

## Interprocedural Analysis

CS252r Spring 2011

#### Procedures

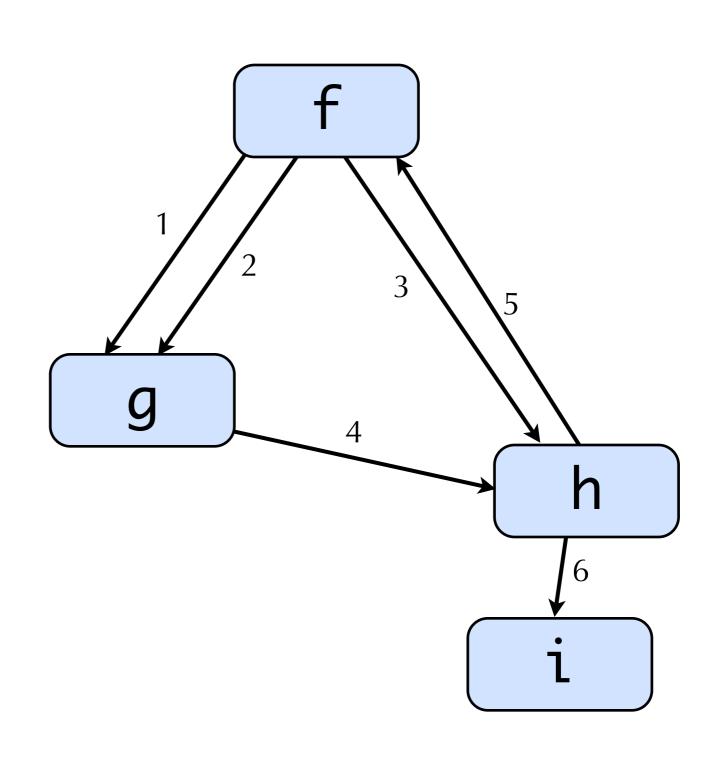
- So far looked at intraprocedural analysis: analyzing a single procedure
- Interprocedural analysis uses calling relationships among procedures
  - Enables more precise analysis information

# Call graph

- First problem: how do we know what procedures are called from where?
  - Especially difficult in higher-order languages, languages where functions are values
  - We'll ignore this for now, and return to it later in course...
- Let's assume we have a (static) call graph
  - Indicates which procedures can call which other procedures, and from which program points.

## Call graph example

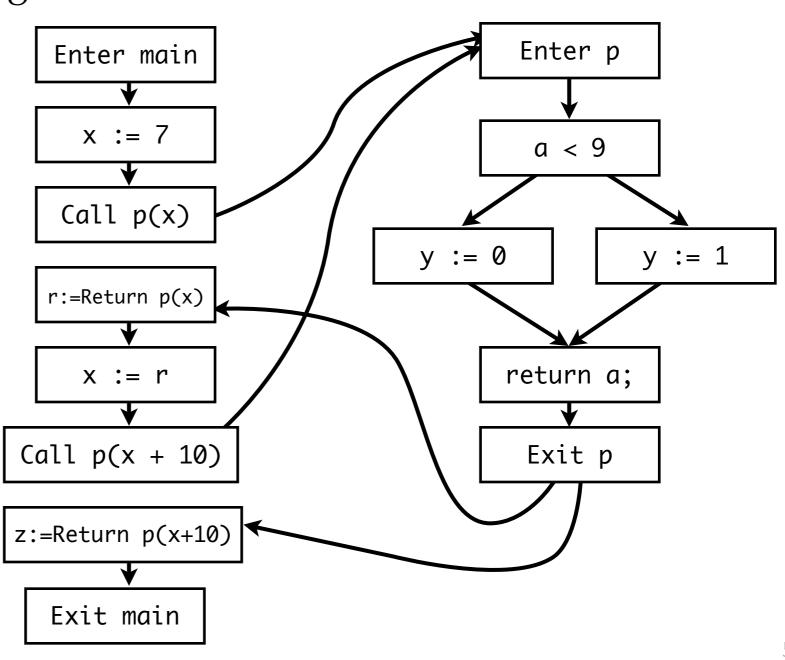
```
f() {
 1: g();
  2:
     g();
   3: h();
g() {
  4: h();
h() {
 5: f();
   6: i();
i() { ... }
```



## Interprocedural dataflow analysis

- How do we deal with procedure calls?
- Obvious idea: make one big CFG

```
main() {
  x := 7;
  r := p(x);
  x := r;
  z := p(x + 10);
p(int a) {
  if (a < 9)
    y := 0;
  else
    y := 1;
  return a;
```

