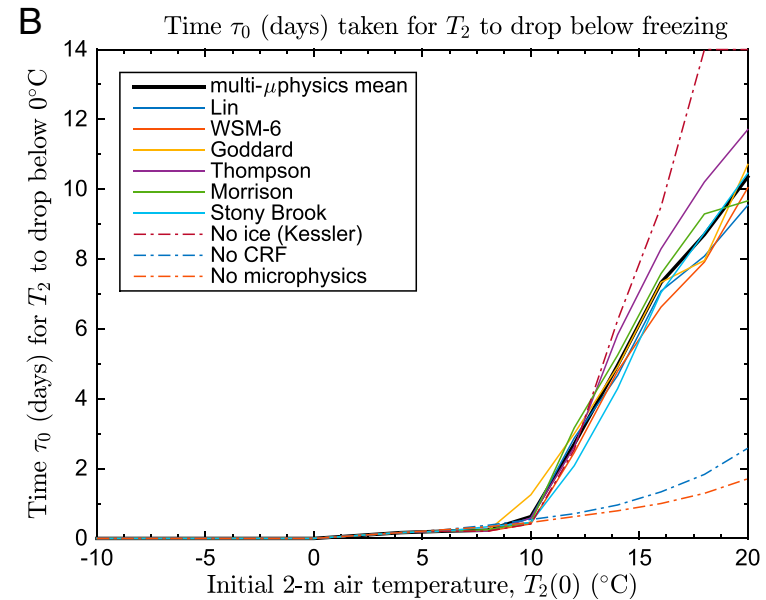
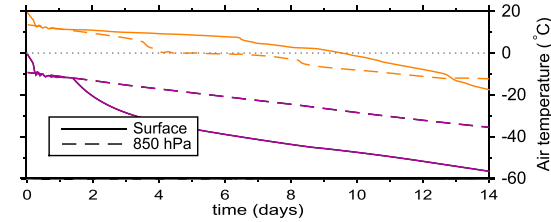


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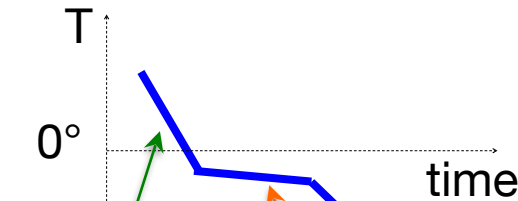
Plateau of suspended cooling due to low clouds



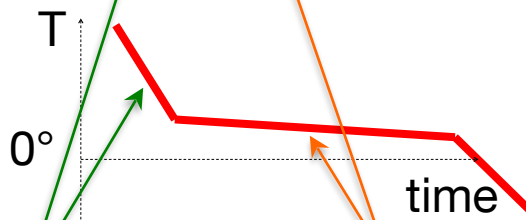
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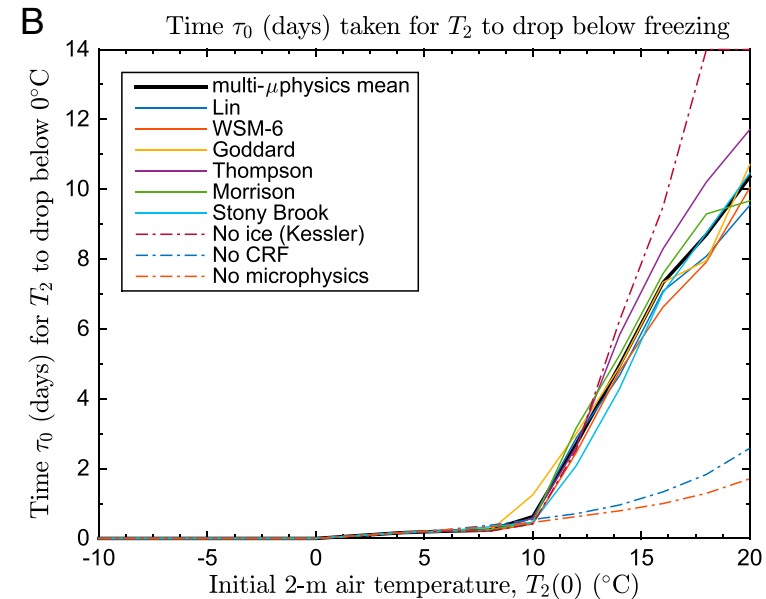
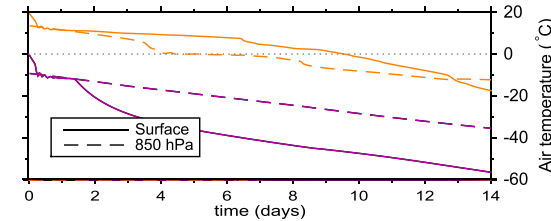


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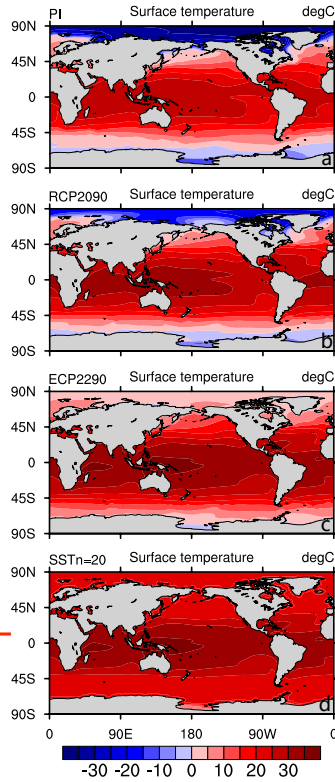
Time-to-freezing increases rapidly for $T_2(t=0) > 10^\circ\text{C}$ because plateau occurs above freezing point then and keeps $T_2 > 0$ for a few days.

Arctic air suppression in a 3-dimensional atmospheric GCM

Preindustrial
SST



Warmer SST

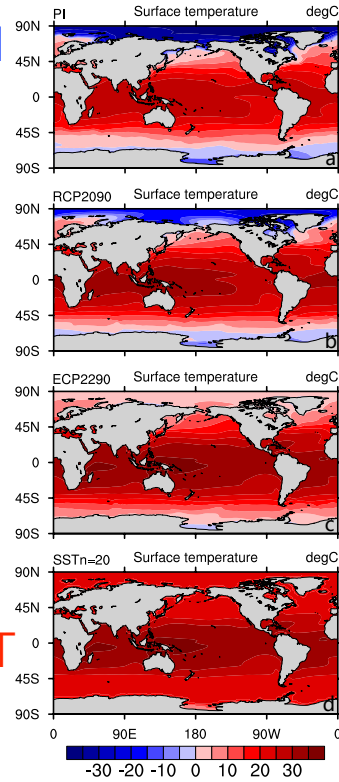


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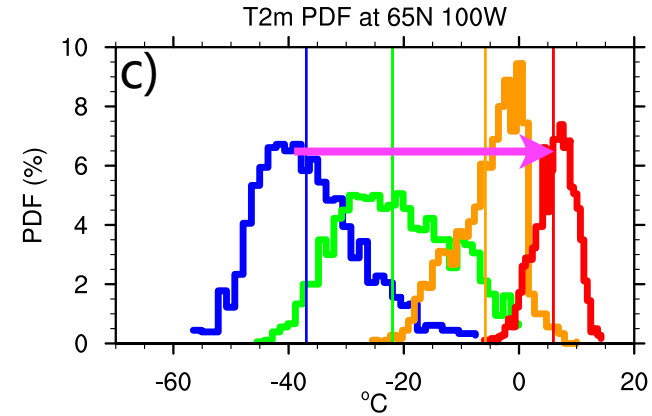
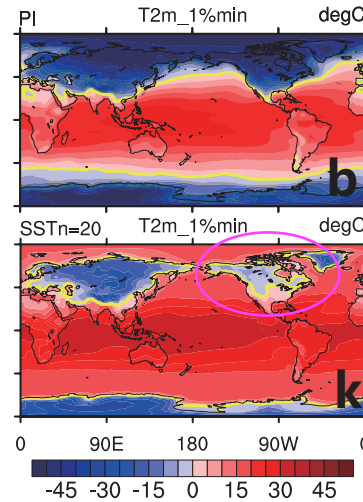