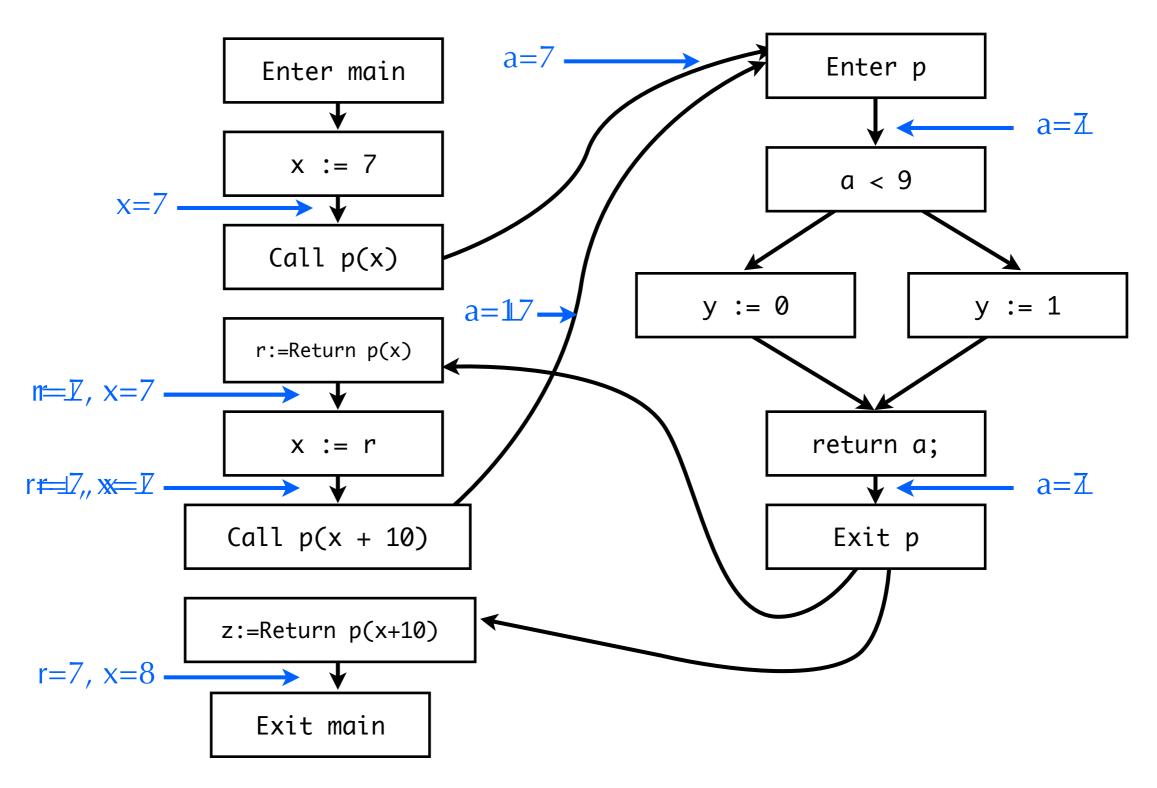


#### Interprocedural CFG

- CFG may have additional nodes to handle call and returns
  - Treat arguments, return values as assignments
- Note: a local program variable represents multiple locations

Set up environment for calling p a := x, ...Enter p Enter main x := 7 a < 9Call p(x)y := 0 y := 1 r:=Return p(x) x := rreturn a; Call p(x + 10)Exit p z:=Return p(x+10)Restore calling environment Exit main z := a

#### Example

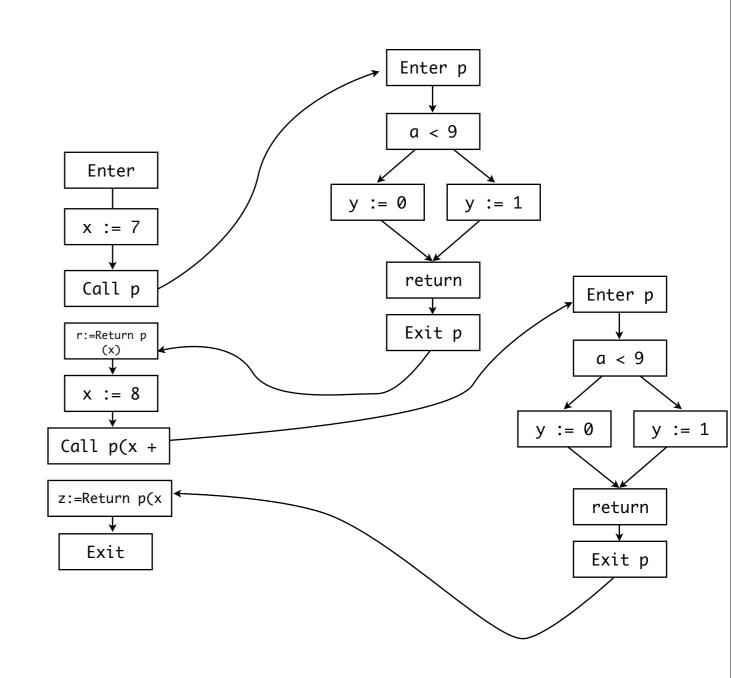


## Invalid paths

- Problem: dataflow facts from one call site "tainting" results at other call site
  - p analyzed with merge of dataflow facts from all call sites
- How to address?

# Inlining

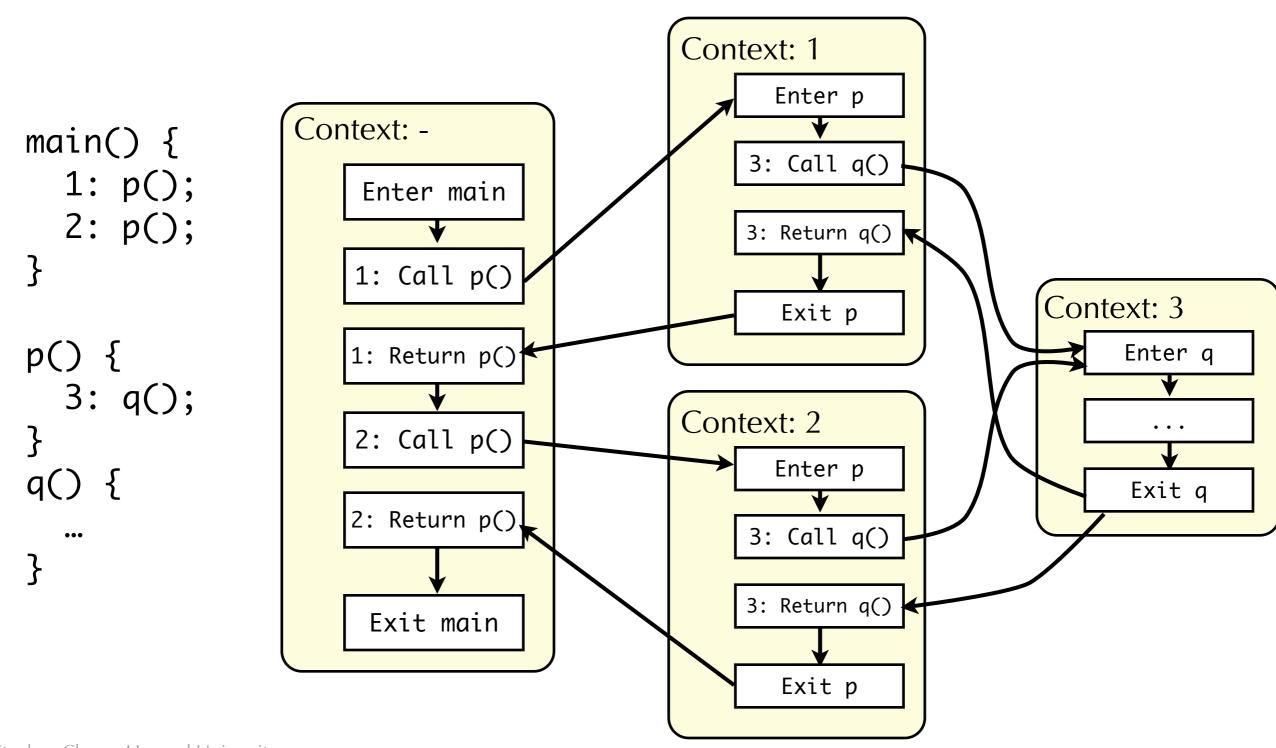
- Inlining
  - Use a new copy of a procedure's CFG at each call site
- Problems? Concerns?
  - May be expensive! Exponential increase in size of CFG
    - p() { q(); q(); } q() { r(); r() }
      r() { ... }
  - What about recursive procedures?
    - $p(int n) \{ ... p(n-1); ... \}$
    - More generally, cycles in the call graph



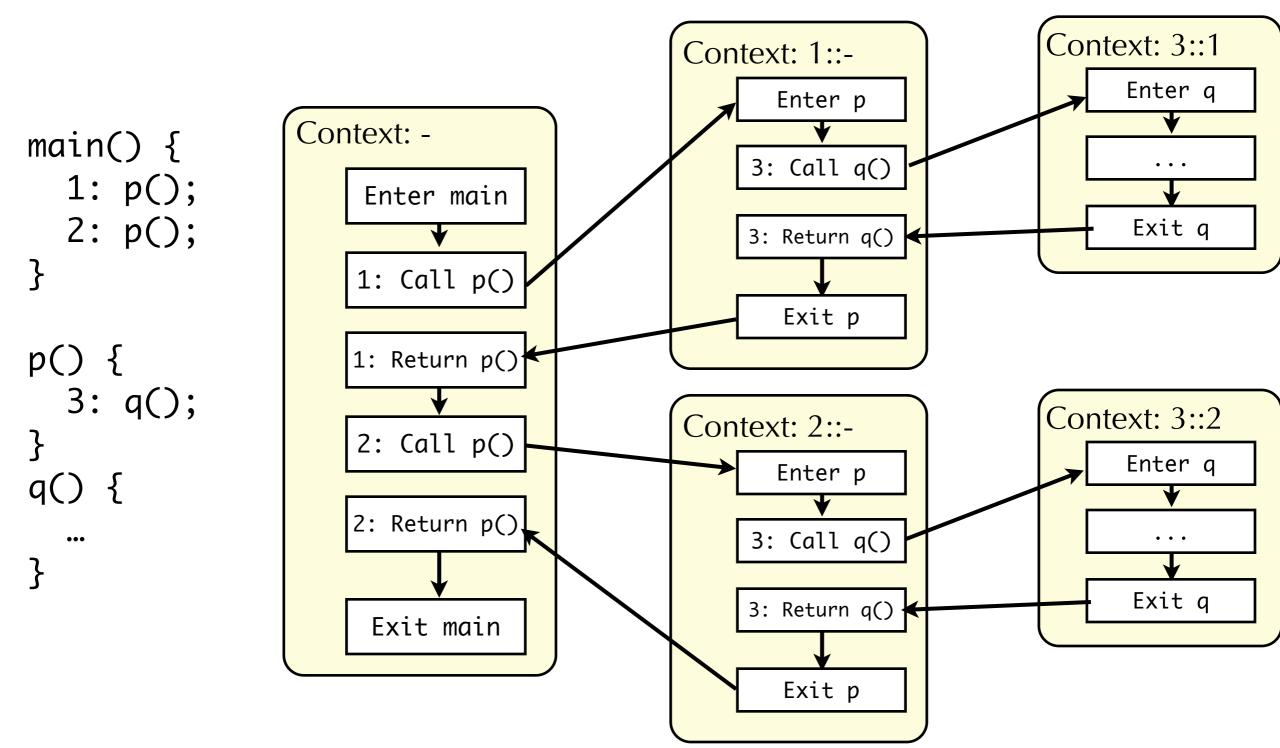
# Context sensitivity

- Solution: make a finite number of copies
- Use context information to determine when to share a copy
  - Results in a context-sensitive analysis
- Choice of what to use for context will produce different tradeoffs between precision and scalability
- Common choice: approximation of call stack