Warmer SST



coldest
2m T for
PI

coldest
2m T for
warm
SST



Coldest temperatures warm (mean&pdf),

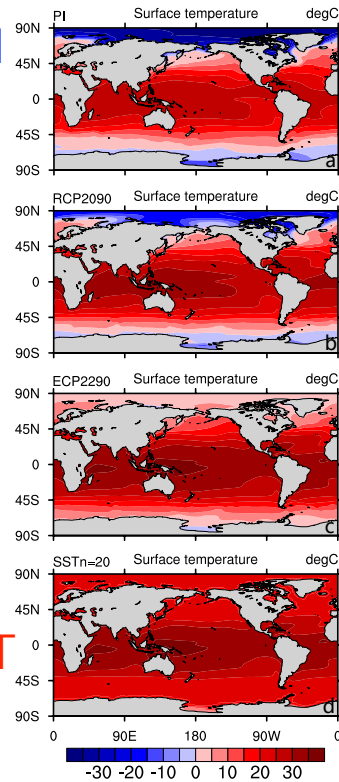
Hu, Cronin,
Tziperman, 2018

Arctic air suppression in a 3-dimensional atmospheric GCM

Preindustrial SST



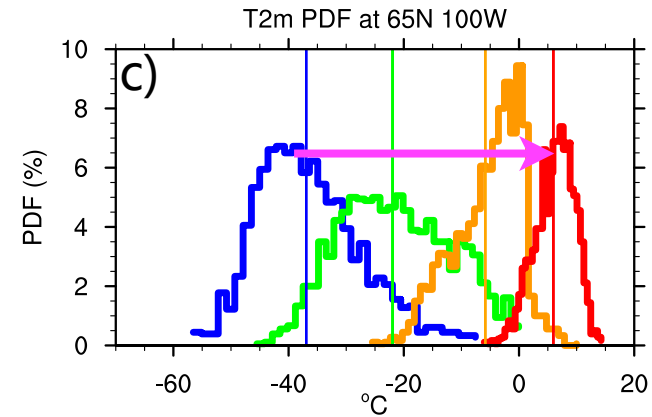
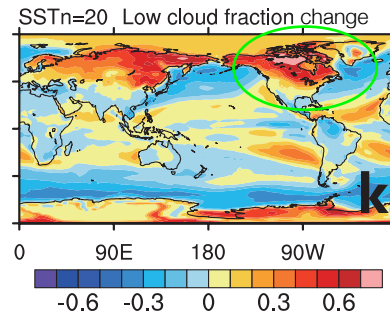
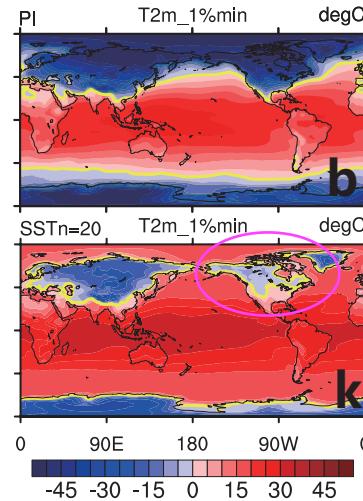
Warmer SST



coldest 2m T for PI

coldest 2m T for warm SST

low clouds increase over land



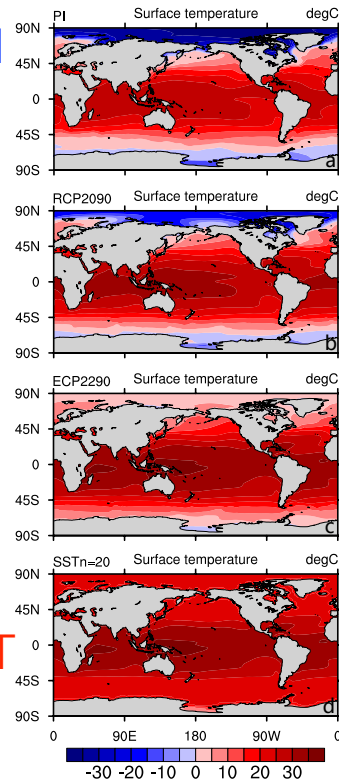
Coldest temperatures warm (mean&pdf),
more low clouds over land,

Arctic air suppression in a 3-dimensional atmospheric GCM

Preindustrial SST



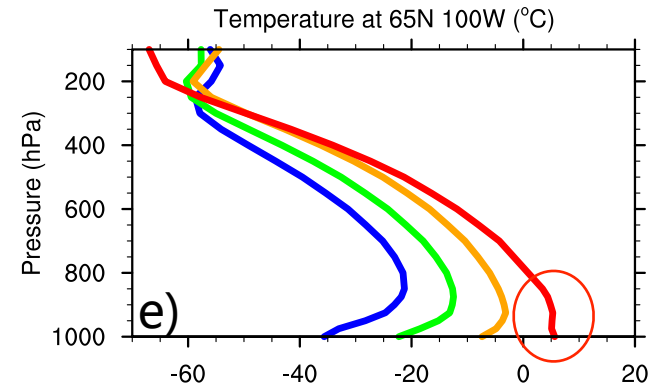
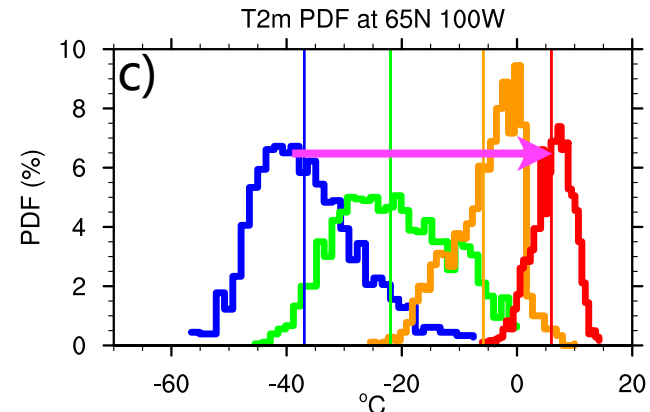
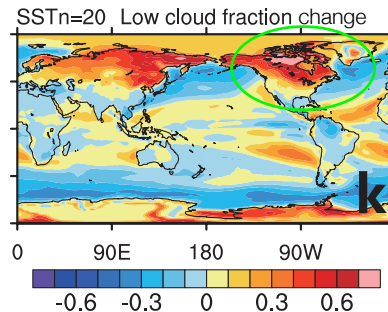
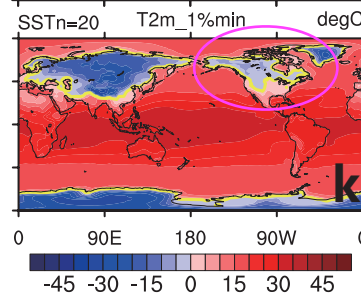
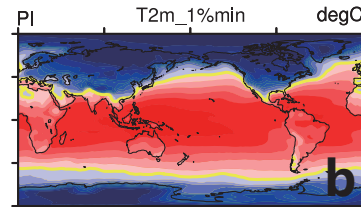
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Coldest temperatures warm (mean&pdf),
more low clouds over land,
T profile without inversion