# Context sensitivity example

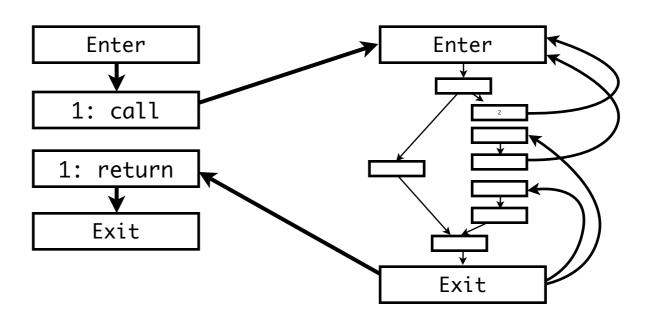


## Context sensitivity example

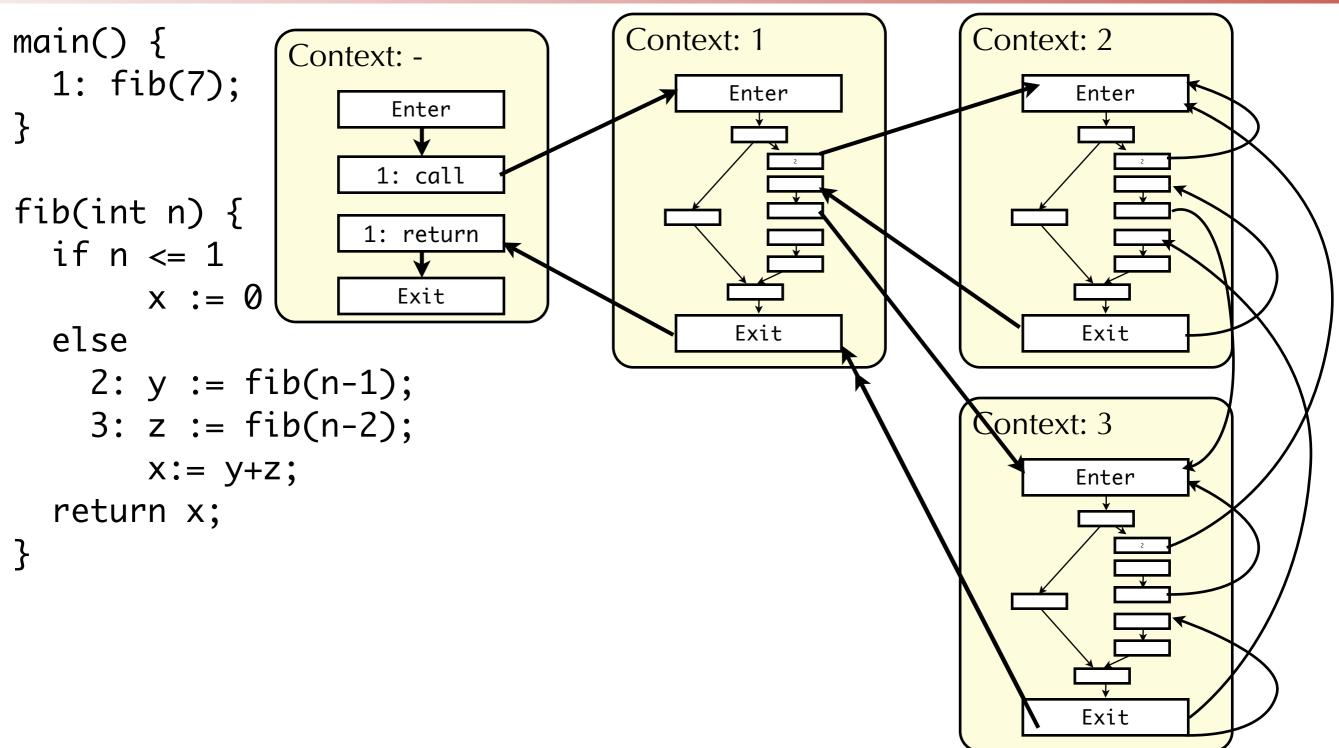


#### Fibonacci: context insensitive

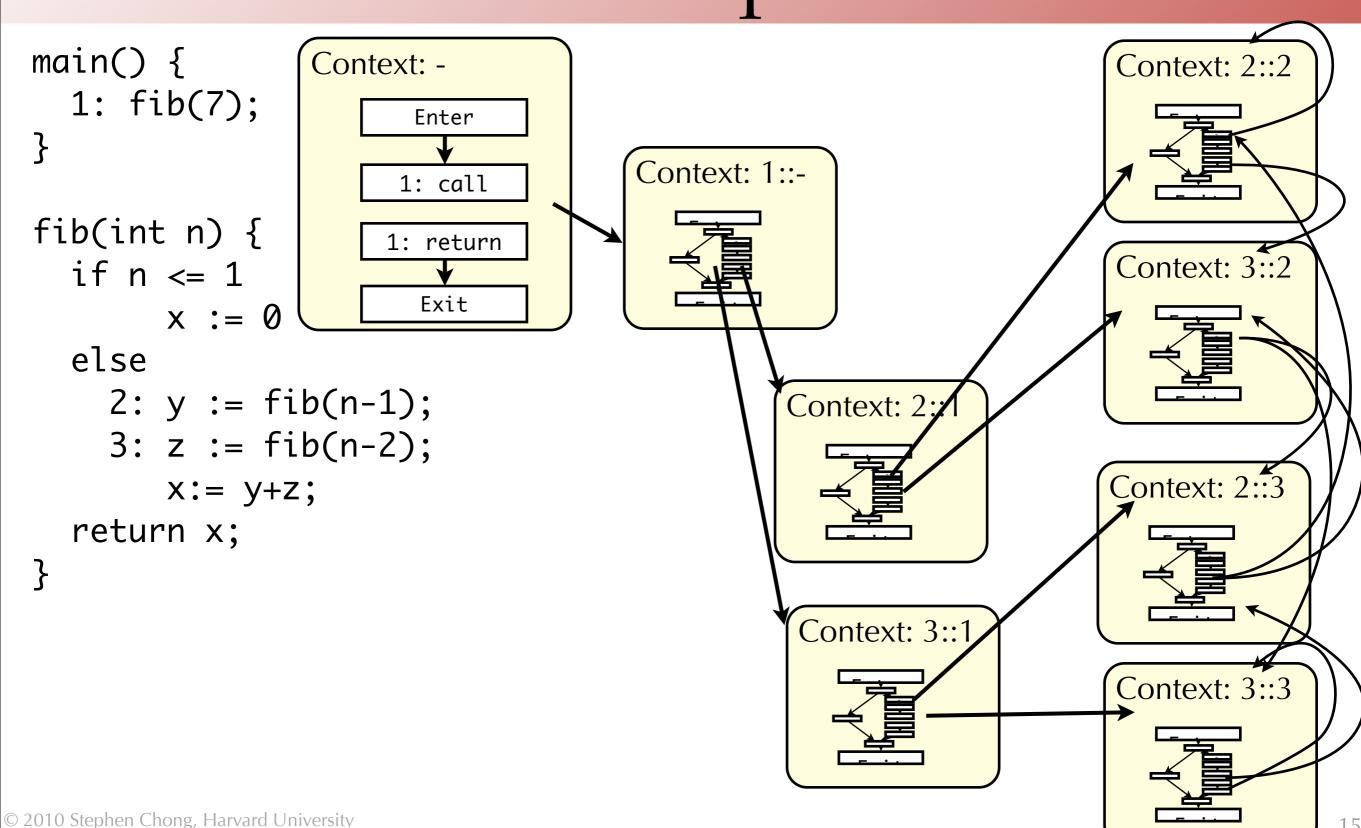
```
main() {
  1: fib(7);
fib(int n) {
  if n <= 1
      x := 0
  else
    2: y := fib(n-1);
    3: z := fib(n-2);
       X := y+z;
  return x;
```



# Fibonacci: context sensitive, stack depth 1



# Fibonacci: context sensitive, stack depth 2



#### Other contexts

- Context sensitivity distinguishes between different calls of the same procedure
  - Choice of contexts determines which calls are differentiated
- Other choices of context are possible
  - Caller stack
    - Less precise than call-site stack
    - E.g., context "2::2" and "2::3" would both be "fib::fib"
  - Object sensitivity: which object is the target of the method call?
    - For OO languages.
    - Maintains precision for some common OO patterns
    - Requires pointer analysis to determine which objects are possible targets
    - Can use a stack (i.e., target of methods on call stack)

#### Other contexts

- More choices
  - Assumption sets
    - What state (i.e., dataflow facts) hold at the call site?
    - Used in ESP paper
  - Combinations of contexts, e.g., Assumption set and object

#### Procedure summaries

- In practice, often don't construct single CFG and perform dataflow
- Instead, store procedure summaries and use those
- When call p is encountered in context C, with input D, check if procedure summary for p in context C exists.
  - If not, process p in context C with input D
  - If yes, with input D' and output E'
    - if  $D' \sqsubseteq D$ , then use E'
    - if  $D' \not\sqsubseteq D$ , then process p in context C with input  $D' \sqcap D$
  - If output of p in context C changes then may need to reprocess anything that called it
  - Need to take care with recursive calls

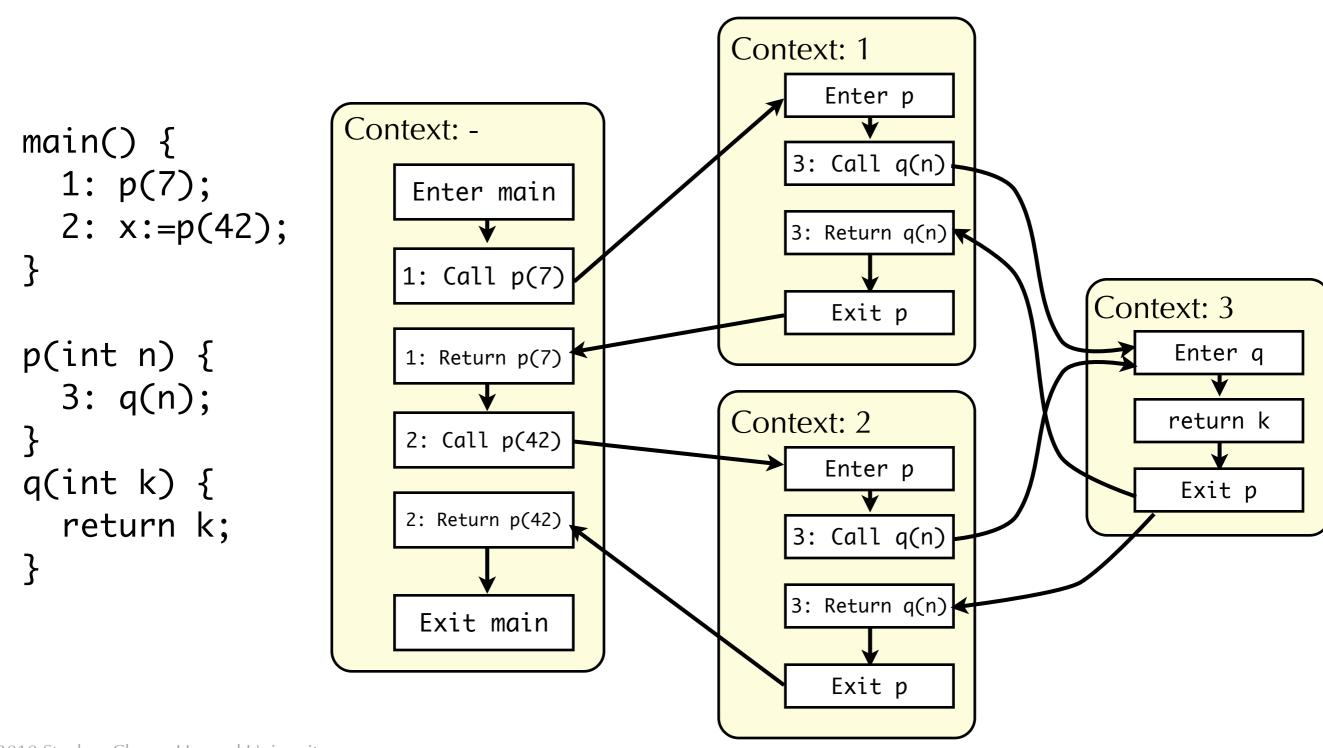
# Flow-sensitivity

- Recall: in a **flow insensitive** analysis, order of statements is not important
  - e.g., analysis of  $c_1$ ; $c_2$  will be the same as  $c_2$ ; $c_1$
- Flow insensitive analyses typically cheaper than flow sensitive analyses
- Can have both flow-sensitive interprocedural analyses and flow-insensitive interprocedural analyses
  - Flow-insensitivity can reduce the cost of interprocedural analyses

### Infeasible paths

- Context sensitivity increases precision by analyzing the same procedure in possibly many contexts
- But still have problem of infeasible paths
  - Paths in control flow graph that do not correspond to actual executions

### Infeasible paths example



## Realizable paths

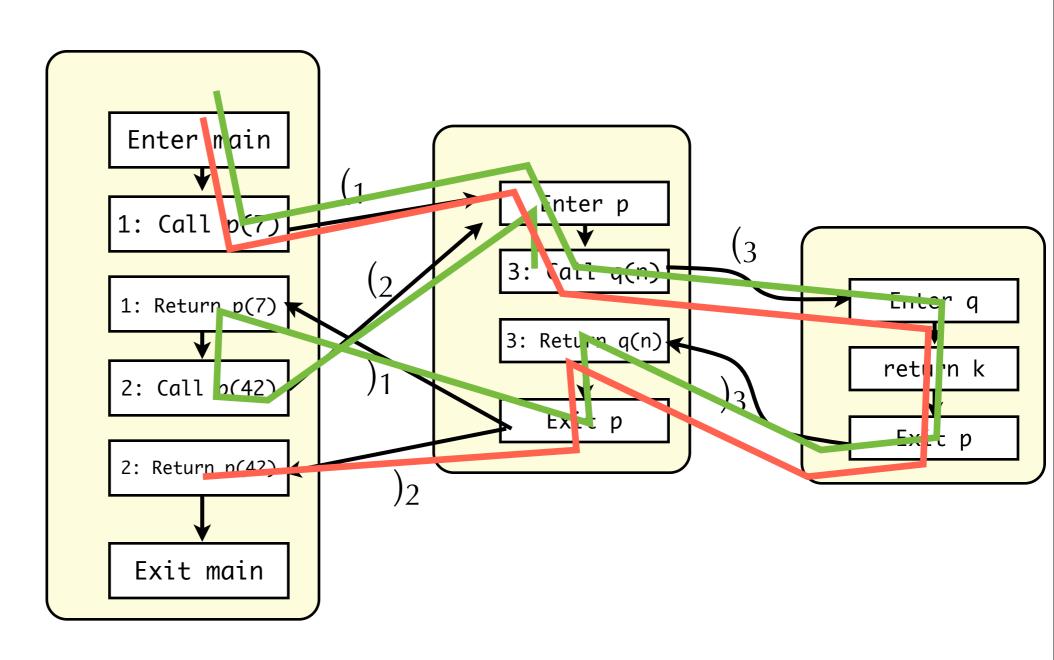
- Idea: restrict attention to realizable paths: paths that have proper nesting of procedure calls and exits
- For each call site *i*, let's label the call edge "(*i*" and the return edge ")*i*"
- Define a grammar that represents balanced paren strings

- Corresponds to matching procedure returns with procedure calls
- Define grammar of partially balanced parens (calls that have not yet returned)