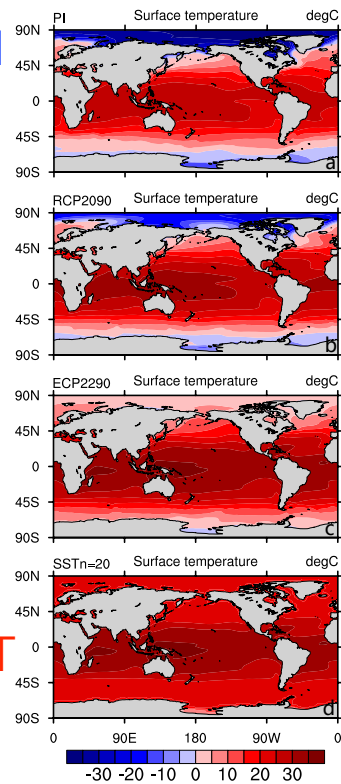
Hu, Cronin,
Tziperman, 2018

Arctic air suppression in a 3-dimensional atmospheric GCM

Preindustrial SST



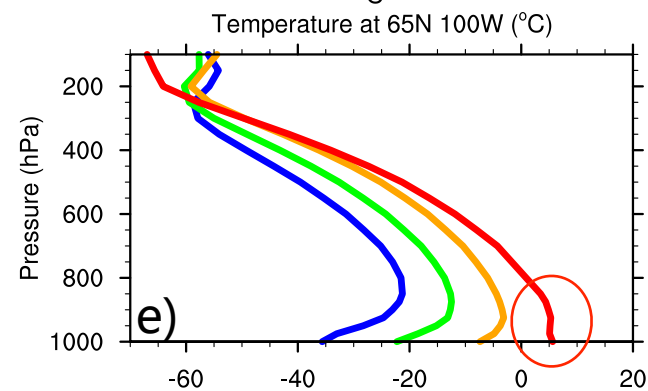
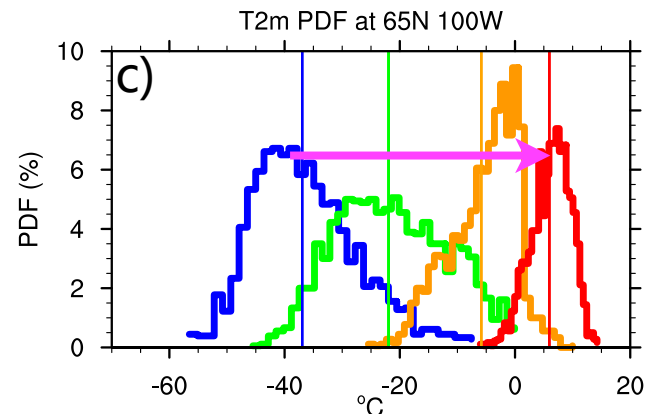
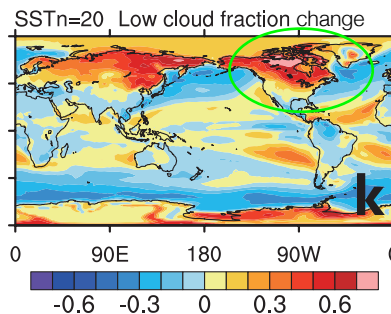
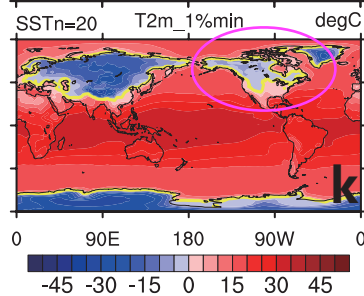
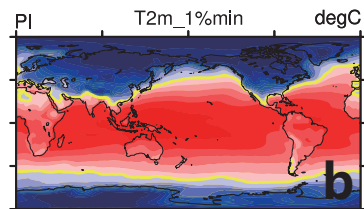
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Hu, Cronin,
Tziperman, 2018

T profile without inversion - all consistent w/ Arctic air suppression

Arctic convective cloud feedback

wintertime
deep Arctic
convection



→ high cloud
emissivity/
greenhouse
effect

→ Warmer
winter Arctic

Abbot & Tziperman 2008

(6)

Arctic convective cloud feedback: idea & outline

Idea:

- In a warm climate, deep convection—which today occurs mostly in the tropics—may occur in the Arctic during polar night (😬)
- Convective cloud greenhouse effect keeps winter Arctic ice-free.
- Warmer Arctic warms temperature minima at nearby continents.

Arctic convective cloud feedback: idea & outline

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Outline:

1. Moist Static Energy, calculating MSE conserving T profile.
2. Moist convection: Lift Condensation Level, Level of Free Convection, Level of Neutral Buoyancy.
3. Condition on stability to convection between the surface ($z=0$) and a height z based on MSE_s vs $MSE^*(z)$.
4. 2-level model formulation.
5. The solution, multiple equilibria, and hysteresis.
6. GCM verification.

Moist convection and cloud formation

Moist static energy (MSE), the energy per unit mass of a moist air parcel, is conserved when the parcel is lifted adiabatically in the atmosphere,

$$MSE(z) = c_p T(z) + gz + Lq(z)$$

c_p : specific heat, J/(kg K); L : latent heat of condensation J/kg;

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Parcel starts at surface, with $MSE_s = c_p T_s + Lq_s$.

Initially, the rising air parcel is not saturated & there is no condensation,

$q(z) = q_s$ so that the conservation may be written in terms of the *Dry*

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This leads to a solution for the temperature profile and lapse rate,

$$T(z) = T_s - gz/c_p, \quad dT/dz = -g/c_p = -9.8 \text{ K/km}$$

Moist convection and cloud formation

The parcel keeps rising & cooling, until the saturation moisture is smaller than the parcel's moisture & condensation occurs, $q(z) = q^*(T(z), p(z))$. The conservation law is $c_p T(z) + Lq^*(T(z), p(z)) + gz = MSE_s$ which may be solved graphically for $T(z)$.

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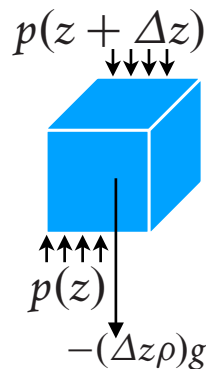
$$MSE_s = c_p T(z) + gz + L \min(q_s, q^*(T(z), p(z)))$$

To solve, need to find $p(z)$ from the vertical momentum (hydrostatic) balance for an air parcel: $dp/dz = -\rho g$. Using $\rho = p/(RT)$ this becomes $dp/dz = -pg/RT$, or $d \ln p = -(g/RT) dz$.

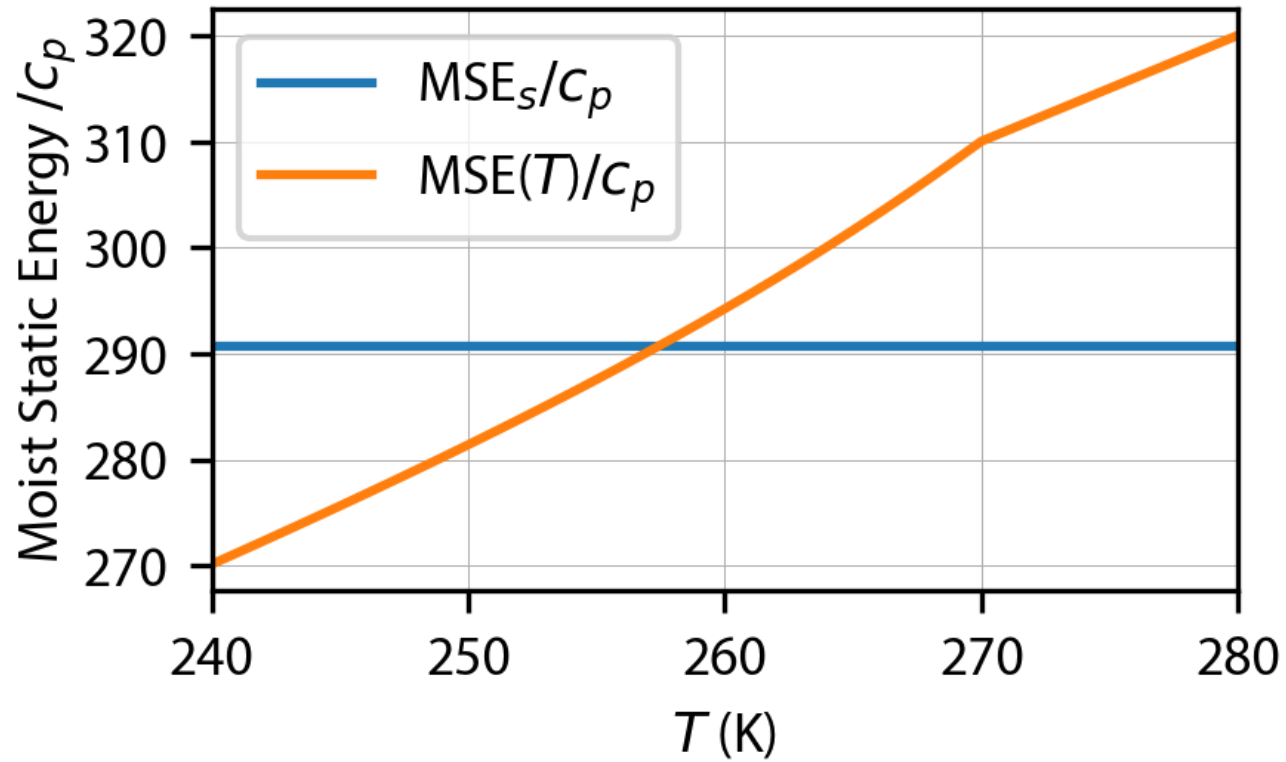
Integrating, we find $\ln p(z) - \ln p_s = -gz/R\bar{T}$,