#### Example

```
main() {
   1: p(7);
   2: x:=p(42);
}

p(int n) {
   3: q(n);
}
q(int k) {
   return k;
}
```



#### Meet over Realizable Paths

- Previously we wanted to calculate the dataflow facts that hold at a node in the CFG by taking the meet over all paths (MOP)
- But this may include infeasible paths
- Meet over all realizable paths (MRP) is more precise
  - For a given node *n*, we want the meet of all realizable paths from the start of the CFG to *n*
  - May have paths that don't correspond to any execution, but every execution will correspond to a realizable path
  - realizable paths are a subset of all paths
  - ⇒ MRP sound but more precise: MRP 

    MOP

# Program analysis as CFL reachability

- Can phrase many program analyses as contextfree language reachability problems in directed graphs
  - "Program Analysis via Graph Reachability" by Thomas Reps, 1998
    - Summarizes a sequence of papers developing this idea

# CFL Reachability

- Let L be a context-free language over alphabet Σ
- Let *G* be graph with edges labeled from Σ
- Each path in G defines word over Σ
- A path in G is an **L-path** if its word is in L
- CFL reachability problems:
  - All-pairs L-path problem: all pairs of nodes n<sub>1</sub>, n<sub>2</sub> such that there is an L-path from n<sub>1</sub> to n<sub>2</sub>
  - Single-source L-path problem: all nodes  $n_2$  such that there is an L-path from given node  $n_1$  to  $n_2$
  - Single-target L-path problem: all nodes n<sub>1</sub> such that there is an L-path from n<sub>1</sub> to given node n<sub>2</sub>
  - Single-source single-target L-path problem: is there an L-path from given node n<sub>1</sub> to given node n<sub>2</sub>

# Why bother?

- All CFL-reachability problems can be solved in time cubic in nodes of the graph
- Automatically get a faster, approximate solution: graph reachability
- On demand analysis algorithm for free
- Gives insight into program analysis complexity issues

# Encoding 1: IFDS problems

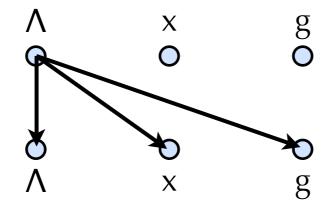
- Interprocedural finite distributive subset problems (IFDS problems)
  - Interprocedural dataflow analysis with
    - Finite set of data flow facts
    - Distributive dataflow functions ( $f(a \sqcap b) = f(a) \sqcap f(b)$ )
- Can convert any IFDS problem as a CFL-graph reachability problem, and find the MRP solution with no loss of precision
  - May be some loss of precision phrasing problem as IFDS

#### Encoding distributive functions

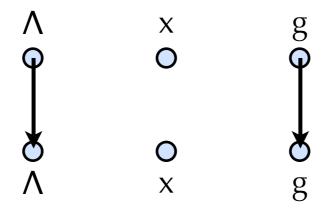
- Key insight: distributive function  $f:2^D \rightarrow 2^D$  can be encoded as graph with 2D+2 nodes
- W.L.O.G. assume ⊓ ≡∪
- Edge  $\Lambda \rightarrow d$  means  $d \in f(S)$  for all S
- Edge  $d_1 \rightarrow d_2$  means  $d_2 \notin f(\emptyset)$  and  $d_2 \in f(S)$  if  $d_1 \in S$
- Edge  $\Lambda \rightarrow \Lambda$  always in graph (allows composition)

# Encoding distributive functions

•  $\lambda S. \{x,g\}$ 

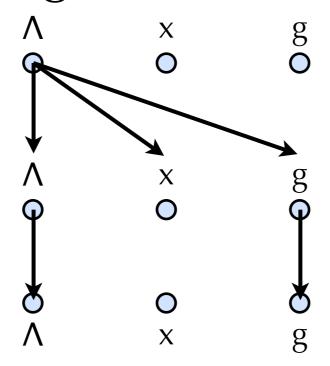


 $\bullet \lambda S. S-\{x\}$ 



# Encoding distributive functions

•  $\lambda S. S-\{x\} \circ \lambda S. \{x,g\}$ 



# Exploded supergraph G#

- Let *G*\* be supergraph (i.e., interprocedural CFP)
- For each node  $n \in G^*$ , there is node  $\langle n, \Lambda \rangle \in G^*$
- For each node  $n \in G^*$ , and  $d \in D$  there is node  $\langle n,d \rangle \in G^*$
- For function f associated with edge  $a \rightarrow b \in G^*$ 
  - Edge  $\langle a, \Lambda \rangle \rightarrow \langle b, d \rangle$  for every  $d \in f(\emptyset)$
  - Edge  $\langle a, d_1 \rangle \rightarrow \langle b, d_2 \rangle$  for every  $d_2 \in f(\{d_2\}) f(\emptyset)$
  - Edge  $\langle a, \Lambda \rangle \rightarrow \langle b, \Lambda \rangle$