so that $p(z) = p_s e^{-gz/R\bar{T}}$

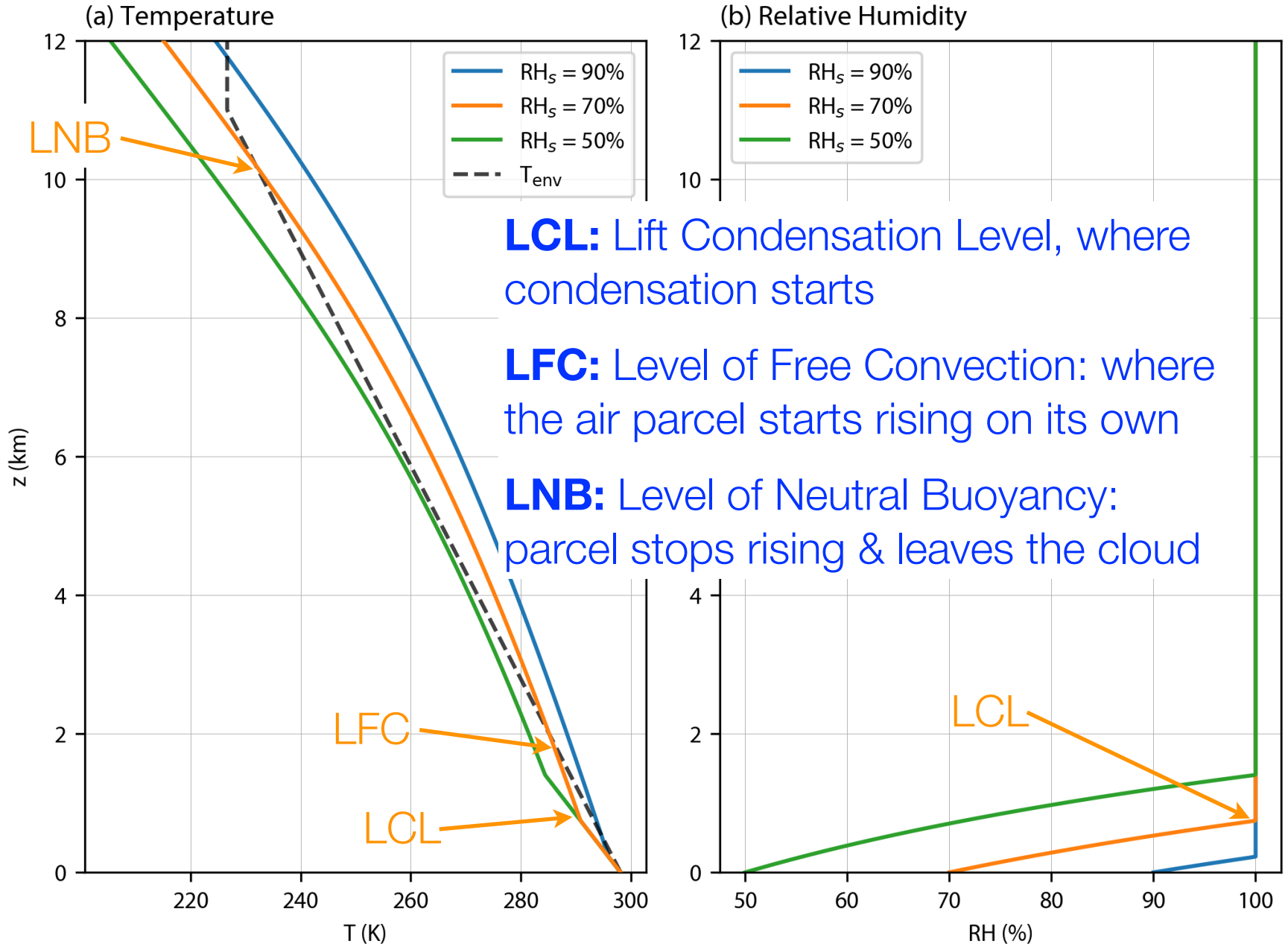
➔ pressure is exponential in height.



Calculating T from MSE conservation



Moist Convection: LCL, LFC, LNB



Condition for convection to occur between surface & z

Condition for convection to occur between surface & z

If z is high enough, we expect a parcel starting at the surface to be saturated there:

$$MSE^{parcel}(z) = MSE^{*,parcel}(z).$$

MSE conservation for the parcel also implies:

$$MSE^{parcel}(0) = MSE^{parcel}(z) = MSE^{*,parcel}(z)$$

A parcel brought to z will be unstable if

$$T^{parcel}(z) \geq T^{env}(z)$$

Because MSE^* is only a function of temperature, this can be written as

$$MSE^{*,parcel}(z) \geq MSE^{*,env}$$

Given above conservation for parcel, condition for convection becomes

$$MSE_s \geq MSE^{*,env}$$

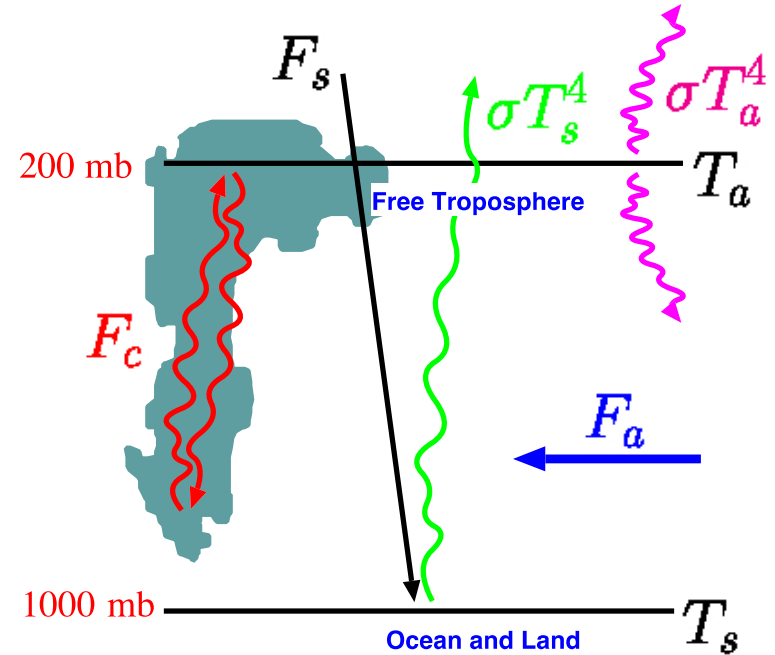
Multiple equilibria due to convective cloud feedback

(Abbot & Tziperman 2009)

A 2-level energy balance model with convective heat flux:

$$C_s dT_s/dt = F_s - F_c + \epsilon\sigma T_a^4 - \sigma T_s^4,$$

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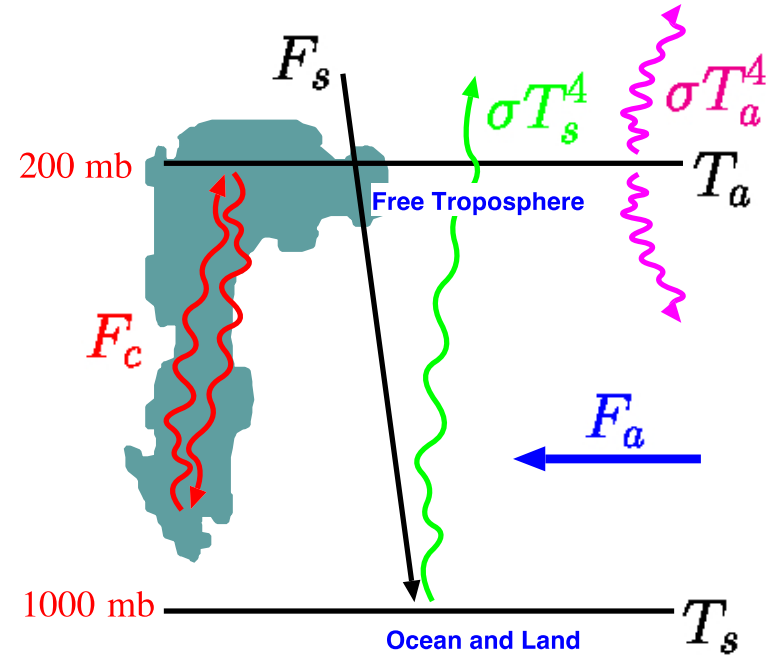
convection occurs when moist static

Energy (MSE) satisfies

$$MSE_s = C_p T_s + gz_s + Lr_s$$

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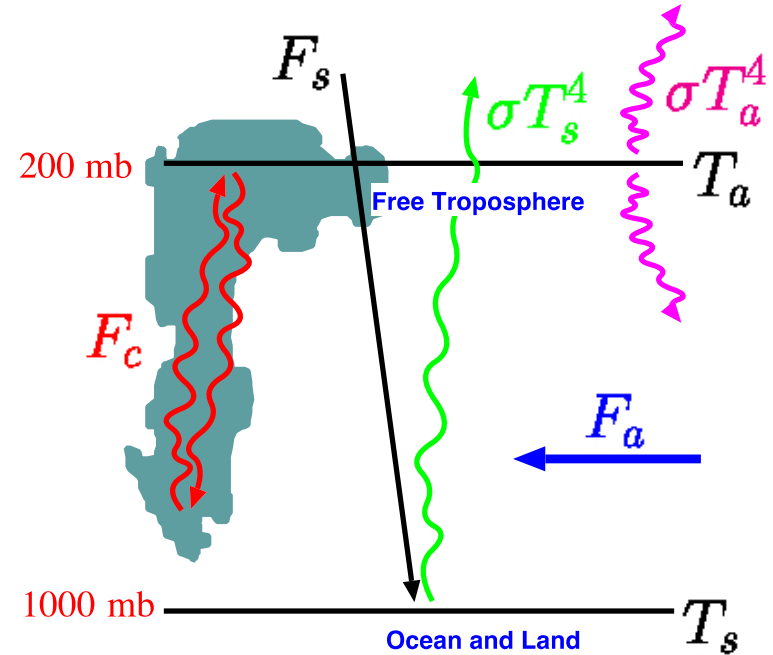
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Without convection, find two temperatures from:

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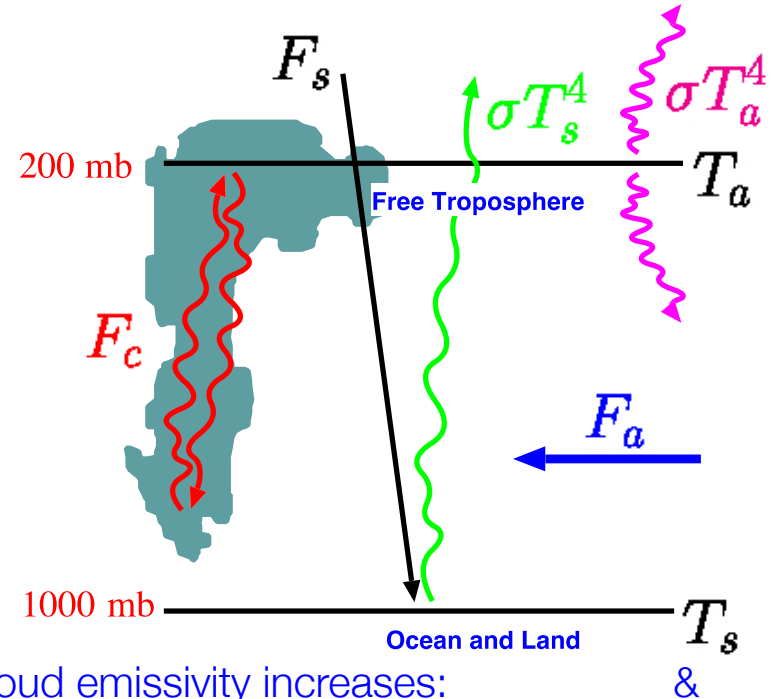
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With convection: cloud emissivity increases:
found from

$$\tilde{\epsilon} = \epsilon_0 + \Delta\epsilon(F_c, T_a, T_s)$$

$$0 = F_s - F_c + \tilde{\epsilon}\sigma T_{s2}^4 - \sigma T_{s2}^4,$$

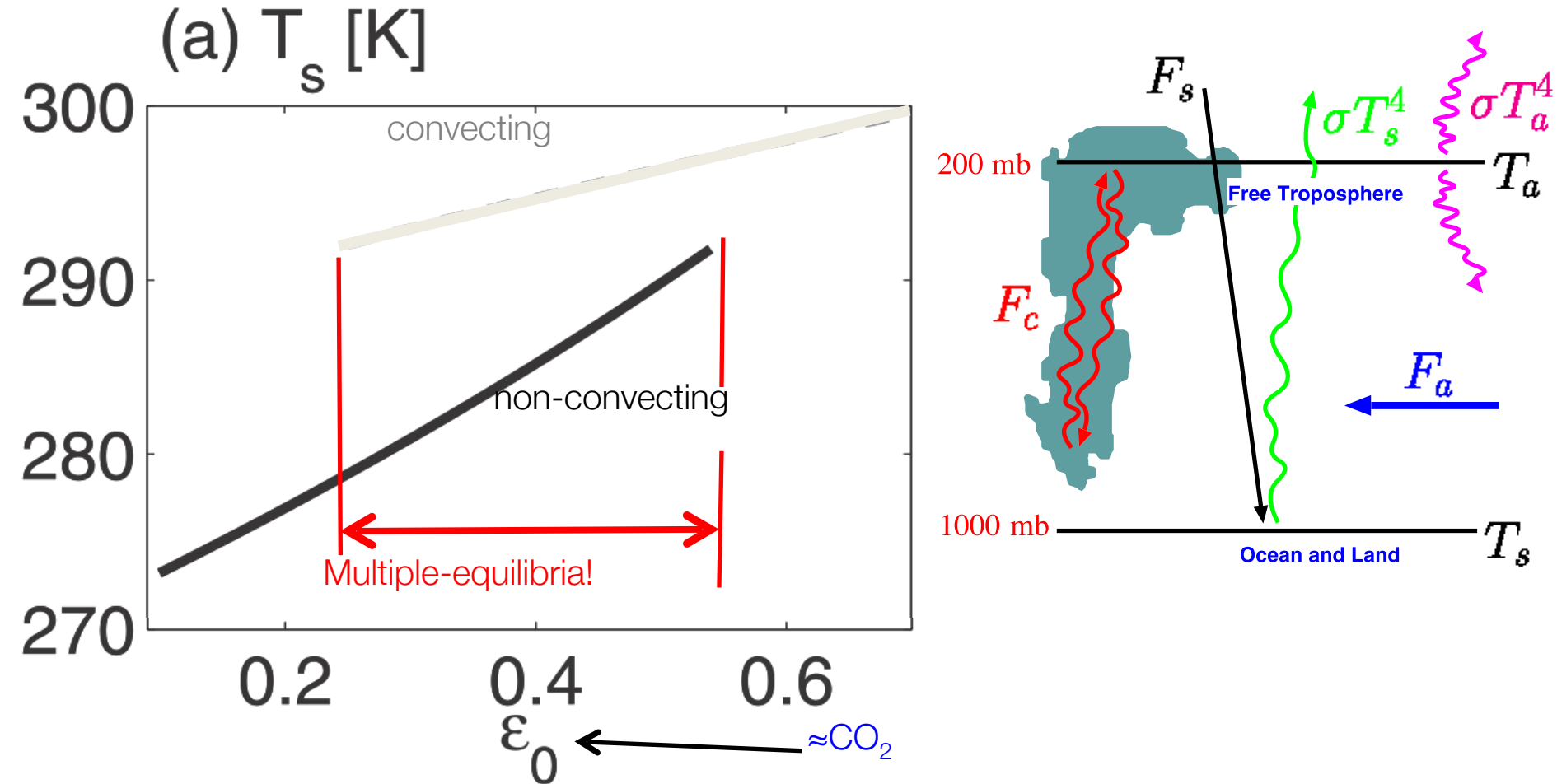
$$0 = F_a + F_c + \tilde{\epsilon}\sigma(T_{s2}^4 - 2T_{a2}^4),$$

$$C_p T_{s2} + Lr_{s2} = C_p T_{a2} + Lr_{a2}^* + gz_a$$

Multiple equilibria due to convective cloud feedback

(Abbot & Tziperman 2009)

Results for surface temperature: multiple equilibria!



Note: must check self-consistency of sol'n with/without convection

Multiple equilibria due to convective cloud feedback

(Abbot & Tziperman 2009)

Reviews & then the following slide with GCM results supporting this mechanism

Back to the future

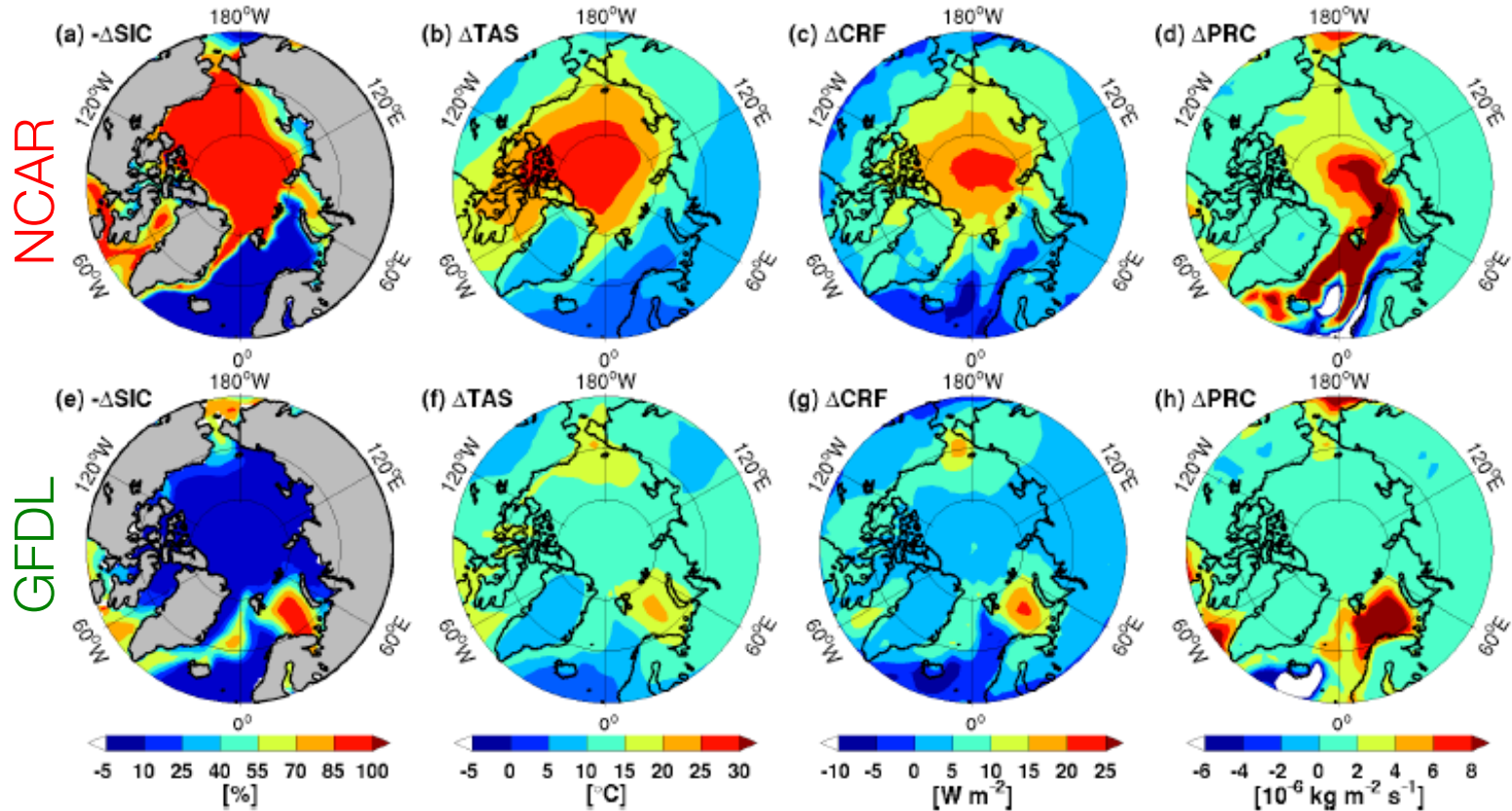


Enticing 3D IPCC Model Simulations

Consider the NCAR & GFDL 3d coupled ocean-atmosphere state-of-the-art (2009...) models, at x4 CO₂; anomaly from pre-industrial