Possibly uninitialized variable example

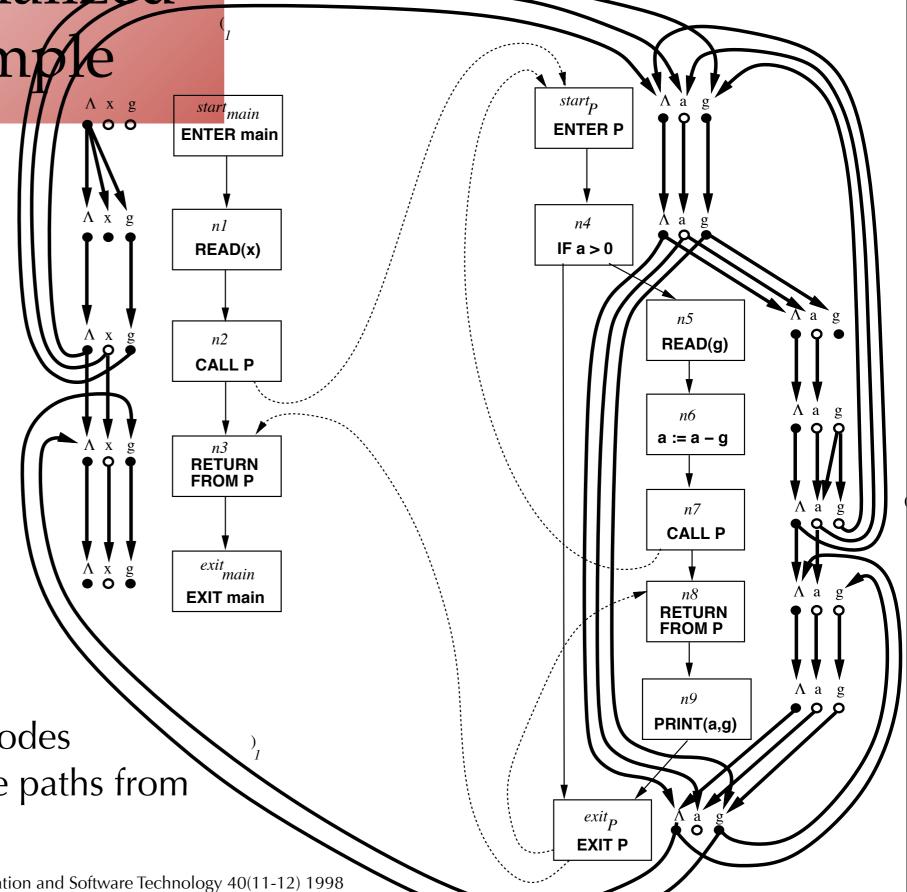
declare g: int

procedure main begin declare x: int read(x) call P(x) end

procedure P (value a: int)
begin
 if (a > 0) then
 read(g)
 a := a - g
 call P(a)
 print(a, g)
 fi
end

• Closed circles represent nodes reachable along realizable paths from  $\langle \text{start}_{\text{main}}, \Lambda \rangle$ 

Program Analysis via Graph Reachability by Reps, Information and Software Technology 40(11-12) 1998



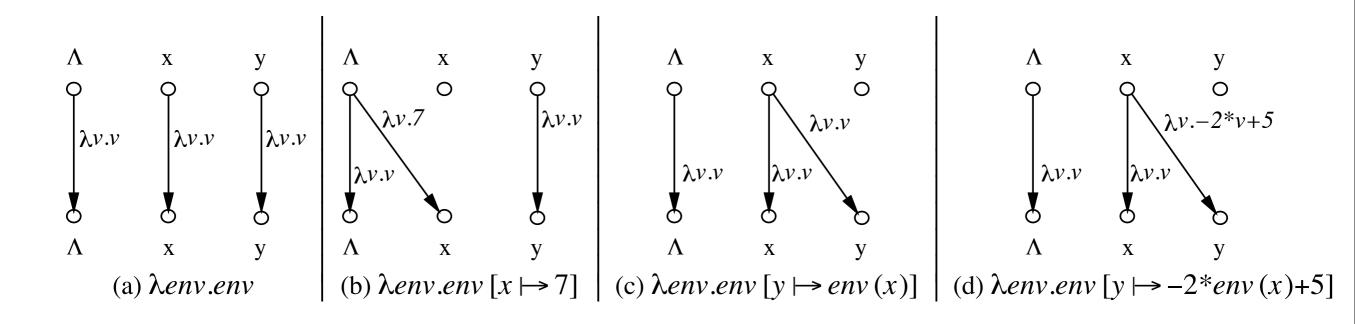
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# Encoding 2: IDE problems

- Interprocedural Distributive Environment problems (IDE problems)
  - Interprocedural dataflow analysis with
    - Dataflow info at program point represented as a finite environment (i.e., mapping from variables/locations to finite height domain of values)
    - Transfer function distributive "environment transformer"
  - E.g., copy constant propagation
    - interprets assignment statements such as x=7 and y=x
  - E.g. linear constant propagation
    - also interprets assignment statements such as y = 5\*z + 9

#### Encoding distributive environment-transformers

- Similar trick to encoding distributive functions in IFDS
- Represent environment-transformer function as graph with each edge labeled with microfunction



# Solving

- Requirements for class F of micro functions
  - Must be closed under meet and composition
  - F must have finite height (under pointwise ordering)
  - f(l) can be computed in constant time
  - Representation of f is of bounded size
  - Given representation of  $f_1$ ,  $f_2 \in F$ 
    - can compute representation of  $f_1 \circ f_2 \in F$  in constant time
    - can compute representation of  $f_1 \sqcap f_2 \in F$  in constant time
    - can compute  $f_1 = f_2$  in constant time

# Solving

- First pass computes jump functions and summary functions
  - Summaries of paths within a procedure and of procedure calls, respectively
- Second pass uses these functions to computer environments at program points
- More details in "Precise Interprocedural Dataflow Analysis with Applications to Constant Propagation" by Sagiv, Reps, and Horwitz, 1996.