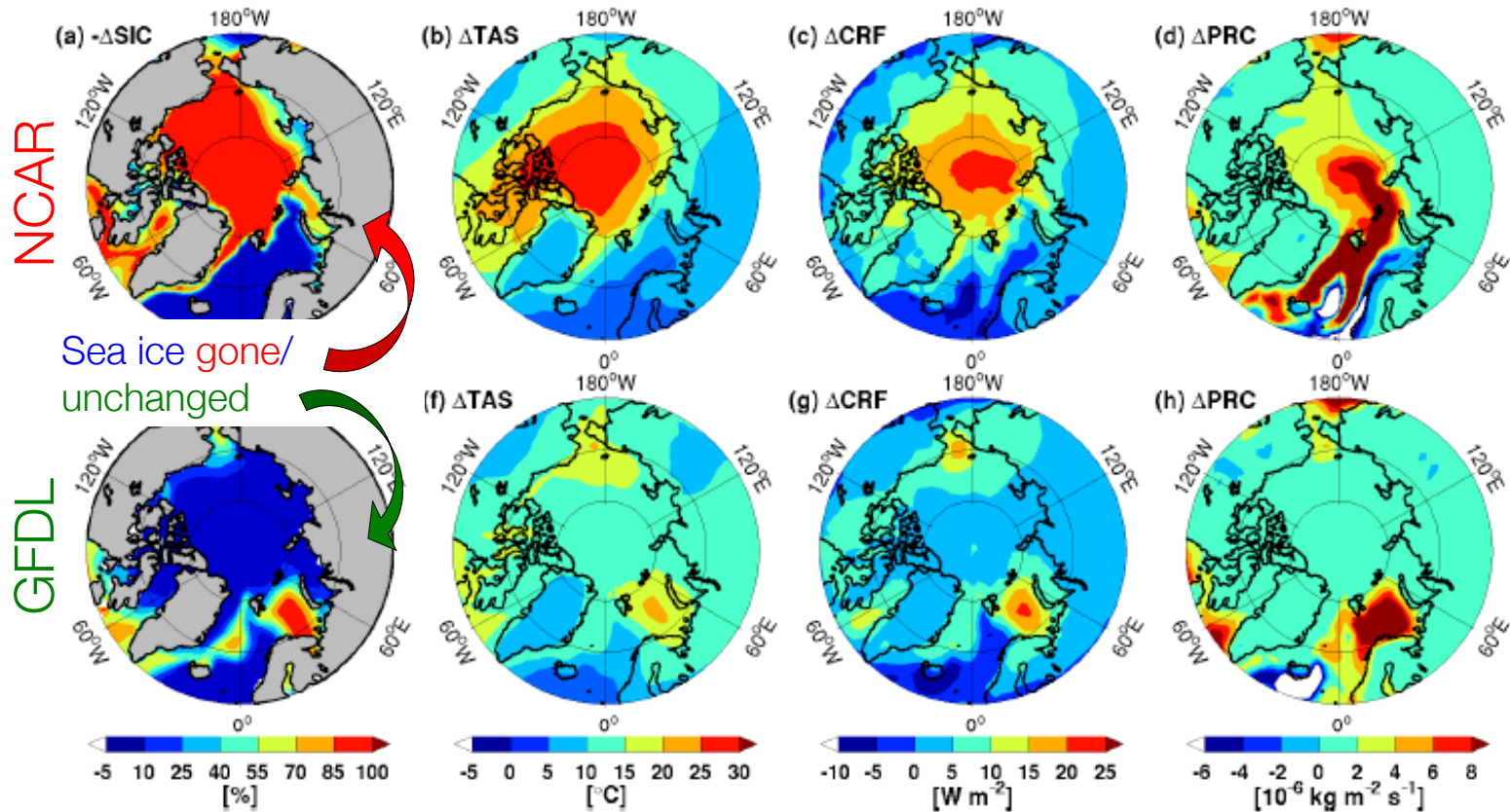
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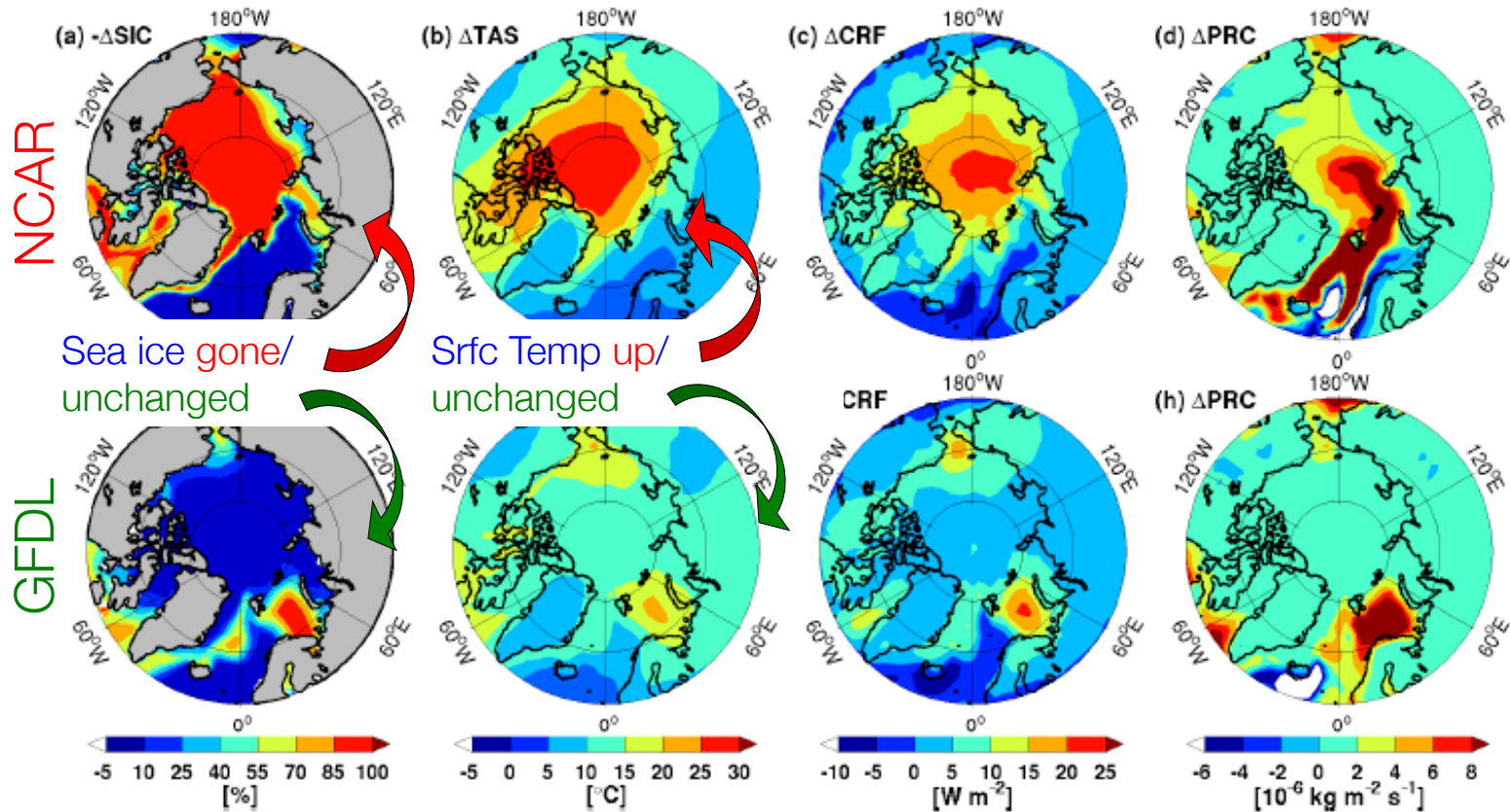
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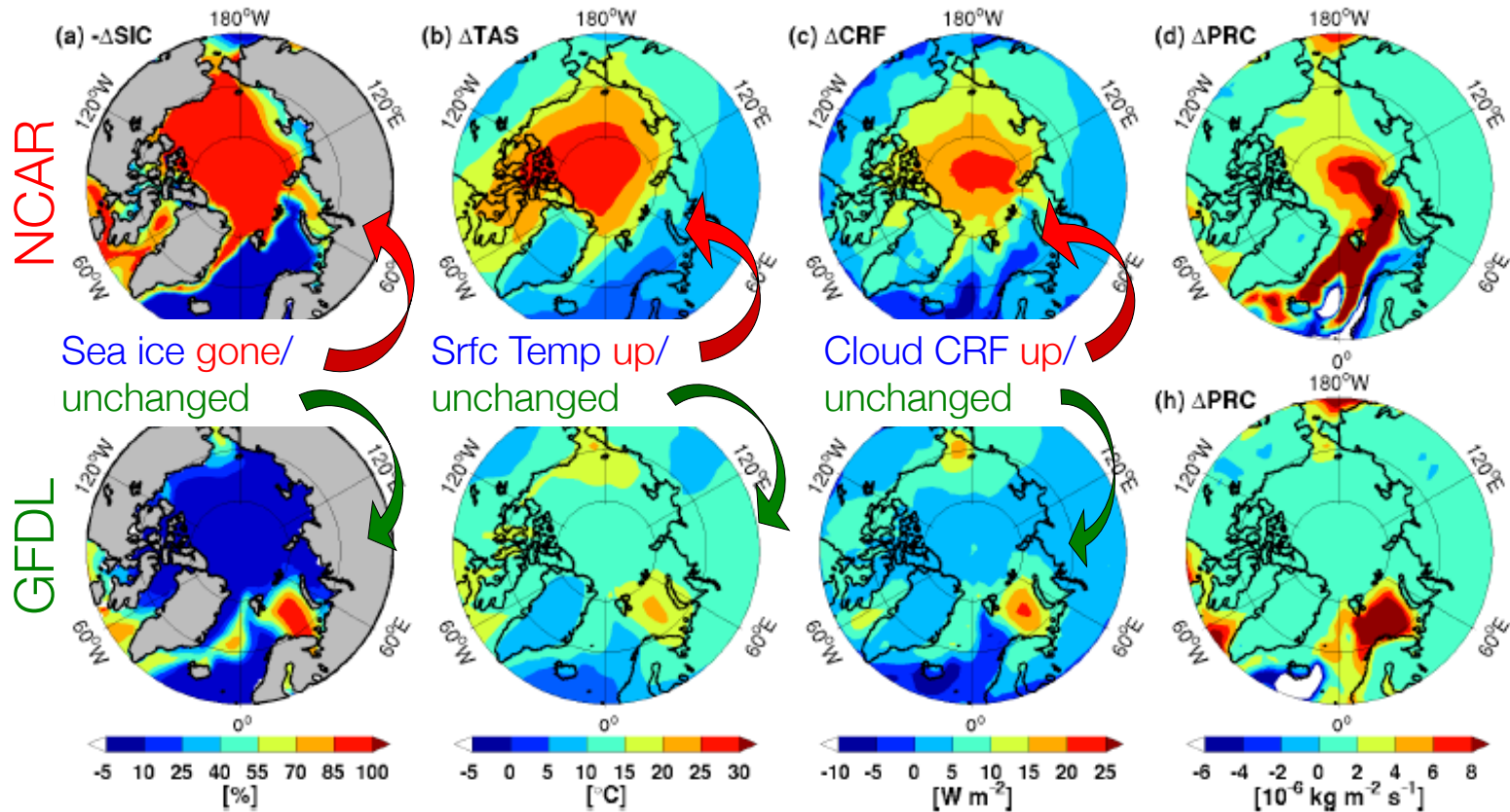
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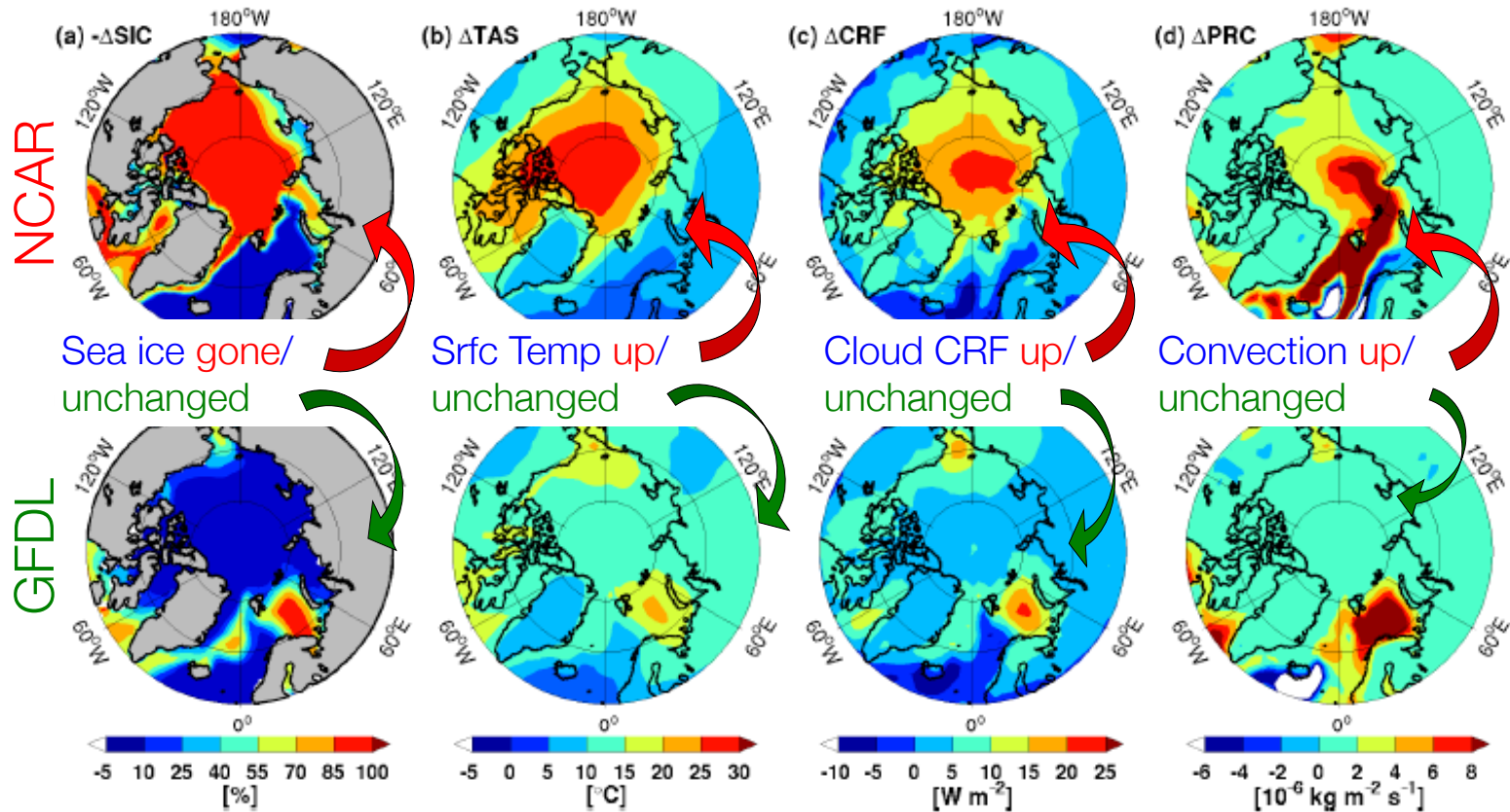
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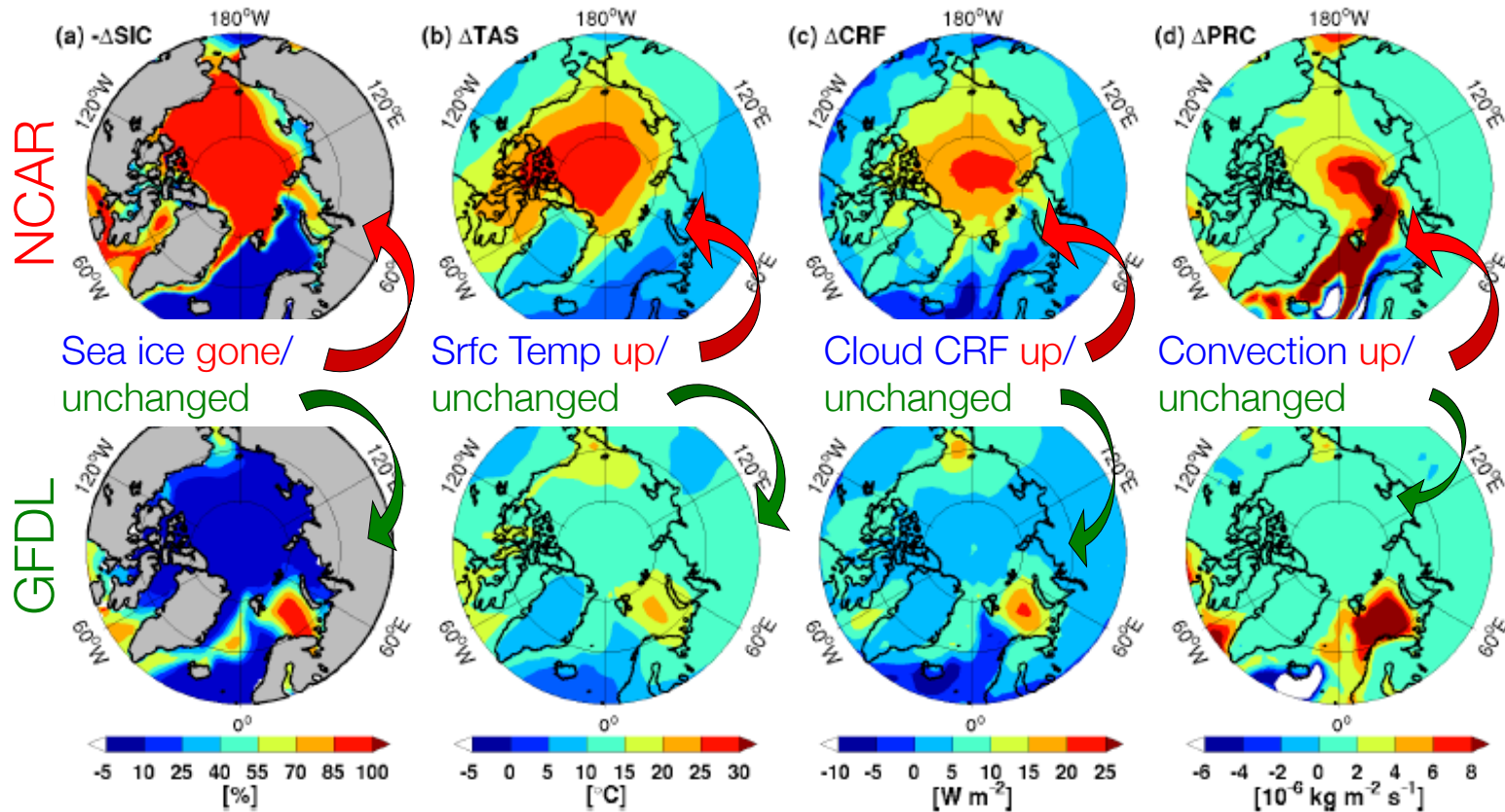
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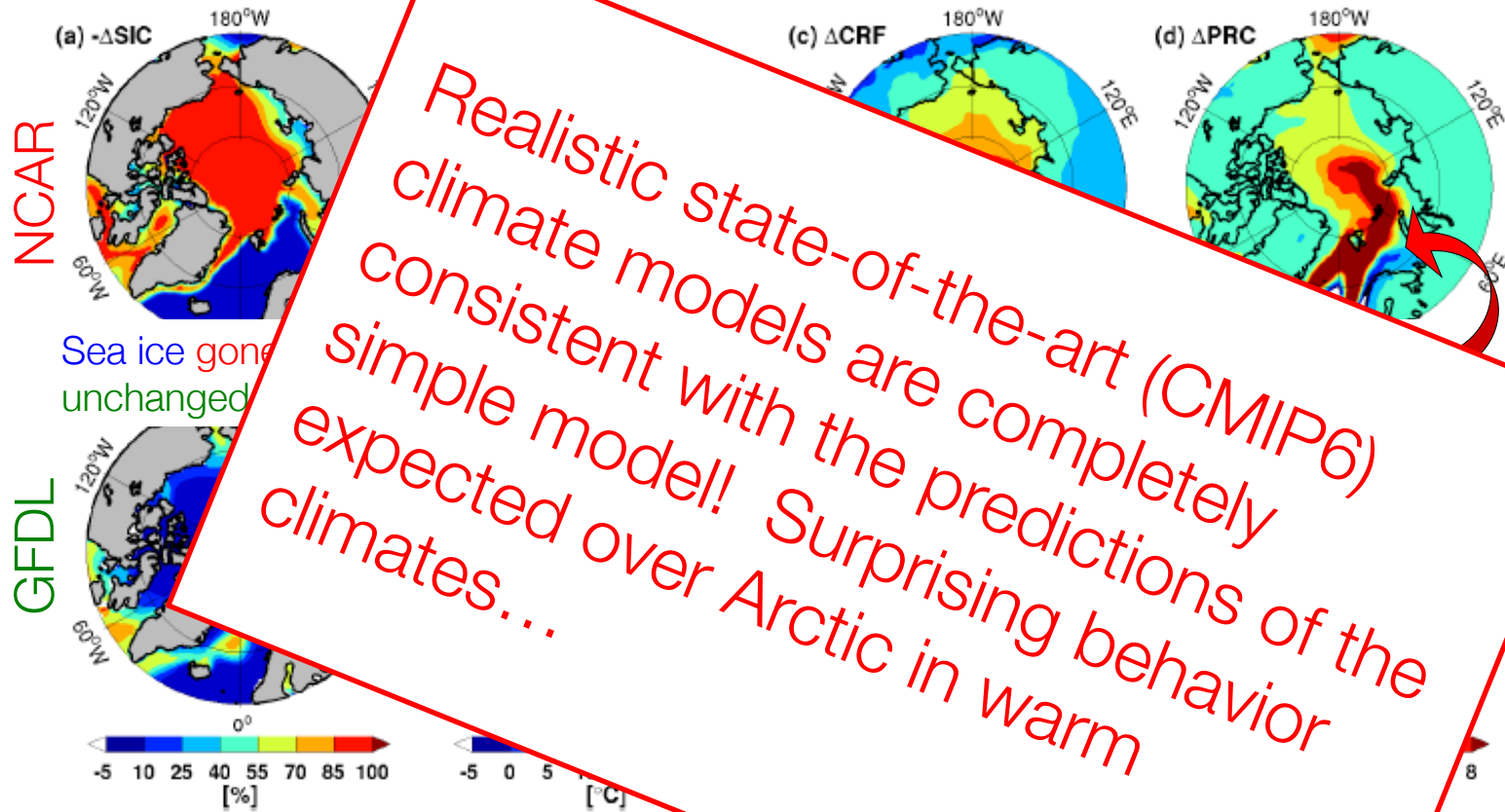
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→ IPCC NCAR 3d model behaves like toy model!!

Enticing 3D IPCC Model Simulations

Consider the **NCAR** & **GFDL** 3d coupled ocean-atmosphere state-of-the-art (2009...) models, at x4 CO₂; anomaly from pre-industrial



→ IPCC NCAR 3d model behavior is completely consistent with the simple model!!

In-class workshop

For each of the six mechanisms covered:

- What did we learn about the natural climate system regardless of the warm climate behavior?
- Come up with a one-minute summary of (two for polar stratospheric clouds, for the two versions there),
- Come up with a one-sentence summary of the weakness(es) of the proposed mechanism.

Equable climate summary

back to two initial overview slides with 6 mechanisms

The End